An overview of underwater sound generated by inter-particle collisions and its application to the measurements of coarse sediment bedload transport

P. D. Thorne

National Oceanography Centre, Joseph Proudman building, 6 Brownlow Street, Liverpool, L3 5DA, UK

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Correspondence to: P. D. Thorne (pdt@noc.ac.uk)

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Abstract

Over the past two to three decades the concept of using sound generated by the inter-particle collisions of mobile bed material, has been investigated to assess if underwater sound can be utilised as a proxy for the estimation of bedload transport. In principle the acoustic approach is deemed to have the potential to provide non-intrusive, continuous, high temporal resolution measurements of bedload transport. It has been considered that the intensity of the sound radiated should be related to the amount of mobile material and the frequency spectrum to the size of the material. To be able to fully realise this use of acoustics requires an understanding of the parameters which control the generation of sound as particles impact. In the present work the aim is to provide marine scientists developing acoustics to measure bedload transport with a description of how sound is generated when particles undergo collision underwater. To investigate the properties of the sound generated, examples are provided under different conditions of impact. It is considered that an understanding of the origins of the sound generation, will provide a basis for the interpretation of acoustic data collected in the marine environment, for the study of bedload sediment transport processes.

1 Introduction

The measurement of bedload transport in rivers, estuarine and coastal environments is generally a difficult parameter to obtain. In particular regarding coarse sediment transport, gravels and cobbles, a number of methods have been developed to measure bedload transport rates. Many measurements have utilised box or tray samplers and this approach is still common today. Hubbell (1964), Engel and Lam Lau (1981), Bunte et al. (2008) and Holmes (2010), along with many others, have considered this technique. Some of the major shortcomings of this direct sampling method are: the impact on the flow introduced by of the sampler itself; the lack of spatial/temporal resolution;
the variable efficiency of samplers; the problems in obtaining continuous records; and other difficulties specific to the particular samplers.

To circumvent some of these difficulties alternative measurement technologies have been investigated. Dorey et al. (1975) investigated, with limited success, the feasibility of using sidescan sonar to track acoustically transponding pebbles. The tagging of gravel particles radioactively was developed by Crickmore et al. (1972) and applied with success to monitoring the movement of gravel. Reid et al. (1984) utilised artificial pebbles constructed with a ferrite rod at its centre and deployed them in a brook. Particle mobility was detected using an electromagnetic sensing system installed in the bed and transport compared with the bed shear. Geophones and particle impacts on pipes, columns and plates are now commonly used to estimate coarse gravel transport (Grey et al., 2010). In recent years acoustic Doppler velocity profiles, ADCP’s, have been used to measure apparent bedload velocity using a combination of ADCP bottom tracking velocity and boat velocity derived from differential global positioning systems, DGPS (Rennie and Church, 2010).

Another approach adopted, and the one focussed upon here, has been to monitor the movement of gravel by recording the acoustic sediment generated noise, SGN, arising from particle-particle collisions as bedload transport occurs. Observations of this type have continued to be reported; Bedeus and Ivicsics (1963), Johnson and Muir (1969), Tywoniuk and Warnock (1973), Jonys (1976), Richards and Milne (1979), Thorne et al. (1984), William et al. (1989), Mason et al. (2007), Camenen et al. (2012) and Basset et al. (2013). The appeal of the acoustic approach is that it offers the potential to obtain, with very little interference with the state of the bed and the flow, the initiation of particle movement, continuous temporal records, sub-second assessment of mass transport rates and estimates of mobile particle size.

To be able to utilise and interpret SGN with any degree of confidence requires an understanding of the sound source generation. The source arises from the impact of two or more particles as interparticle collisions occur as the bed becomes mobile and bedload transport occurs. The generation of sound by impacting bodies has primarily
been examined in air, usually by parties interested in machine noise emissions (Banerji, 1916, 1918; Koss and Alfredson, 1973; Koss, 1974a, b; Akay and Hodgson, 1978a, b; Akay, 1978). It is this work which has been adapted for the study of acoustic radiation by colliding bodies underwater (Thorne and Foden, 1988; Thorne, 1990). The source of radiation has been labelled rigid body radiation due to the origin of the pressure disturbance being generated by the acceleration of the body, rather than due to the natural modes of vibration of the body (Koss and Alfredson, 1973). To solve the problem, each sphere is treated as an independent source which generates a transient that can be described by an impulse solution convolved with the acceleration time history during the collision. The impact process is assumed to be elastic so that a Hertzian acceleration description can be employed (Goldsmith, 1960). The sound field is then obtained from the sum of the two transients with due allowance for the phase shift due to the path difference from each sphere to the field point.

Using the rigid body radiation theory initial calculations have been carried out to elucidate the origins of the structure of the radiated signal in the time and frequency domain. To investigate how changes in impact parameters affected the time domain signal and the frequency spectrum a series of calculation were conducted. The intention of this work was to provide broad illustrations of the radiated signal response due to variation in impact. Some general features are identified and considered in the light of using SGN for the measurement of bedload transport. Some modelling of multiple impacts is presented as an analogy to the type of data that may be collected in a coastal or riverine environment.

2 Theory for the underwater sound generated by impacting spheres

The background theory for impacting spheres in water was developed in Thorne and Foden (1988) and only the results of the theoretical analysis are presented here. The geometry for the theory is given in Fig. 1. When solid elastic spheres collide the main source of sound generation is due to the rigid body radiation associated with
the deceleration of the impactor and the acceleration of the impactee. These produce a sound wave which radiates from the spheres into the water. To simplify the analysis presented here the first conditions assumed is $\rho_s/\rho_o \ll 1$, where $\rho_s$ is the density of spheres and $\rho_o$ the density of water. This condition is not strongly adhered to for marine gravels with densities of the order of 2500 kg m$^{-3}$, however, it does considerably reduce the complexity of the time domain solution and simply leads to an overestimate of the signal levels by 10–20%. The second condition is $r/a \gg 1$, where $r$ is the distance from the impacting spheres to the location at which the radiated sound is observed and $a$ is the radius of the spheres, this condition can generally be readily adhered to. The pressure, $P_s(t)$, in the time domain for a single particle undergoing Hertzian impact with a half sine wave acceleration profile (Goldsmith, 1960; Koss and Alfredson, 1973) can then be expressed as

$$
0 \leq t \leq t_o \\
P_s(t) = P_{to}\{(2\xi^2 - 1)\cos \pi \tau + 2\xi \sin \pi \tau - [(2\xi^2 + 1)\sin \pi \xi \tau + (2\xi^2 - 1)\cos \pi \xi \tau]e^{\pi \xi \tau}\} 
$$

(1a)

$$
t > t_o \\
P_s(t) = P_{to}\{[(1 - 2\zeta^2)\cos \pi \zeta(\tau - 1) - (2\zeta^2 + 1)\sin \pi \zeta(\tau - 1)]e^{-\pi \xi(\tau - 1)} \\
- [(2\zeta^2 + 1)\sin \pi \zeta \tau + (2\zeta^2 - 1)\cos \pi \zeta \tau]e^{-\pi \xi \tau}\} 
$$

(1b)

where $t_o$ is the duration time of the collision. The pressure wave, $P_p(t)$, from the impactor and the impactee pair, is the combined pressure with due allowance for the time delay of the impactor signal relative to the impactee signal as given below

$$
P_p(t) = P_s(t, a_1) + P_s[(t - T_d), a_2].
$$

(1c)
Equation (1) provides the time domain waveform for the sound radiated when one sphere impacts with another. A number of parameters are defined below,

\[
P_{t_0} = \frac{A\rho_0 a c U \cos \theta}{2r(4\xi^4 + 1)}
\]

\[
t_0 = 4.53 \left[ \left( \frac{1 - \sigma_1^2}{E_1 \pi} \right) + \left( \frac{1 - \sigma_2^2}{E_2 \pi} \right) \left( \frac{m_1 m_2}{m_1 + m_2} \right) \right]^{0.4} \left( \frac{a_1 + a_2}{Ua_1 a_2} \right)^{0.2}
\]

\[
A_1 = 2m_2/(m_1 + m_2), \quad A_2 = -(m_1/m_2)A_1, \quad \xi = ct_0/\pi a, \quad \tau = t/t_0.
\]

Here \( A \) is associated with acceleration, \( m \) is the sphere mass, \( E \) Young's modulus, \( \sigma \) Poisson's ratio for the spheres and subscripts (1) and (2) refer to the impactee and the impactor. \( T_d \approx a_1(1 + \pi/2)/c \) for \( \theta = 0 \) and \( T_d \approx 2a \cos \theta/c \) when \( a_1 = a_2 \) and \( \theta > 0 \), where \( \theta \) is the angle between the line of sphere movement and the direction to the field point.

Similar expressions can be obtained for the frequency spectrum when two spheres collide and these are given below.

\[
P_s(f) = P_{f_0} \frac{1 + e^{-i\pi \epsilon}}{1 - \epsilon^2} \frac{\xi a + i \epsilon}{2\xi^2 - \epsilon^2 + 2i\xi \epsilon}
\]

\[
P_p(f) = P_s(f, a_1) + P_s(f, a_2) e^{-i\omega T_d}
\]

\[
\epsilon = \frac{f}{f_0}, \quad f_0 = 1/2t_0, \quad \omega_0 = 2\pi f_0 \quad i = \sqrt{-1}.
\]

To illustrate the sound generated when one particle impacts with another, Fig. 2 shows how the structure of the pressure wave is formed. The predicted underwater rigid body...
radiation for two spheres impacting was computed using Eqs. (1) and (2). Glass sphere properties were chosen for the calculations to represent marine shingle as both materials are often composed of silicates. For the calculation presented in Fig. 2, the velocity of sound and the density of water were respectively taken to be $1480 \text{ m s}^{-1}$ and $1000 \text{ kg m}^{-3}$, for the colliding spheres $a_1 = a_2 = 0.02 \text{ m}$, $\rho_s = 2500 \text{ kg m}^{-3}$, $U = 0.3 \text{ m s}^{-1}$, $r = 0.3 \text{ m}$, $\theta = 0^\circ$, $E = 7 \times 10^{10} \text{ N m}^{-2}$ and $\sigma = 0.2$ (Kaye and Laby, 1986). In Fig. 2a, the time series solution is presented. The first signal to arrive is from the accelerating impactee, this consists initially of a compressive peak from the surface of the sphere closer to the receiver, followed by a rarefaction from the rear surface. After a delay $T_d$ the signal from the impactor arrives. This is phase inverted due to the impactor decelerating in the direction towards the receiver, thereby giving initially a rarefaction followed by a compression peak. The total signal from the two spheres can be seen to have a “M” waveform. The spectrum, obtained using Eq. (2), can be seen in Fig. 2b. The spectrum is oscillatory in form peaking at $f \approx 1.7f_o$, with nulls at $f = (2n + 1)f_o$ where $n$ is an integer and with the spectrum reducing to negligible values above $7f_o$. The oscillations in the spectrum are associated with the term arising from the Fourier transform of the half sinusoidal acceleration profile. Software to calculate the impact radiation is given at http://noc.ac.uk/using-science/products/software/csr-acoustic-inversionsProgram(4)glass_sphere_impact_paper.m.

3 Prediction for the radiated sound and comparisons with laboratory observations

3.1 Single particle pair impacts

The aim here was to provide insight into the structure of the rigid body radiation field as impact parameters were varied. Therefore a number of calculations for the time domain waveform and the frequency spectrum were carried out. Initially spheres of equal size were considered with radii of 0.005, 0.015 and 0.05 m. For the calculations Eqs. (1)
and (2) were evaluated with all the others parameter having the same values as used to obtain Fig. 2. Figure 3 shows the results of the computations. Considering the time domain waveforms shown in Fig. 3a–c, it can be observed that both the duration and amplitude, $P_p(t)$, of the waveform increase with sphere size. For spheres of equal size $A_2 = -A_1 = 1$, $\xi$ is constant and therefore it is the linear dependence of $P_{to}$ on $a$ which produces the increase in amplitude with sphere size. The duration of the waveform is controlled by $t_o$ and $T_d$ and for equal sized spheres both are a linear function of $a$ and therefore the waveform duration linearly increases with sphere size. For the spectra shown in Fig. 3d–f the spectrum shifts to lower frequencies and increases in amplitude as sphere size increases. The shift to lower frequencies is due to the inverse relationship between $f_o$ and $t_o$ and hence $f_o\alpha_{1}/a$. For the spectral amplitude, $P_p(f)$, it is a function of $a/\omega_o$ with $\omega_o$ being dependent on $1/a$ through $t_o$, hence $P_p(f)$ is proportional to $a^2$ as seen in the plots. In Thorne and Foden (1988) a number of comparisons were made between predictions and measurements of impacting steel spheres underwater, the results supported the rigid body impact model. Two cases of glass spheres impacting underwater were also made and the results for $a_1 = a_2 = 0.015$ m case are compared with predictions in Fig. 3b and e where is can be seen that the predictions from rigid body radiation compare very favourably with the observations.

In the marine environment particles of different size will generally be impacting and it is therefore interesting to examine this case. To assess the radiated sound field from spheres of different size impacting, calculations were carried out using the same parameters as used for Fig. 3, but with the individual impacting spheres having a different radius. The results are presented in Fig. 4 and can be directly compared with the plots in Fig. 3. In the frequency spectrum plots in Fig. 4 the vertical solid and dashed lines respectively show the location of the spectral peak for the same size spheres impacting with radii $a_1$ and $a_2$ respectively. For the case of $a_1 = 0.005$ m and $a_2 = 0.015$ m the time domain waveform and frequency spectrum are given in Fig. 4a and d. Relative to the case of $a_1 = a_2 = 0.005$ m shown in Fig. 3a and d, the time domain signal is 50% longer in duration and 25% higher in amplitude, while the location of the peak frequency in the
spectrum has reduced by 20%, lying between the two vertical lines, and with a spectral amplitude which has doubled. Comparing the results for \( a_1 = 0.005 \text{ m} \) and \( a_2 = 0.015 \text{ m} \) with \( a_1 = a_2 = 0.015 \text{ m} \) in Fig. 3b and e, the converse is the case, with the duration and amplitude of the time domain waveform being reduced and the location of the peak frequency in the spectrum doubled and the spectral amplitude significantly lower. Colliding spheres of different size therefore have an admixture of properties of the accelerating impactee, \( a_1 \), and the decelerating impactor, \( a_2 \). Figure 4b–e and c–f further illustrates this admixture when compared with results presented in Fig. 3.

To assess how changes in the impact velocity, \( U \), and the field point angle, \( \theta \), had on the time domain waveform and the frequency spectrum, a number of calculations were carried out and the results are presented in Fig. 5. For these calculations \( a_1 = a_2 = 0.015 \text{ m} \) and apart from the changes in \( U \) and \( \theta \) all other parameters were the same as used for the calculations shown in Fig. 2. As shown in Fig. 5a and b an increase in \( U \) has a marginal influence on the duration of the time domain waveform and the frequency spectrum covered, with the main response being an increase in signal amplitude. The former is due to the weak dependence of \( t_0 \) on \( U^{-0.2} \), while inspection of Eqs. (1) and (2), for \( \xi > 1 \), shows the signal amplitude can be approximated as being proportional to \( U/\xi^2 \) which due to \( \xi \) dependence on \( t_0 \) results in a signal amplitude related to \( U^{1.4} \). For the changes in \( \theta \), the response is observed in Fig. 5c and d, where an increase in \( \theta \) has the primary response of decreasing the signal amplitude and a second order effect of reducing the duration of the time domain waveform and broadening the frequency spectrum, although the location of the peak frequency in the spectrum remains essentially unchanged. The significant reduction in signal amplitude is owing to the \( \cos(\theta) \) term in \( P_{to} \), \( P_{fo} \) and \( T_d \), which leads to the signal amplitude being dipole in form, reducing approximately as \( \cos^2(\theta) \), while the decrease in pulse length and broadening of the spectrum is due to the reduction in \( T_d \).

The implications from the results presented in Figs. 3–5 are that to first order the duration of the time domain waveform, the width of the spectrum and the frequency at which the spectrum peaks, are principally controlled by the size of the spheres.
impacting, while the amplitude of the time domain waveform and frequency spectrum depend upon sphere size and impact velocity, with the additional factor of the dipole structure for the amplitude of the radiated field.

### 3.2 Multiple particle pair impacts

Laboratory measurements on multiple particles impacting have been carried out by Jonys (1976), Millard (1976) and Thorne (1985, 1986a). The works of Thorne incorporated the results of the earlier works and are still the most comprehensive study of the underwater sound radiated from multiple collisions of quasi-bedload transport and therefore the measurements from these two papers are used here to illustrate the salient acoustic features.

The instrumentation used has been previously described (Thorne, 1985) therefore only a brief description is given here. Sediments were agitated in a vertical wooden drum 1 m in diameter and 0.5 m deep, this rotated about a horizontal axis and was totally submerged underwater in a concrete tank 3 m × 2 m × 2 m. The drum was lined with an expanded polystyrene sheet 0.002 m thick to ensure that the only significant collision noise generated was due to interparticle collisions. The front of the drum was open, apart from a small lip around the circumference to retain the sediments, thereby allowing hydrophones (underwater sound receivers) to be placed at any position inside the drum while the material was being agitated. The output from the hydrophones was fed into a low-noise amplifier, then through a filter with a passband between 1–600 kHz, and in parallel into an signal envelope detector and a spectrum analyzer. The results were corrected for background noise, instrumentation frequency response and the effect of measuring in a confined reverberant environment, to yield effectively free-field amplitude and spectra levels. The measurements in the rotating drum were intended to simulate quasi-bedload like transport and impacts. Measurements were carried out on glass spheres ranging in radius between \( a = 0.0018–0.015 \) m and gravels between \( a = 0.0015–0.0125 \) m. In Figs. 6 and 7 some of the measurements are compared with predictions from the rigid body model of acoustic radiation due to impact.
Presented in Fig. 6 are the spectrum for particles centred on nominal radii of 0.00075, 0.0015 and 0.005 m. In Fig. 6a data for spheres and gravel of radius of 0.005 m are shown, both data sets are broadband in nature with spectral peaks frequencies being around 15 kHz. The fact that spectral levels are lower for the gravel is not necessarily significant because measurements were made under different conditions of mass and rotation speed. Owing to the impact velocities, number of particles impacting and the value of $\theta$ not being well specified in the rotating drum experiments, the output from the rigid body radiation calculations were scaled to the observations. The comparison is therefore between the modelled and measured spectral form. Further when multiple particle size pairs of slightly different effective sizes and velocities are impacting simultaneously, marginally different overlapping frequency spectrums are summed at the receiver. Therefore for the rigid body calculations the spectra have been smoothed to reduce the oscillations in the spectrum observed in the previous figures associated with only a single size particle pair impacting. As can be seen in Fig. 6a the smoothed rigid body radiation spectra compare reasonably well in form with the sphere and gravel spectra, although, particularly for the gravel, the data does not appear to reduce in amplitude at the lower frequencies as much as the model suggests. This was a common and unresolved observation for gravel across most of the measurements (Thorne, 1986a, 1990). In Fig. 6b, results for 0.0015 m glass spheres and 0.00075 m gravel are shown and the measurements clearly show a separation in the spectra with the smaller gravel material having a maximum in the spectrum at twice the frequency of that of the glass spheres. Comparison of the predicted spectrum with the observations again captures the broadband nature of the sound, the location of the maximum in the spectrum, the roll off at the higher frequencies and the smaller material having a maximum amplitude at a higher frequency, however, as with the cases in Fig. 6a, the modelled lower frequency components are underestimated.

To represent the variation of the spectra with particle size, the frequency at which the spectrum nominally peaks, or the centroid of the spectrum, has been used to define a characteristic central frequency. This is illustrated in Fig. 7a where results from the
studies of Jonys (1976), Millard (1976) and Thorne (1985, 1986a) are presented. What can be clearly seen is that the characteristic central frequency has to first order an inverse dependency on particle size. From rigid body radiation theory the frequency at which the spectrum peaks, \( f_{pk} \), can be seen in Fig. 2b to be approximately given by \( 1.7f_o \) where \( f_o = 1/2t_o \). For simplicity if the assumption is made that particles of equal size are impacting the expression for \( t_o \) can be simplified and this allows \( f_{pk} \) to be expressed as

\[
 f_{pk} = 0.15 \left\{ \frac{E}{\rho_s(1 - \sigma^2)} \right\}^{0.4} U^{0.2} a. \tag{3}
\]

All the parameters in Eq. (3) were known apart from the particle impact velocities in the rotating drum. Typical circumferential drum speeds of 0.3 m s\(^{-1}\) were used so impact velocities in the range of 0.01–0.1 m s\(^{-1}\) would not seem unreasonable and were therefore used in the evaluation of Eq. (3) to obtain the lines in Fig. 7a. The data generally lie between the two lines thereby indicating that Eq. (3) is probably a reasonable description for a characteristic central frequency for the broadband impact spectrum, with, guided by Fig. 2b, the significant section of the spectrum lying in the frequency band between approximately \( f_{pk}/4 \)–\( 4f_{pk} \).

In the marine environment the amount of material transported as bedload will vary over time depending on the size of the sediments on the bed and the hydrodynamic conditions. To simulate this variability a series of measurements were carried out on gravels of different radii, with \( a = 0.0012, 0.0024, 0.005, \) and 0.0085 m where the mass of sediments in the drum, \( M \), was increased at constant rotation speed. Treating the interparticle impacts in the drum as similar random independent noise sources the total signal can be expressed as (Beranek, 1971)

\[
P^2 = \sum_{i=1}^{N} P_i^2 \approx N\bar{P}^2 \tag{4}
\]

where \( N \) is the number of sources, \( P_i^2 \) are the individual source pressure levels squared, the over-bar represents a mean value and \( P^2 \) is the total mean squared
pressure. As $N$ is proportional to $M$, then $P^2$ should be approximately linearly dependent on $M$. Figure 7b shows the results of the measurements and the line represents Eq. (4). Although there is some variability in the four data sets the general slope of the data is consistent with a linear relationship between $P^2$ and $M$.

In general therefore, it can be seen that the relatively simple rigid body radiation model captures in broad terms the form of the spectrum for large numbers of particles impacting in a quasi-bedload like manner, although for reasons not resolved in the present analysis the lower frequency components are somewhat under predicted. The spectrum can be broadly specified with having a characteristic central frequency which is inversely related to particle size and with a bandwidth nominally between $f_{pk} / 4–4f_{pk}$. Finally to represent increases in bedload, the amount of material in the drum was gradually increased at a constant rotation speed, which resulted in the mean squared pressure increasing linearly with mass.

4 Example from a field study

There have been a number of field trials of the SGN technique and the results have been variable (Bedeus and Ivicsics, 1963; Tywoniuk and Warnock, 1973; Jonys, 1976; Richards and Milne, 1979; Thorne et al., 1989; Williams et al., 1989; Voulgaris et al., 1995; Mason et al., 2007; Barton et al., 2010; Belleudy, 2010; Bassett et al., 2013). One of the more successful and interesting studies was to utilise the non-intrusive high temporal resolution measuring capability of SGN to examine the relationship between turbulent bursting in tidal flows and the bedload transport of coarse gravels (Heathershaw and Thorne, 1985; Thorne et al., 1989). Using an instrumented frame, concurrent measurements of the three orthogonal components of the turbulent flow and instantaneous bedload transport, were collected above a gravel bed in a tidally dynamic environment with currents peaking at around 1.0 m s$^{-1}$ at 1 m above the bed. High resolution bedload transport measurements were derived from two hydrophones measuring the SGN and calibrated in-situ for bedload transport using visual
measurements of sediment transport using an underwater video camera (Thorne, 1986b). The flow and acoustic measurements were respectively collected at 0.33 and 0.24 m above the bed and the synchronised data digitised at 5.0 Hz and recorded. From the turbulent flow measurements the kinematic Reynolds stress were calculate using $-\mu w \text{ m}^2 \text{s}^{-2}$, where $u$ and $w$ were respectively the horizontal and vertical fluctuating turbulent components of the flow. From the acoustic calibration it was shown that the SGN acoustic intensity, $I \mu \text{W m}^{-2}$, which is proportional to the squared pressure, was an acceptable surrogate for bedload transport. Applying a quadrature analysis to the kinematic Reynolds stress, events in the flow were identified as sweeps ($u > 0$, $w < 0$), ejections ($u < 0$, $w > 0$), outward ($u > 0$, $w > 0$) and inward ($u < 0$, $w < 0$) interactions and compared with the corresponding values for $I$. The results of the analysis are shown in Fig. 8.

The measurements demonstrated quite clearly in Fig. 8a and b that the acoustic intensity, and hence gravel transport, associated with sweep events were substantially higher than the intensity levels during ejection events at high stress values. This difference increased as the magnitude of the kinematic stress increased. From this it was concluded that of the two types of motion that contributed to the bulk of the kinematic Reynolds stress, ejections and sweeps, only sweeps were capable of supporting appreciable coarse sediment movement. It was also noted that unexpectedly outward interaction events, although weaker and less frequent than sweeps, as shown in Fig. 8c and e, were capable of supporting greater sediment movement than sweeps for the same stress levels. This is despite the fact that they make a negative contribution to the Reynolds stress. Correspondingly, there was little sediment movement associated with inward interactions. The results showed that horizontal turbulent velocity fluctuations, $u$, may have greater dynamical significance in terms of coarse sediment movement, than the instantaneous contributions, $-\mu w$, to the Reynolds stress. Also vertical fluctuations were considered as important provided they were associated with increases in $u$. This was the case for outward interactions, Fig. 3c, where $w > 0$ indicated additional lift on exposed gravel particles by fluid moving away from the bed. This, in turn was
considered to account for sediment transport rates being higher than those of similar sized sweeps. The observed close dependence on $u$ was considered explainable if the gravel was moved principally by form drag acting on the flow-normal projected area of exposed particles. To examine this a correlation analysis between the total horizontal flow, $U$, and $I$ and Reynolds stress, $-\rho_o \overline{uw}$, and $I$ were carried out. The results of the analysis showed that in all cases sediment movement was better correlated with form drag than with the instantaneous stress.

This study illustrated that SGN can provide detailed high temporal resolution measurements of sediment response to turbulent flow conditions and showed for the first time that the bedload movement of seabed gravels is caused principally by sweep–type motions in the bottom boundary layer and to a lesser extent by outward interactions. This observation could be explained if form drag rather than shear stress was assumed to be the principle cause of gravel movement. It was speculated that such relationships between sediment transport and turbulent motions could lead to a new generation of sediment transport equations which accounted for the turbulent bursting process (Clifford et al., 1995; Williams, 1996; Sumer et al., 2003).

5 Discussion and conclusion

The aim of the present paper has been to provide scientist and engineers, interested in the measurement of coarse sediment bedload transport, in coastal and riverine environments, with an overview of the background of sediment generated noise, SGN. When the bed becomes mobile interparticle collisions occur which radiate sound into the water and this SGN has been used as a proxy for bedload transport rates. To understand and predict the sound field generated by the collision of particles, a theoretical framework based on rigid body radiation has been utilised. Initially predictions were made with colliding pairs of glass spheres and the impact of sphere size, impact velocity and field point angle examined to assess the effect these had on the measured time domain signal and the frequency spectrum. Limited comparison with available data was
carried out to assess the veracity of the theory. To move beyond simple two particle impacts, larger numbers of particles were impacted using a rotating drum arrangement, this experimental configuration was employed to simulate quasi-bedload conditions. In these studies data were collected on glass spheres and natural gravels. Spectral analysis of the measurements showed comparable spectra to the two sphere impact results and rigid body radiation gave reasonable first order agreement with the rotating drum data. Assessment of a characteristic central frequency for the spectra showed a clear inverse relationship with the size of the impacting particles and an expression derived from the impact duration of the collision time, $t_0$, given by Eq. (3), provided a reasonable description for the observations. To establish a relationship between the amount of material impacting in the rotating drum and the mean square signal level recorded, measurement were carried out for a number of different particle sizes at constant drum rotation speed. The results showed that the mean square signal level was proportional to the amount of material in the drum and hence ostensibly the number of collisions. To explain the observations the interparticle impacts in the drum were considered to be similar random independent noise sources which summed linearly with the mean square pressure.

The outcome from the two sphere impact studies and the measurements in the rotating drum indicated that the relatively simple Eqs. (1)–(4), derived from rigid body radiation, and the linear summation of mean square pressures, provide a framework for a first order understanding of SGN. The results showed that for pairs of spheres impacting the amplitude of the signal is a function of the sphere size, impact velocity and the location of the position of observation. For measurements of bedload in the field, the location of the receiver will normally remain fixed relative to the bed and the size of the bedload material will be nominally constant, therefore the signal amplitude will essentially depend on the impact velocity and the number of particles impacting. If it is assumed that impact velocity is proportional to the velocity on the mobile material, then the mean square signal amplitude should be acting ostensibly as a nominal proxy for the bedload transport and this has been reported in a number of studies (Johnson et al., 2014).
and Muir, 1969; Thorne, 1986b; Barton et al., 2010). The form of the spectrum has been showed to be primarily dependent on the size of the impacting particles, with the impact velocity and measurement location having only second order effects. The form of the spectrum is therefore a reasonably robust indicator of the size of the mobile material and as such has been used to estimate the size of the bedload material (Thorne, 1986a; Mason et al., 2007; Belleudy et al., 2010; Basset et al., 2013).

One of the more common difficulties in the application of SGN to the measurement of coarse sediment bedload transport is the level of the background aquatic soundscape (Wenz, 1972; Thorne, 1986b; Vracar and Mijic, 2011). Contributions from biophony (sounds from aquatic animals), geophony (sounds from natural abiotic phenomenon) and anthrophony (sounds from manmade activities) can make interpretation and assessment of the SGN problematic. To-date most SGN measurements have been collected using nominally omnidirectional hydrophones. Looking to the future the mounting of such hydrophones in acoustically reflective housings to increase directionality (as with an omnidirectional bulb in a car headlight) and thereby rejecting erroneous background noise could be an interesting step forward. Also given that predictions can be made for the spectrum of the sound from a knowledge of particle size, this may be used with bandpass filtering to enhance the SGN signal relative to the general soundscape. One area which is still deficient is rigorous assessments of the SGN technique using independent measurements of coarse sediment bedload transport. Further studies in flumes and in the field would establish with greater veracity than available at present, the capabilities and uncertainties in the application of SGN to the robust measurement of bedload transport and particle size.

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References


Figure 1. Geometry for the theory.
Figure 2. Normalised solutions for (a) time domain Eq. (1) and (b) the frequency domain Eq. (2), for two glass spheres impacting with radius $a = 0.02$ m.
Figure 3. (a)–(c) Time domain waveform and (d)–(f) frequency spectrum, for spheres of the same size impacting as a increases. Measurements (●) from Thorne and Foden (1988).
Figure 4. (a)–(c) Time domain waveform and (d)–(f) frequency spectrum, for spheres of different size impacting. The vertical lines are the location of the peak frequencies for spheres of equal size impacting have respectively radii of the impactee, $a_1$ (–), and the impactor, $a_2$ (---).
Figure 5. Calculations for the time domain waveform and the frequency spectrum for $a = 0.0015$ m as velocity, $U$, is increased (a) and (b) and as the angle $\theta$ is increased (c) and (d).
Figure 6. Comparison of the measured and calculated spectra under quasi-bedload conditions in a rotating drum for; (a) 0.005 m radius glass spheres and gravel and (b) 0.0015 m radius glass spheres and 0.00075 mm radius gravel.
Figure 7. (a) Measured and calculated characteristic central frequency, $f_c$, with particle radius, $a$. (b) The mean square pressure, $P^2$, with mass, $M$. Both were collected under quasi-bedload conditions in a rotating drum.
Figure 8. Comparison of the proxy for sediment transport, acoustic intensity, due to (a) sweeps, (b) ejections, (c) outward interactions, (d) inward interactions and the number of events of the four kinematic stress quadrature components (e), (f), with the magnitude of the kinematic stress $|\mu w|$. 