Author’s Response to Reviewer A. Chappell

We would like to thank Adrian Chappell for his constructive comments. In this response we provide an answer to all the comments and the indicated changes will be applied in the revised manuscript. The line numbers in the answers to the Referee comments correspond to the lines in the marked-up manuscript that follows the response sections.

Comment 1: “I think equation 10 is a description of net soil redistribution by water. The $E$ provides gross water erosion and $1-f$ provides an adjustment based on the "remaining soil that has not been transferred to the floodplain directly". I think this approximation of net soil redistribution by water should be made clear as I think this emphasises the need for and significance of a net approach. I also think that (if I have understood the approach correctly) you should be able to validate your approximation against maps of net soil redistribution e.g., Australia. Note that 137Cs-derived maps for net soil redistribution across Australia include wind and water erosion and to validate only the water component the gross wind erosion would need to be removed (for which data is also available for Australia)”

Answer part 1: Our approach emphasizes the importance of simulating each of the main processes related to sediment dynamics by water, which are erosion, deposition and transport. As such, we do not only study the net export of sediment from a catchment but also explicitly represent both net and gross erosion. In order to clarify this, we rephrased the manuscript to emphasize these points. Equations 9 and 10 describe the soil redistribution flux by water in on hillslopes and in floodplains, respectively. The variable ‘f’ describes the fraction of the eroded sediment that is transported directly to the floodplains in the respective grid cell, while ‘1-f’ describes the fraction of eroded sediment that remains on the hillslopes in the respective grid cell. The change of sediment storage in the floodplains and hillslopes of a grid cell as a result of erosion, deposition and transport are then together a representation for the net soil redistribution in that grid cell.

Changes in the manuscript: Line 183: “…sediment loss. Equation 1 can also be seen as a representation for the net soil redistribution flux, and can be approximated by the following as function of time:”
Line 290: “The modelling approach as presented by the equations above focuses on the net soil redistribution by separately modelling the main processes of soil redistribution, which are erosion, deposition and transport. In the following paragraphs we will show how this modelling approach performs for the Rhine catchment.”

**Answer part 2:** We fully agree that a thorough validation of our approach in terms of net soil redistribution could provide valuable insights. However, reliable soil redistribution maps for large regions are very scarce. As suggested by the reviewer, we could use 137Cs-derived maps for net soil redistribution for Australia during the last ~50 years, to validate our results. However, we feel that this is outside the scope of our study where the focus is on millennial timescales. This could be done in a following-up study where we expand our modelling approach to other global catchments. It should be noted that 137Cs-derived maps represent soil redistribution for recent times, while in this study we focus on the soil redistribution for the last millennium. We have addressed this suggestion by adding the potential use of 137Cs-derived (and other approaches) on short-time scales as an outlook in the conclusions in the revised manuscript.

**Changes in the manuscript:** line 762: “The next steps in quantifying soil redistribution on the global scale will be to apply the sediment budget model on other large catchments or regions, and validate the model with existing data on net soil redistribution, sediment storage or yields.”

**Comment 2:** “I think I understand why you needed to choose a grid resolution for your study. However, if the modelling is to be used in global ESM then it will need to be independent of grid resolution. I suspect that its application to other larger and flatter catchments would be represented by much of your model but perhaps not in the assumption that 5 arcmin is optimal for representing floodplain and hillslope. For example, Australia has some very large catchments which could mean that your chosen grid resolution may have no floodplain. I agree that a finer resolution would also not work in many regions but would work in other very steep, rugged terrain regions.”

**Answer:** We agree that the model is currently limited to the resolution of 5 arcmin as it has been tested and calibrated for this specific resolution. We chose this particular resolution assuming that it includes both a hillslope and floodplain part for most of the Rhine catchment (and other catchments of similar size worldwide). We agree that if we want to make our model fully compatible with ESMs it would be good to make the model independent of grid resolution.
However, we see our study as a first step into this direction. An issue that has to be addresses is the delineation of floodplain areas at global scales. Derivation of floodplains from soil properties and types is found to be insufficient. We are currently experimenting with deriving floodplains from Digital Elevation Models (DEMs). However, this is still work in progress. We will address this issue in the conclusion part of the revised manuscript.

**Changes in the manuscript:** line 762: “The next steps in quantifying soil redistribution on the global scale are applying the sediment budget model on other large catchments, and validate the model with existing data on net soil redistribution, sediment storage or yields. Furthermore, in order to make the soil redistribution model better applicable on a global scale and to prevent conflict with the underlying assumption of the simultaneous presence of floodplains and hillslopes in each grid box, the model needs to be made independent of grid resolution.”

**Comment 3:** “There is very little justification for the model parameter values in section 2.2 (page 8). You may be interested in considering for this manuscript and future work whether your approximation for f is consistent with the Multi-resolution Valley Bottom Flatness (MrVBF) data for Australia can be found on the link below.


The land cover type and metrics are readily available Australia and presumably for present slope so that might provide additional calibration / validation for your model. I’m not convinced about the use of average slope (as opposed to median) and which will be influenced by the resolution of the grid.”

**Answer:** Thank you for this suggestion, we will consider this alternative approach in our further development of the model (see comment above). We can use this index to help identifying floodplains in a future study when applying the sediment budget model on a global scale (related to the previous comment). In addition to this we can then also use the data on land cover for Australia to validate our model. We will need to consider that due to the rapid changes of land use, recent maps are of limited use in our study that focuses on time-scales in the order of 1000 years.
Comment 4: ”I think if scaling is to be an important part of the paper, as demonstrated by section 3.1 and abstract, then some background on Hoffmann et al. (2013) needs to be included so that this topic in the manuscript is easier to comprehend.”

Answer: We will add in the revised manuscript more background on the scaling relationships found by Hoffmann et al. (2013) and why this scaling is an important feature that needs to be reproduced with our model.

Changes in the manuscript: Line 358: ”...linear. With these scaling relationships, for the first time, a direct comparison is made between the behavior of soil redistribution on hillslopes and in floodplains at large spatial scales. This is an essential difference between hillslopes and floodplains that sediment budget models like ours needs to capture in order to reliably simulate the spatial distribution of sediment on such a scale.

Line 370: „, With the estimated scaling coefficients (Eq.12 and Eq.13) Hoffmann et al. (2013) showed that even for large catchments (in the order of 10^5 km^2) hillslopes store an equal amount of sediment as floodplains. They pointed out that this is a substantial sink that needs to be considered in sediment budgets of large catchments.”

Comment 5: ”I think it reasonable to qualify the extent to which this modelling can be used generally within ESMs to model soil redistribution by making explicit the contribution of soil redistribution by wind. In many global regions and drier more gusty phases in the past (and potentially the future), wind erosion may be considerably more important than water erosion. In other semi-arid regions the interplay between downslope erosion by water and removal by wind may cause a net soil redistribution to tend towards little change for some long period. In any case, I think it may be worthwhile for modellers interested in implementing your model that the wind erosion and dust emission component is important for soil redistribution. I accept that these processes may not be particularly relevant in the Rhine but note that they are in the sandy previous outwash plains of other parts of Germany and NW Europe.”

Answer: We agree that soil redistribution by wind may play an important role for soil redistribution in many arid regions. Although we focus on soil redistribution by water in this study, generally considered to be the dominant erosion process at the global scale (e.g. Quinton et al., 2010) we will add some sentences in the revised manuscript in the conclusions and outlook
section on the importance of including soil redistribution by wind and other types of soil erosion in ESMs.

**Changes in the manuscript:** Line 768: “Finally to have a complete picture of the net soil redistribution and the feedbacks on the carbon and nutrient cycles, it is essential to model also other types of soil erosion, such as wind erosion (Chappell et al., 2015), tillage erosion (Van Oost et al., 2009) and gully erosion (Poesen et al., 2003).”

**Comment 6:** "I think the grammar and syntax of the manuscript need to be improved e.g., focus on consistent tenses. This might also be a good time to reduce the duplication of background material in the Introduction cf. start of Methods section. I think much of the technical justification might be moved from the Introduction to the start of the Methods section.”

**Answer:** We will work on improving the syntax and grammar in the revised manuscript and try to avoid the duplication of material.

**Comment 7:** “References need some attention e.g., Oost or Van Oost.”

**Answer:** We will correct for this mistake in the revised manuscript.
Author’s Response to Referee B. Guenet

We would first like to thank Bertrand Guenet for his constructive comments. In this response we provide an answer to all the comments and the indicated changes will be applied in the revised manuscript. The line numbers in the answers to the Referee comments correspond to the lines in the marked-up manuscript that follows the response sections.

Comment 1: "You used a modified version of the RUSLE equations without the support practice factor and then conclude that land use change is a driving factor of erosion. I think that you should discuss carefully how their conclusions would be impacted by the use of the support practice factor. In particular, how it could change the trends after the 1950’s and during the middle age when animal traction was more and more used to plough."

Answer: The exclusion of the support practice factor, which represents the effect of contouring, terracing, and subsurface drainage areas on erosion (Renard et al., 1997), may indeed impact the effect of land use change on erosion and the resulting sediment fluxes in regions with a long agricultural history, such as the Rhine catchment. However, our assumption that the factor equals unity in our study is consistent with a detailed assessment at the European scale where the average P factor for 2012 was estimated at 0.97 (Panagos et al., 2015). Furthermore, the study of Doetterl et al. (2012) showed that the S, R, C and K factors explain approximately 78% of the total erosion rates on cropland in the USA. This indicates that on cropland the L and P factors, which are related to agriculture and land management, contribute only for 22% to the observed variability in erosion rates. Thus, although we neglect these factors in agricultural regions where they may play an important role, we expect that this does not affect the overall results of our study, such as that land use change is the driving factor of erosion. We will comment on the exclusion of L and P in the discussion.

Changes in the manuscript: Line 663: “Neglecting the support practice (P) and slope-length (L) factors in agricultural regions, where they may play an important role, results in an overestimation of the increases of soil erosion especially during the 1950’s. However, we expect that this does not affect the overall trends. This assumption is also supported by Doetterl et al. (2012), who shows that the L and P factors explain only up to 22% of the variability in water erosion rates on cropland in the USA.”
Comment 2: "You used a modified version of RUSLE on non-croplands areas whereas this equation has been developed on croplands areas. I missed few sentences to justify that the use of RUSLE makes sense also for forest and grassland."

Answer: Indeed the original USLE model, the predecessor of RUSLE, was originally developed for cropland. However, as the model name already indicates, it is universal and can also be applied to forested and grassland areas. Model parameters for these land uses have been estimated using observational data and the model has been applied on a regular basis for the estimation of erosion in nature conservation areas, mine sites, forested areas and range- and grasslands (Dissmeyer, 1981; Millward and Mersey, 1999; Lu et al., 2004). We will include this short explanation in the methods section of the revised manuscript.

Changes in the manuscript: Line 220: “… global scale. Although, RUSLE was originally developed for agricultural land, model parameters for other land cover types such as forest and grassland have also been estimated using observational data (Dissmeyer, 1981; Millward and Mersey, 1999; Lu et al., 2004).

Comment 3: ”It would have been quite interesting to know the sensitivity of your approach to the inputs coming from the MPI-ESM using simulations coming from other ESMs. I am aware that this is asking a lot of additional work to redo everything using other ESMs outputs therefore adding just few elements in the discussion will be enough but at least it is important to mention it and to discuss how the uncertainties from the ESMs results might impact your conclusions.”

Answer: Indeed, the sensitivity of our model to input data can be tested using data from other ESMs. We expect that the input data from other ESMs may significantly alter the trends in erosion rates and sediment fluxes for the last millennium. This is due to the fact that ESMs simulate climate and land cover in different ways.

Changes in the manuscript: Line 647: “… R factor remain. It is therefore also important to test the sensitivity of the sediment budget model with input data on precipitation and land cover from other ESMs.”

Comment 4: ”The discussion refers several times to the land use history but without enough references. Please document better this part.”
**Answer:** We will add in the revised manuscript references to the studies of Hoffmann et al. (2007), Dix et al. (2005) and Kalis et al. (2003), who describe the long land use history of the Rhine catchment in more detail.

**Minor comments:** “L 133: You implicitly assume that movement of water during the flooding events do not induce erosion? If I understood well it should be clearly stated.”

**Answer:** We only focus on rill and interrill erosion (which is indicated in the paper line 165), and not gully erosion or stream bank erosion that are the more extreme forms of erosion and related to flooding.

**Changes in the manuscript:** None

“L 151: I am not sure to fully understand what at and bt mean physically. Please clarify.”

**Answer:** $a_t$ and $b_t$ in equation 3 are the adjustment parameters of our model relating the residence time to the flow-accumulation or catchment area. We will make this more clear in the revised manuscript.

**Changes in the manuscript:** Line 196: “$a_t$ and $b_t$ are the adjustment parameters of the model that relate the residence time to the Flowacc. Flowacc is the flow-accumulation and is defined as the number of grid cells….”

“L 355: Does it means that you use the same climate each year without inter-annual variability or do you repeat the sequence between 850 and 950 AD?”

**Answer:** We use the same yearly mean precipitation, temperature and the R factor, averaged over the 100-year period of 850-950AD (no inter-annual variability). In our study we calculated the R factor as an average over 100 year timeperiods starting from 850 AD and over a 50 year time period between 1950 and 2000.

“Fig. 4: Since it is scatter plot, you should fix the intercept to zero to have a better idea on how close to the 1:1 line the model is.”

**Answer:** We will include the 1:1 line in the figure in the revised manuscript.
“Supplementary material l 44: If I understood well these parameters are fixed during the
simulations? Why not use the stock of organic C predicted by the MPI ESM?”

**Answer:** Yes, the parameters to calculate the K factor, and the K factor itself are fixed during the
simulations. We didn’t use the C predicted by MPI-ESM because it is a very uncertain parameter
of the model and it is therefore better to use the data from GSCE. Also we assume that in the
timeperiod of the last millennium the K factor will not change drastically in a way that it can
change the erosion rates significantly.
Modelling long-term, large-scale sediment storage using a simple sediment budget approach

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Abstract.
Currently, the anthropogenic disturbances to the biogeochemical cycles remain unquantified due to the poor representation of lateral fluxes of carbon and nutrients in Earth System Models (ESMs) that couple the terrestrial and ocean systems. Soil redistribution plays an important role in the transport of carbon and nutrients between terrestrial ecosystems, however, quantification of soil redistribution and its effects on the global biogeochemical cycles is strongly affected by accelerated soil erosion rates. However, the quantification of global soil erosion by rainfall and runoff, and the resulting redistribution is missing. This study aims at developing new tools and methods to represent soil redistribution on a global scale, and contribute to the quantification of anthropogenic disturbances to the biogeochemical cycles. We present a new large-scale coarse resolution sediment budget model that is compatible with ESMs. This model can simulate spatial patterns and long-term trends in soil redistribution in floodplains and on hillslopes, resulting from external forces such as climate and land use change. We applied this model on the Rhine catchment using climate and land cover data from the Max Planck Institute Earth System Model (MPI-ESM) for the last millennium (850 - 2005 AD). Validation is done using observed Holocene sediment storage data and observed scaling relationships between sediment storage and catchment area from the Rhine catchment. We found that the model reproduces the spatial distribution of floodplain sediment storage and the scaling behavior for floodplains and hillslopes as found in observations. The exponents of the scaling relationships can be modified by changing the spatial distribution of erosion or by changing the residence time for floodplains. However, the main feature of the scaling behavior, which is that sediment storage in floodplains increases stronger with catchment area than sediment stored on hillslopes, is not changed. Based on this behavior on the main parameters of the model, we argue that the scaling behavior is an emergent feature of the
model and mainly dependent on the underlying topography. Additionally, we identified Furthermore, we find that land use change is the main contributor to the change in sediment storage in the Rhine catchment during the last millennium. Land use change also explains most of the temporal variability in sediment storage for the last millennium in the Rhine catchment in floodplains and on hillslopes.

1 Introduction

Soil erosion by rainfall and the resulting sediment deposition and transport (soil redistribution) soil redistribution in a landscape play an important role in the mineralization and sequestration cycling of soil carbon and the loss of carbon and nutrients from ecosystems [Van Oost et al., 2007]. On the one hand, mineralization of soil carbon at eroding sites and during transport can lead to fluxes of greenhouse gases [Lal, 2003; Van Oost et al., 2007; Lal, 2005]. Vertical fluxes of carbon and nutrients occur due to either mineralization on eroded landscapes and during sediment transport, or due to sequestration in depositional sites [Lal, 2003; Van Oost et al., 2007; Lal, 2005; Quinton et al., 2010]. On the other hand, the transport of significant lateral fluxes of soil carbon and nutrients from a terrestrial ecosystem can result in either sequestration of carbon at deposition sites [Stallard, Van Oost et al., 2007], or significant lateral fluxes of carbon and nutrients can take place when soil redistribution promotes the lateral transport of these elements in and between terrestrial ecosystems [Van Oost et al., 2007; Quinton et al., 2010].

Recent evidence demonstrated that human activities, such as land use change, have accelerated soil erosion and altered the lateral transport rates globally [Van Oost et al., 2012; Wall and Six, 2015]. Accelerated soil erosion has the potential to alter not only the vertical fluxes of carbon and nutrients [Regnier et al., 2013; Stallard, Bauer et al., 2013; Le Quéré et al., 2013]. For example, Regnier et al. [2013] estimated that human activities increased the carbon flux to inland waters by as much as 1.0 Pg carbon year$^{-1}$. However, the effect of soil, but also the lateral export of these elements from terrestrial ecosystems to the coastal oceans [Regnier et al., 2013; Stallard, Bauer et al., 2013; Le Quéré et al., 2013]. Based on the various effects of soil erosion and redistribution on the vertical and lateral fluxes of carbon and nutrients on a global scale is still unknown. This complicates the quantification of anthropogenic disturbances of the biogeochemical cycles carbon and nutrient cycles, these processes can either result in accelerated soil erosion to be a net source [Lal et al., 2004], or in a net uptake or sink of CO$_2$ [Stallard, Van Oost et al., 2007].

Data on large to global scale soil redistribution rates however, data on global soil erosion and redistribution are scarce to non-existing. There exist several modelling approaches to estimate global soil erosion rates [Yang et al., 2003; Ito, 2007; Montgomery, 2007; Doetterl et al., 2012; Naipal et al., 2015]. These modelling approaches mainly address the soil detachment process only, and do not simulate the dynamics of sediment soil redistribution by ignoring processes such as sediment deposition and transport. There is, to our knowledge, no globally applicable spatially explicit model that can
explicitly simulate soil redistribution, which is a result of the sediment dynamics in a landscape, on large spatial scales, for the past, present and future. The lack of such kind of large-scale models on soil redistribution substantially limits the understanding of the relative importance of the various effects of soil erosion and related processes on the global biogeochemical cycles, interaction of soil erosion and redistribution with the global biogeochemical cycles. Therefore, the net global effect of accelerated soil erosion on the vertical and lateral fluxes of soil carbon and nutrients is still unknown.

Consequently, the land components of Earth System Models (ESMs), which are the main tools to investigate the terrestrial carbon cycle and the carbon flux between soil and the atmosphere, ignore the lateral carbon fluxes associated with soil redistribution [Regnier et al., 2013; Van Oost et al., 2012]. Therefore, they miss an important aspect of the coupling between land and the ocean. In addition, omitting soil erosion from soil organic carbon cycling schemes results in uncertainties in the soil organic carbon flux with various implications (Chappell et al., 2013). Including soil redistribution processes in ESMs is thus essential to create the possibility to study the full interactions and feedbacks between the soil and atmosphere with respect to the global biogeochemical cycles, and to better understand the anthropogenic perturbation of these cycles.

The holistic understanding of the interaction and linkages between soil erosion, deposition and transport, can be addressed using the sediment budget approach (Walling and a.L. Collins, 2008). Slaymaker (2003) defined the sediment budget as a mass-balance based approach. Mass-balance where the mass of sediments, water or nutrients is conserved in the considered system so that the net increase in sediment storage is equal to the excess of inflow over outflow of the conserved quantity sediment. However, long-term large-scale sediment budgets are very scarce to non-existing. Sediment budgets that have been constructed previously range from small catchments (Verstraeten and Poesen, 2000; Walling et al., 2001) to large river catchments (Milliman and Meade, 1983; Ludwig and Probst, 1998; Syvitski et al., 2003; Slaymaker, 2003). However, these sediment budgets are usually for present day only as they are mostly based on measurements using methods such as sediment tracing or fingerprinting. Also, most of these studies only focus on the sediment delivery from a catchment. These studies are therefore limited in use for assessing the spatial distribution of sediment sources and storage or in predicting long-term sediment yields. Considering explicitly the spatial distribution of these variables within a catchment is not only essential for a proper land management strategy to combat land degradation, but also for a detailed assessment of how erosion and sediment transport interact with the carbon and nutrient cycles. Furthermore, it is important to distinguish between sediment related processes in floodplain and hillslope systems (de Moor et al., 2013). Human activities usually lead to a stronger increase in sediment deposits on hillslopes compared to floodplains, and an overall decreased export of sediment out of a catchment, despite increased soil erosion (de Moor and Verstraeten, 2008). In this way, sediments stored in floodplains and hillslopes over long timescales can significantly delay
or alter the human induced changes to the carbon and nutrient cycles (Hoffmann et al., 2013). This indicates that there is a need for also essential to consider long-term sediment budgets, as they can provide essential information on the forces behind sediment, carbon and nutrient fluxes in a catchment such as human activities and climate change.

There is thus a need for spatially explicit models that can simulate long-term sediment budgets. There exist different spatial models of suspended sediment flux that also consider the soil redistribution or sediment dynamics in a catchment (Merritt et al., 2003; de Vente and Poesen, 2005; Ward et al., 2009). However, many of them are developed to simulate single events or require input data that is not available for large spatial scales (Wilkinson et al., 2009). There are also partly empirical models which can operate on catchment scale such as the WATEM/SEDEM model, which is used to predict hillslope sediment storage and sediment yields (de Moor and Verstraeten, 2008; Nadeu et al., 2015). Or such as the suspended sediment model from Wilkinson et al. (2009) that also simulates some other processes such as floodplain deposition, gully and riverbank erosion. However, these models are not compatible for a global scale application as they require parameters for which data is not available on a global scale and these type of models also need to be calibrated to measured sediment yields of the studied area (Van Rompaey et al., 2001). Pelletier (2012) proposed a global applicable model for long-term suspended sediment discharge, where he used various environmental controlling parameters to simulate soil detachment and sediment transport. However, in his study he mainly focuses on the sediment discharge and delivery of catchments and his model does not take into account the full dynamics of sediment in a catchment, which would also include the spatial distribution of sediment deposition and storage in the different reservoirs of a catchment. Furthermore, he does not consider land use change and thus his approach is limited to natural catchments only.

The land components of Earth System Models (ESMs) are the main tools to investigate the terrestrial carbon cycle and land use and land cover change (LULCC). They mainly represent the effects of fossil fuels and land use change on the carbon cycle and the resulting carbon flux between soil and the atmosphere (Regnier et al., 2013). However, they ignore the lateral carbon fluxes associated with soil redistribution and, therefore, miss an important aspect of the coupling between land and the ocean (Regnier et al., 2013; Van Oost et al., 2012). Including soil redistribution processes in ESMs would facilitate this coupling and create the possibility to study the full interactions and feedbacks between the soil and the biogeochemical cycles on a global scale. The overall aim of this study is to make a first step in quantifying large-scale soil erosion and redistribution rates and identifying their drivers, in order to contribute to the quantification of the anthropogenic impact on lateral fluxes of carbon and nutrients through the representation of sediment dynamics and associated lateral fluxes in global-of carbon and nutrients in ESMs. Therefore, we present and evaluate a new large-scale sediment budget model that is able to simulate spatial patterns and long-term trends of soil erosion, sediment deposition and sediment storage, based on
climate and land use changes. Compatibility of this new model with ESMs is important for a future extension of the model to include the carbon and nutrient cycling. The specific objective of this study is to present and evaluate the new model for the non-Alpine part of the Rhine catchment using the environment of ESMs. The choice of the Rhine catchment is based on the fact that it is the only large catchment with a long land use history for which we had long-term sediment storage data available. For the validation of the model we used scaling relationships between sediment storage and catchment area found from observations for the non-Alpine part of the Rhine catchment by [Hoffmann et al. 2013]. The scaling relationships are an important criteria for the sediment budget model, as they represent the overall main behavior of sediment in a catchment as function of catchment area. These relationships can thus function as a simple test for the spatial variability of stored sediment that is modelled with a large-scale coarse resolution sediment budget model.

We use the model to quantify the spatial variability of floodplain and hillslope sediment storage for the Rhine catchment, and its dependence on climate change and land use change during the last millennium (850-2005AD). We also investigate the relationship between catchment area and sediment storage on hillslopes or in floodplains to derive a general validation test for our large-scale model. Finally, we discuss the main challenges in modelling large-scale, long-term soil erosion and soil redistribution and future perspectives for application in ESMs.

2 Methods

2.1 Basic model concept

The main purpose of the sediment budget model presented here, is to estimate large-scale long-term floodplain and hillslope sediment storage and lateral fluxes of sediment. The model should therefore be spatially explicit and capable of estimating erosion, deposition and sediment transport processes. Furthermore, we want to differentiate performance of this new model with ESMs is important for a future extension of the model to include the carbon and nutrient cycling. Furthermore, it is essential to distinguish between floodplain and hillslope sediment storage for a better quantification of the impact of human activities in a catchment. Therefore, we use a grid cell based approach where we assume that each grid cell contains a floodplain and hillslope reservoir. Systems due to the distinct differences in sediment dynamics between these systems [Hoffmann et al. 2013]. Human activities usually lead to a stronger increase in sediment deposits on hillslopes compared to floodplains, and an overall decreased export of sediment out of a catchment, despite increased soil erosion [de Moor and Verstraeten 2008].

In this way, sediments stored in floodplains and on hillslopes over long timescales can significantly delay or alter the human induced changes to the carbon and nutrient cycles [Hoffmann et al. 2013].

Before we can define a model that satisfies the above mentioned conditions we have to make some
basic assumptions. Firstly, as it is difficult to disentangle the floodplains and hillslopes in available soil data sets, we assume that each grid cell contains both a hillslope and a floodplain reservoir. When estimating large-scale sediment storage with the aim of predicting fluxes of carbon in the future, the effects of soil redistribution on the biogeochemical cycles, the focus is to get the large-scale spatial patterns right, rather than accurate numbers for the sediment storage. Secondly, and fluxes. Second, we assume that the deposition and sediment deposition and transport behave differently between the floodplain and hillslope reservoirs on the timescale of the last millennium. Thirdly, and deposition and sediment transport behave differently between the floodplain and hillslope reservoirs on the timescale of the last millennium. Third, erosion is considered to mainly take place on hillslopes, where part of the eroded sediment is directly transported from hillslopes and deposited in the floodplains. The underlying model framework (Fig. 1a) that consists out of the erosion, deposition and sediment transport modules, is based on the sediment mass-balance method. The change in sediment storage $(\Delta M)$ within a certain unit of time and space is given by the difference between sediment input and sediment output (Slaymaker 2003). For sediment stored in floodplains $(M_a)$, this leads to:

$$\frac{dM_a}{dt} = D_a - L$$

(1)

Here, $D_a$ is the sediment deposition rate in floodplains, and $L$ is the sediment loss. Equation 1 can also be seen as a representation for the net soil redistribution flux, and can be approximated by the following as function of time:

$$\frac{dM_a}{dt} = D_a(t) - k \times M_a(t)$$

(2)

where $D_a(t)$ is the time-dependent input rate in the model, which is independent from $M_a(t)$. $k \times M_a(t)$ is the loss term in of the floodplain reservoir, and $k$ is the specific rate for floodplains. The specific rate is the inverse of the residence time (1/$\tau$) for floodplain sediment, which is defined as the time (in years) a soil particle stays in the floodplain reservoir of a certain grid cell. Here, we assume that $\tau$ is assumed to be independent of time for timescales in the order of several thousands of years, and is assumed to increase. We also assume that $\tau$ is increasing exponentially with catchment area, where the catchment area is represented by the weighted flow-accumulation ($Flow\text{Acc}$):

$$\tau = e^{\frac{(Flow\text{Acc} - a_\tau)}{b_\tau}}$$

(3)

$a_\tau$ and $b_\tau$ are residence time constants and the adjustment parameters of the model that relate the residence time to FlowAcc. FlowAcc is defined as the number of grid cells located upstream that flow into a certain grid cell. As each grid cell represents a certain catchment area, the value of $\tau$ will be dependent on the location of the grid cell.
in the catchment. The presented relationship between $\tau$ and catchment area in equation 3 is based on the fact that large catchment areas are usually characterized by low slopes, which mainly result in a low connectivity that makes the system capable of storing sediment for a long time periods. The opposite is true for small catchment areas, where the connectivity is usually high and the sediment in these systems will therefore have, resulting in short residence times for sediment (Hoffmann, 2015).

The deposition rate ($D_a$) in the floodplain reservoir can be defined as a certain fraction of the erosion rate ($E$). In this way equation 2 can be rewritten as:

$$\frac{dM_a}{dt} = f \cdot E - \frac{M_a(t)}{\tau}$$  \hspace{1cm} (4)

Where $f$ is the dimensionless floodplain deposition fraction ranging between 0 and 1, and $E$ is the erosion rate in $(t \text{ ha}^{-1} \text{ year}^{-1})$. The erosion rate is computed according to the adjusted Revised Universal Soil Loss Equation (RUSLE) model (Naipal et al., 2015), which computes annual averaged rill and interril erosion rates and is formulated as a product of a rainfall erosivity factor ($R$, MJ mm ha$^{-1}$ h$^{-1}$ yr$^{-1}$), a slope steepness factor ($S$, dimensionless), a soil erodibility factor ($K$, t ha h$^{-1}$ MJ$^{-1}$ mm$^{-1}$), and a land cover factor ($C$, dimensionless):

$$E = S \cdot R \cdot C \cdot K$$  \hspace{1cm} (5)

The underlying RUSLE model stems from the original Universal Soil Loss Equation (USLE) model developed by USDA (USA Department of Agriculture), which is based on a large set of experiments on soil loss due to water erosion from agricultural plots in the United States (Renard et al., 1997). These experiments covered a large variety of agricultural practices, soil types and climatic conditions, making it a potentially suitable tool on a regional to global scale. Although, RUSLE was originally developed for agricultural land, model parameters for other land cover types such as forest and grassland have also been estimated using observational data (Dissmeyer and Foster, 1981; Millward and Mersey, 1999; Lu et al., 2004).

In the adjusted RUSLE model, as presented above, the effects of the slope-length ($L$ factor) and support practice ($P$ factor) are excluded. In the original RUSLE model (Renard et al., 1997), these factors are part of the model, however, on large to global scale there is too little data available on these factors. Including them in the model would only result in additional uncertainties, while we try to keep the model simple, to be able to capture and quantify the main processes and drivers behind large-scale sediment mobilization. We do, however, agree that leaving these two factors out could introduce some biases in erosion rates, especially in agricultural areas.

The floodplain deposition fraction $f$ is calculated by a simple growth function where deposition is a
function of the mean topographical slope $\overline{\text{average percent topographical slope}}$ ($\overline{\theta}$) and the main land cover type in a grid cell:

$$f = a_f \times \left(\frac{b_f \times \theta}{\theta_{\text{max}}}\right)$$  \quad (6)

where $a_f$ and $b_f$ are constants for deposition and dependent adjustment parameters that relate $f$ to the average slope depending on the land cover type, and $\theta$ is the average percent slope on a Shuttle resolution grid. $\theta_{\text{max}}$ is the maximum percent slope. According to equation 6, an increase in the overall average slope of a grid cell leads to a larger transport of eroded soil from the hillslopes to the floodplains. This results in an increase in, leading to an increased deposition rate to the floodplain reservoir of that specific grid cell. Hereby we consider in equation 6 that this increase is exponential. For a natural landscape we assume a good ‘sediment connectivity’ between hillslopes and the floodplain in a grid cell. In natural landscapes the sediment connectivity, we assume the increase of $f$ to be exponential.

The effect of the land cover type on $f$ in our model represents mainly the interaction of the landscape connectivity with sediment transport. The connectivity of a natural landscape, consisting out of mainly forest, is largely based on the vegetation density and morphological structures (Gumiere et al., 2001; Bracken and Croke, 2007). To keep the model simple we do not adapt these parameters to the complexity of natural landscapes, but rather differentiate between the deposition rates in natural and agricultural landscapes, assuming that the sediment connectivity differs fundamentally between these landscapes. In crop- and grassland, however, the landscape connectivity is strongly affected by anthropogenic structures. Several recent studies (Hoffmann et al., 2013; de Moor and Verstraeten, 2008; Gumiere et al., 2011) showed that a large part of the eroded sediment is deposited and stored directly on the hillslopes where agricultural activities take place. Agricultural activities that use anthropogenic structures, show that these anthropogenic structures and activities reduce the sediment transport from hillslopes to the floodplains (Gumiere et al., 2011). In this way, the stored hillslope sediment is disconnected from the fluvial system on timescales of 100 to a few 1000 years. Based on this, we assume that for agricultural land (crop and pasture) and in our model that for crop- and grassland the sediment connectivity is disturbed. A bad disturbed sediment connectivity will result in a larger fraction of eroded soil that remains on the hillslopes compared to the fraction that flows along the hillslopes and is deposited in the floodplains. For natural landscapes we assume a better sediment connectivity, meaning that an equal or larger fraction of the eroded soil will be deposited in the floodplains compared to the fraction that remains on the hillslopes. Here we ignore morphological conditions that can cause deconnectivity in the landscape.

After calculating erosion and deposition, the sediment is transported between the grid cells based on a multiple flow sediment routing scheme such as presented by Quinn et al. (1991) (Fig. 1b).
the multiple flow routing scheme the weight \((W, \text{ dimensionless})\), which specifies the part of the flow that comes in from a neighboring grid cell, is calculated as:

\[
W_{(i+k,j+l)} = \frac{\theta_{(i+k,j+l)} \cdot c_{(i+k,j+l)}}{\sum_{k,l} \theta_{(i+k,j+l)} \cdot c_{(i+k,j+l)}} \tag{7}
\]

where \(c\) is the contour length and is respectively 0.5 in the cardinal direction and 0.354 in the diagonal direction. \((i,j)\) is the grid cell in consideration where \(i\) counts grid cells in the latitude direction and \(j\) in the longitude direction. \(i+k\) and \(j+l\) specify the neighboring grid cells where \(k\) and \(l\) can be either -1, 0 or 1. \(\theta\) is calculated here as:

\[
\theta_{(i+k,j+l)} = \frac{h_{(i,j)} - h_{(i+k,j+l)}}{d} \tag{8}
\]

where, \(h\) is the elevation in meters derived from a digital elevation model, \(d\) is the grid size in meters.

The floodplain sediment storage rate \(\text{t ha}^{-1} \text{ year}^{-1}\) of a grid cell \((i,j)\) is then a function of the deposition rate in that grid cell, the loss from that grid cell and the incoming sediment from the neighboring grid cells, and is calculated at each time step \(t\) as:

\[
M_{a(i,j)}_{t+1} = M_{a(i,j)}_{t} + [f_{t} \cdot E_{t} - \frac{M_{a(i,j)}}{\tau_{(i,j)}}] + \sum_{k,l} \frac{M_{a(i+k,j+l)}}{\tau_{(i+k,j+l)}} \cdot W_{(i+k,j+l)} \tag{9}
\]

For hillslopes the change in sediment storage is assumed to be equal to the input rate \((\text{Eq.10})\), because we assume that the stored hillslope sediment has an infinite residence time on the timescale of the last millennium \((\text{Eq.10})\) in accordance with the study of [Hoffmann (2015)]. This means that the hillslope sediment storage will increase linearly with time \((\text{Eq.11})\). The hillslope sediment deposition rate \((D_{e})\) is here defined as the remaining part of the eroded soil that has not been transferred to the floodplain directly \((1-f)\). The equations for the hillslope sediment storage rate \((M_{e}, \text{ t ha}^{-1} \text{ year}^{-1})\) are represented by:

\[
\frac{dM_{e}}{dt} = D_{e} = (1-f) \cdot E \tag{10}
\]

And as a function of time:

\[
M_{e(i,j)}_{t+1} = M_{e(i,j)}_{t} + (1-f) \cdot E_{t} \tag{11}
\]

The modelling approach as presented by the equations above focuses on the net soil redistribution by separately modelling the main processes of soil redistribution, which are erosion, deposition and transport. In the following paragraphs we will show how this dynamical modelling approach performs when applied on the Rhine catchment.
2.2 Model implementation and parameter estimation

The resolution of the sediment budget model is 5 arcmin. The main reason for choosing this particular model resolution, because we assume that this is the optimal resolution, is based on the assumption that this resolution is optimal when considering that each grid cell contains a floodplain and hillslope fraction. Here, a higher resolution could lead to cases where this assumption is not met. Also, the 5 arcmin resolution fits well with the resolution of the adjusted RUSLE model.

The sediment budget model uses climate and land cover data from simulations of MPI-ESM that have been performed under the Coupled Model Intercomparison Project Phase 5 (CMIP5) framework (Hurrell and Visbeck [2011] Taylor et al. [2009]). As this data was given at a resolution of approximately 1.875 degrees, we had to downscale the data to the resolution of the sediment budget model. For the period 1850-2005 AD, three ensemble members from MPI-ESM (r1i1p1, r2i1p1, r3i1p1) were available, while for the period 850-1850 AD, only one ensemble member (r1i1p1) was available. This data existed on a 6 hourly, monthly or yearly time step for the last millennium.

Calculation of soil erosion according to the adjusted RUSLE model is mostly based on the methods presented in the study of Naipal et al. [2015]. However, the calculation of the R and C factors had to be adapted due to the very coarse resolution of the data from MPI-ESM or the lack of data on certain parameters of the model. A detailed description of erosion estimation with the adjusted RUSLE model in combination with data from the MPI-ESM model is presented in the supply material.

Additionally, due to the overestimation of erosion rates by the adjusted RUSLE model in the Alps, we defined a mean soil erosion rate of 20 t ha⁻¹ year⁻¹ for this region based on high resolution erosion data from Bosco et al. [2008].

We chose the floodplain deposition fraction \( f \) to range between 0.5 and 0.8 for natural landscapes that consist out of mainly forest, and between 0.2 and 0.5 for agricultural lands. According to equation 6, \( f \) increases exponentially with slope crop- and grassland. These numbers are based on findings from the study of de Moor and Verstraeten [2008], where they show an approximately equal deposition rate in floodplains as on hillslopes before agricultural activities started in the Geul river catchment in The Netherlands. However, for present-day they show that much more sediment is trapped on hillslopes than is transferred to the floodplains. Based on this, the chosen ranges for \( f \) and equation 6, we calculated \( a_f \) and \( b_f \) to be respectively for forest to be 0.5 and 0.47 for natural landscapes and respectively, and for crop- and grassland to be 0.2 and 0.917 for agricultural land, respectively.

This means that for low slopes (\( \leq 0.2 \% \)) in a natural landscape forest an equal amount of sediment is deposited in the floodplain as on the hillslope, floodplains as on hillslopes, while for agricultural land crop- and grassland only 20% of the eroded soil from the hillslope floodplains will reach the floodplain

The floodplain residence time is made to range between the median and maximum residence time of floodplain sediment in the Rhine catchment of respectively 260 and 1500 years.
This is in accordance with the residence times derived from observed sediment storage in the Rhine catchment. Furthermore, Wittmann and von Blanckenburg (2009) found a residence time of 600 years for floodplain sediments at Rees in the Rhine catchment, which falls in the range of the floodplain residence times of our study. According to equation 3, \( \tau \) increases exponentially with flow-accumulation. As the maximum flow-accumulation is different for different catchments, we used the median and maximum residence times and the maximum flow-accumulation of the Rhine catchment to determine the \( a_\tau \) and \( b_\tau \) in equation 3. The exact values for \( a_\tau \) and \( b_\tau \) are respectively -922442.54 and 165886.77, respectively.

2.3 Criteria for model evaluation

A large-scale spatial model like the one we presented is difficult to validate due to the lack of large-scale and long-term observational data. Hoffmann et al. (2013) compiled published data on sediment storage for regions in Central Europe, mainly for the Rhine catchment, where human induced soil erosion took place. Combined with a long land use history, where agricultural activities go back till started about 7500 years ago (Houben et al., 2006; Hoffmann et al., 2007; Dix et al., 2016; Kalis and Merkt, 2003), the Rhine catchment serves as a good case study to investigate the impact of human activities on erosion and sediment yields through history. The Rhine catchment (Fig. 2) has a size of \( \sim 185000 \text{km}^2 \) with a main river channel length of \( \sim 1320 \text{ km} \) and drains large parts of the area between the European Alps and the north sea. It has a complex topography where the elevation ranges between -180 and 1967 m with a mean topographical percent slope of 0.07, where percent slopes can go up to 1.2. It consists out of two large sedimentary catchments (ie, upper Rhine Graben and the lower Rhine Embayment-Southern North Sea Basin) that serve as large floodplain sinks for sediment, and some upland areas, such as the Black Forest and the European Alps that serve as major sediment production areas.

From the observed Holocene sediment storage Hoffmann et al. (2013) derived scaling relationships between sediment storage \( S \) \( (10^9 \text{ kg} = 1 \text{ Mt}) \) and catchment area \( A \) \( (\text{km}^2) \) for floodplains and hillslopes. They found that for floodplains the sediment storage increases exponentially in a non-linear way with catchment area, while hillslope sediment storage shows a different behavior and increases almost linear with catchment area. For hillslopes this increase is linear. With these scaling relationships, for the first time, a direct comparison is made between the behavior of soil redistribution on hillslopes and in floodplains at large spatial scales. This is an essential difference between hillslopes and floodplains that large-scale sediment budget models like ours need to capture in order to reliably simulate the spatial distribution of sediment on such a scale. The scaling relation-
ships, given by equation 12 for hillslopes and equation 13 for floodplains, will be used as the main validation for our a simple validation test for our coarse resolution sediment budget model.

\[ S = (364 \pm 168) \times 10^6 \times \left( \frac{A}{A_{ref}} \right)^{1.06 \pm 0.07} \] (12)

\[ S = (184 \pm 24) \times 10^6 \times \left( \frac{A}{A_{ref}} \right)^{1.23 \pm 0.06} \] (13)

Here, \( A_{ref} \) is an arbitrary chosen reference area, in this case \( 10^3 \) km\(^2\). The observation data contains 41 hillslope and 36 floodplain sediment storage values, derived from a large number of auger and bore holes that are used to measure sediment thickness related to human induced soil erosion. With the estimated scaling exponents (Eq. 12 and Eq. 13) Hoffmann et al. (2013) showed that even for large catchments (in the order of \( 10^5 \) km\(^2\)) hillslopes store an equal amount of sediment as floodplains. They pointed out that this is a substantial sink that needs to be considered in sediment budgets of large catchments.

Furthermore, Hoffmann et al. (2007) established a Holocene sediment budget for sediments in the floodplains and the delta of the non-Alpine part of the Rhine catchment. They derived sediment thickness of Holocene deposits from borehole data that consists out of 563 drillings and available geological maps. This was then multiplied with floodplain areas to calculate floodplain volumes. Sediments on hillslopes were not addressed in this study. A total floodplain sediment mass of 53.5 \( \pm \) 12.4 \( \times \) 10\(^9\) tons was found for the whole Rhine catchment, of which 50\% is stored in the Rhine Graben and the delta. The spatial variability of this observed sediment storage in floodplains will be a second validation test for our model.

Finally, Hoffmann et al. (2007) also found an average erosion rate of \( 0.55 \pm 0.16 \) t ha\(^{-1}\) year\(^{-1}\) for the last 10000 years, with extreme minimum and maximum values of 0.3 and 2.9 t ha\(^{-1}\) year\(^{-1}\). However, Hoffmann et al. (2013) included also hillslope sediment storage and calculated a total sediment storage of 126 \( \pm \) 41 Gt for the Rhine catchment, which requires a minimum Holocene erosion rate of approximately \( 1.2 \pm 0.32 \) t ha\(^{-1}\) year\(^{-1}\). This shows that hillslopes are not only the main sources of eroded sediment but can be major millennial-scale sinks for eroded sediment that comes from agriculture. We will compare the erosion rates of the Rhine catchment use the average erosion erosion rates from the above mentioned studies as a comparison to the rates derived from our sediment budget model also with the above presented values from the studies of Hoffmann et al. (2007) and Hoffmann et al. (2013).

### 2.4 Simulation setup

In order to simulate sediment storage for a certain catchment, an initial state of that catchment has to be assumed. Here we assume the initial state to be the equilibrium state of a catchment, defined
as the state of a catchment where the sediment input is equal to the sediment output, and thus the sediment yield at the outlet of the river should be constant in time. External forces working on a catchment such as, land use activities or deglaciation, can bring the catchment out of equilibrium into a transient state. In the case of the Rhine catchment the period directly after the Last Glaciation Maximum (LGM) could be of major importance due to strong erosion that was triggered by the retreating ice sheets. From today’s observations on sediment budget yields or erosion rates we cannot determine when the Rhine catchment was in an equilibrium state. Additionally, there are no observations of sediment storage before the start of agricultural activities in the Rhine catchment, which date back to 7500 years ago. This poses a problem in simulating and interpreting the present-day absolute values of sediment storage and yields with our sediment budget model.

In order to still being able to interpret the simulated sediment storage results for the Rhine catchment, we will not focus on the absolute values of sediment storage. We will only focus on the change in sediment storage due to land use and climate change since 850 AD. Considering mainly the changes induced by external forcing, it is not necessary to know if the system was in an equilibrium or transient state at 850 AD. Based on this reasoning, we take use the environmental conditions of 850 AD—the period between 850 and 950 AD to determine the equilibrium state of the model.

In the rest of this study, we will refer to 850 AD—the period between 850 and 950 AD as the ‘default equilibrium state’ that we define based on the mean climate and land cover conditions at 850 AD. The period 850 to 950 AD is used here as the equilibrium state due to reasons related to data availability, and because human impact in this time period is still small compared to present day.

Hence, our simulation setup structure is generally defined by an equilibrium simulation based on the conditions of 850 AD, followed by a transient simulation for the last millennium.

We used climate and land cover data from different simulations of MPI-ESM that were available from the CMIP5 experiment to force the sediment budget model. We performed three equilibrium simulations, one based on the mean climate and land cover conditions of the period 850-950 AD, and the two others based on the mean climate and land cover conditions of the mid-Holocene period (6000 years ago) from the mid-Holocene experiment of the MPI-ESM (Table 1). The reason for performing an equilibrium simulation for the mid-Holocene period is to investigate how different initial conditions for climate and land cover would influence the overall sediment storage change during the last millennium.

In the equilibrium simulations the erosion and deposition rates are kept constant and the model is run with a yearly time step till the total floodplain sediment storage of a catchment does not change more than 1 ton per year. The floodplain and hillslope sediment storage at equilibrium were then used as
a starting point for the transient simulation that covers the period 850 - 2005 AD. In the transient simulation erosion and deposition rates are averaged over time steps of 100 and 50 years, based on the time resolution of the rainfall erosivity factor \( R \) that is part of the erosion module. We performed five ‘default’ transient simulations, two based on the mid-Holocene equilibrium states, and three others based on the equilibrium state of the period 850 - 950 AD. The different ensemble simulations were used to investigate the uncertainty in the resulting sediment storage due to the input data of MPI-ESM. Additionally, we also performed a climate change and land use change simulation based on the equilibrium state of the period 850 - 950 AD (Table 1). In the climate change simulation the land cover was fixed to the mean conditions of the period 850-950 AD during the whole period of the period 850-950 AD during the last millennium, while the climate was variable. In the land use change simulation the climate was fixed to the mean conditions of the period 850-950 AD during the last millennium, while the land cover was variable (Table 1).

3 Application of the sediment budget model

3.1 Scaling test

In order to validate the sediment budget model we tested if the model can reproduce the scaling relationships found by Hoffmann et al. (2013) for the non-Alpine part of the Rhine catchment (Eq.12 and 13). For this we chose the grid cells in the Rhine catchment that correspond to the observation points from Hoffmann et al. (2013). Observation points that fell outside the Rhine catchment, were not considered. When considering only the selected grid cells and applying the same scaling approach as in the study of Hoffmann et al. (2013), we found an average scaling exponent for floodplains and hillslopes, respectively of 1.2 ± 0.04 and 1.05 ± 0.07 for floodplains and hillslopes, respectively (Table 2). These values fall in the range of floodplain and hillslope scaling exponents of 1.23 ± 0.06 and 1.08 ± 0.07, respectively, found by Hoffmann et al. (2013). The uncertainty in the scaling exponents is mainly due to the regression, while the uncertainty due to different ensemble simulations is very small (Table 2). Our model also indicates that our model reproduces the characteristic differences in scaling between floodplains and hillslopes as found by Hoffmann et al. (2013) (Fig. 3a and b). One should note that the grid resolution of the model limits the prediction of sediment storage to grid points with a catchment area $\geq 10^2 \text{ km}^2$.

When considering all the grid cells of the Rhine catchment we derived a scaling exponent for floodplain storage of 1.33 ± 0.02 (Table 3), which is somewhat higher than the value found when only the selected grid cells are used. This may be due to the inclusion of grid cells that are located in the Alpine region of the Rhine catchment. Including the Alpine region leads then to a stronger gradient in sediment storage and catchment area between the Alps and the Rhine delta. In the Alpine region the model predicts much less sediment storage due to
the low residence time and high sediment connectivity, while for the Rhine delta the sediment storage is large due to high flow-accumulation and high residence times. For hillslope storage the scaling exponent is also slightly higher when including all grid cells in the scaling approach (Table 3). This can also be explained by including the Alpine region, where the model predicts more sediment storage on hillslopes compared to the rest of the Rhine catchment due to the as a result of high erosion rates in this region. Furthermore, when including all grid cells in the scaling approach there is more the spread in the data increases, which is clear from the lower r-value of the regression. The small difference between the scaling exponents when considering all grid cells and the scaling exponents when considering only selected grid cells indicates that the selected observation points from [Hoffmann et al. (2013)] are robust and representative for the catchment. The relatively small difference can be partly attributed to biases in simulated erosion and deposition rates and the floodplain residence times. Finally, we found that keeping either the climate or land cover constant throughout the last millennium has very little impact on the scaling exponent for floodplain storage. Here, the climate change simulation resulted in a slightly higher and the land use change simulation in a slightly lower scaling exponent. The different forcings have a stronger impact on the scaling for hillslope storage, as hillslope sediment storage is only dependent on erosion and deposition rates. For In the climate change simulation the scaling exponent for hillslope storage increases by 3.8%, while for in the land use change simulation a small decrease of 0.1% was found. This decrease could result from the fact that most land use change took place in the lower parts of the Rhine catchment resulting in an increased sediment storage there. In contrast, the land use conditions in the Alpine region did not change that rapidly, resulting in a decreased difference in sediment storage on hillslopes between the upper and lower areas of the catchment.

The above results indicate that the scaling relationships are a general feature for the entire Rhine catchment and are independent of the selected observation points. As the Rhine catchment is a large catchment with a complex topography, this result indicates that the scaling relationships might be applicable for other large river catchments.

### 3.2 Origin of scaling between sediment storage and catchment area

We also performed a sensitivity study to test the robustness of the scaling relationships derived with the model. For this we investigated the dependence of the scaling on the three main variables of the model, namely, the residence time, erosion and deposition. First, we investigated the dependence of the scaling exponent of floodplain storage on the residence time. To do this, we chose different median residence times of floodplain sediment in the Rhine catchment, while keeping the maximum residence time fixed. Changing the median residence time by a factor of 10, from 50 to 500 years, results in a decrease of 21.8% in the scaling exponent for floodplain storage.
storage for floodplains in the transient simulation (Table 4). When the median floodplain residence time is increased, the range in the residence time decreases. This leads to a decreased difference in sediment loss between grid cells with small and large catchment area in terms of the sediment loss, and consequently, which then leads to a decrease in the scaling exponent. We found that when the residence time is increased by 5.2% (from 50 to 260 years) the scaling exponent decreases by 18.2%, while an increase in the residence time of 1.9% (from 260 to 500 years) results only in a decrease of the scaling exponent of 4.4%. This indicates that the scaling exponent of floodplain storage does not change linearly with the residence time, and points out that the model shows a non-linear behavior. The equilibrium simulation shows the same way. Applying the same approach for the equilibrium simulation results in a similar behavior for the scaling exponent when the residence time is changed. However, here the 10 fold change in the residence time leads to a slightly larger change in the scaling exponent.

Next, we investigated the dependence of the scaling exponents of floodplains and hillslopes for floodplain and hillslope storage on erosion. We changed the spatial variability of erosion in the Rhine catchment by changing the spatial variability of the $R$ factor. We increased the $R$ values in the Alpine region and decreased the $R$ values in the rest of the catchment. This resulted in a larger difference between the sediment storage in small catchment areas and sediment storage in large catchment areas. Although the resulting scaling exponent for floodplains was floodplain storage is still much higher than the scaling exponent for hillslope storage, both scaling exponents increased significantly. For the deposition we found a minor to neglecting effect on the scaling parameters. Overall we found that changing erosion and residence time does not change the basic property of the scaling, which is that floodplain storage grows in a non-linear way with catchment area while hillslope storage shows a linear scaling with catchment area. As the residence time is determined by flow-accumulation and flow-accumulation determines the spatial variability of floodplain sediment storage, we expect that the scaling parameters of floodplain sediment storage are also mainly determined by flow-accumulation. Erosion is mainly determined by the slope, and slope determines the spatial variability of hillslope sediment storage. Therefore, we expect that the slope determines the scaling parameters of hillslope sediment storage. Based on this we argue that the scaling for both floodplain and hillslope storage is an emergent property of the model and that the scaling parameters are controlled by the underlying topography.

3.3 Last millennium sediment storage

We estimated an average soil erosion rate of $2.8 \pm 0.002 \text{ t ha}^{-1} \text{ year}^{-1}$ for the last millennium for the entire Rhine catchment. We find that this value is twice as high as the $1.2 \pm 0.32 \text{ t ha}^{-1} \text{ year}^{-1}$, which was estimated as the minimum average soil erosion rate for the Holocene by [Hoffmann et al.].
The average soil erosion rate for the last millennium resulted in a mean floodplain and hillslope sediment storage change for the last millennium of 11.95 ± 0.01 and 29.68 ± 0.03 Gt, respectively for the last millennium (Table 5). Altogether, floodplain and hillslope storage result in 41.63 ± 0.02 Gt of sediment, which can be considered as the contribution of climate and land use change to sediment storage in the last millennium. It is, however, hard to say what the range in the change of sediment storage should be for this period, as there are no related studies for this specific time period. Hoffmann et al. (2007) found a total sediment storage we find is lower than the total Holocene sediment storage of 126 ± 41 Gt for the Holocene in the found by Hoffmann et al. (2007) for the Rhine catchment. Our values are lower than this range found by Hoffmann et al. (2007), due to the fact that we only consider the impact of last millennium on the sediment storage. This is logical as we consider only the last millennium and not the past 7500 years as in the study of Hoffmann et al. (2007). Our results show that the sediment storage of the last millennium form 25 to 50% of the total sediment storage of the last 7500 years. This indicates that the average sediment storage rate during the last millennium is higher than the average rate during the last 7500 years. This also supports the findings from previous studies (Bork, 1989; Notebaert et al., 2011), which show that land use change has a significant and long-term impact on erosion and sediment mobilization.

Furthermore, Hoffmann et al. (2013) found a floodplain to hillslope ratio of about 0.88, indicating that during the Holocene more sediment was stored on hillslopes than in floodplains. We find with our model a floodplain to hillslope ratio of about 0.46, confirming that more sediment is stored on hillslopes. However, the floodplain to hillslope ratio from our model indicates a much larger difference in sediment storage between floodplains and hillslopes than in the study of Hoffmann et al. (2013). This can be attributed to the simple lack of an explicit representation of the sediment deposition process in our size and location of floodplains in the model, and may indicate that a more complex representation of deposition is needed where for example the effect of the roughness of the landscape is explicitly included the simple representation of the sediment deposition processes for floodplains and hillslopes.

We also analyzed the spatial variability of the modelled sediment storage, and found simulated sediment storage in floodplains, and find that the model reproduces the spatial variability well when compared to the observed values from Hoffmann et al. (2007) for the Holocene (Fig. 4). Here we find a correlation coefficient of 0.76 ± 0.77, where sediment storage in floodplains increased with the catchment area. Furthermore, we find that most floodplain sediment is stored in the Mosel sub-catchment, in contrast to the observations that show that most of the sediment is stored the largest storage in the Upper-Rhine sub-catchment (Table 6). This can be related to the fact that different dynamical processes, which are not captured with our model, play a role in the Upper-Rhine catchment, which are triggered by the Alps. Melting ice sheets for example can produce a lot of
erosion that is not captured by our model and in this way the total stored sediment in the catchment could be underestimated. Furthermore, the Mosel sub-catchment has a highly complex topography, which may indicate that our sediment budget model is too coarse for an accurate representation of floodplain storage for this catchment.

For hillslope sediment storage we found a similar spatial trend as for the floodplain sediment storage, with some more variation between the minimum and maximum values (Table 6). Also here, the Mosel sub-catchment stores the most sediment. Furthermore, when comparing floodplain to hillslope sediment storage we find that the floodplain to hillslope ratio varies significantly between the various sub-catchments. The highest ratio of 0.48 is found for the Lower Rhine sub-catchment, while the lowest ratio of 0.14 is found for the Emscher sub-catchment. The ratios seem not to be correlated with slope or catchment area and can be assumed as independent features of the model.

The sediment budget model presented here, has been developed to simulate long-term historical trends and to determine the main drivers behind these trends. Figure 5 shows the land use change and the 10 year-mean precipitation timeseries averaged over the Rhine catchment for the last millennium. There are two interesting periods, respectively, 1350-1400AD and 1750-1950AD, that show increased precipitation amounts correlating with a sudden increase in land use change (increase in crop and pasture). Both periods lead to maxima in the erosion timeseries of 2.8 t ha\(^{-1}\) year\(^{-1}\) and 4.3 t ha\(^{-1}\) year\(^{-1}\), respectively (Fig. 6a and 6b).

This corresponds to increased erosion rates during the 14th and 18th century found by (Bork, 1989; Lang et al., 2003) for Germany.

We find the strongest increase in the sediment storage rate for floodplains during the period 1750-1850AD, while 1750-1850 AD, and for hillslopes during the period 1850-1950AD 1850-1950 AD. For hillslopes this maximum sediment storage rate corresponds to a maximum increase in the deposition rate, which is a result of a maximum increase in land use change and a high erosion rate. Land use change leads to a sediment disconnectivity in the landscape, which prevents the sediment stored on hillslopes of reaching the fluvial system on the timescale of the last millennium. In contrast to hillslopes, the maximum sediment storage rate for floodplains is a result of the interplay between deposition and sediment loss from the catchment. In the period 1750-1850AD-1750-1850 AD land use change started to increase in the Alpine region, which did not experience such a strong change in land-use before 1750 AD compared to the downstream regions of the catchment before this time period. During this period, the deposition to floodplains increased significantly due to the increased erosion rates as a result of land use change. Also, as land use change started to impact the Alpine region, where areas with steep slopes and short residence times lead to a strong sediment flux downstream. However, due to the long residence time of the areas located downstream, the sediment loss from the total catchment did not increase as much, leading to an increased sediment storage in the floodplains. This is in accordance
with the findings of Asselman et al. (2003), who found that due to an inefficient sediment delivery, an increase in soil erosion in the Alps will have a little effect on sediment load downstream the Rhine catchment.

Furthermore, if we disentangle the effects of land use and climate on the sediment storage for floodplains and in floodplains and on hillslopes, we can see find that land use change explains most of the change in sediment storage. For floodplains climate change also has a non-negligible impact on the temporal variability of sediment storage. For example, in the periods 1350-1400 AD and 1750-1950 AD, the sediment storage rate is increased due to increased precipitation that leads lead to a strong sediment flux downstream from upstream areas. If the land use change conditions of the period 850 and 950 AD were kept constant, the total change in sediment storage in floodplains and on hillslopes during the last millennium would be is 2.9 and 15.4 Gt, respectively. This is four and two times, respectively, less than the change in floodplain and hillslope sediment storage when land use change is variable (Fig. 7a and 7b). When the land cover is kept constant Here, the overall sediment storage still increases for the climate change scenario due to the overall increased trend in precipitation during the last millennium. If only the climate change conditions are kept constant, the resulting change in sediment storage in floodplains and hillslopes would be on hillslopes is 10 and 27.4 Gt, respectively.

3.4 Uncertainty assessment and limitations of the modelling approach

As shown in the previous sections, the average modelled erosion rate for the last millennium of the Rhine catchment is found to be overestimated when compared to the average erosion rate for the Holocene from the study of Hoffmann et al. (2013). As we consider in this study only the last millennium, where human impacts through land use change are strongest pronounced, it is logical that our estimated average soil erosion rate is higher. For present day, we found estimate an average soil erosion rate of 3.3 t ha$^{-1}$ year$^{-1}$ for the non-Alpine part of the Rhine catchment, which is also overestimated when compared to other studies. Cerdan et al. (2010) found for the non-Alpine part of the Rhine catchment a value of 1.5 t ha$^{-1}$ year$^{-1}$, while Auerswald et al. (2009) found for Germany a value of 2.7 t ha$^{-1}$ year$^{-1}$.

Comparing the spatial variability of our simulated erosion rates for present day with the high resolution estimates from Cerdan et al. (2010), we find that erosion is our rates are overestimated for the whole entire Rhine catchment. We expect that the overestimation in the modelled erosion rates is mainly due to uncertainties related to the coarse input datasets on climate and land cover, and biases in the adjusted RUSLE model. We found For example, we find that precipitation is generally overestimated by MPI-ESM for the Rhine catchment. Even after introducing a correction factor, which partly adjusted the $R$ value estimation to values from present-day observational datasets, biases related to the $R$ factor remain. It is, therefore, also important to test the sensitivity of the sediment budget model with input data on precipitation and land cover from other ESMs.
Additionally, coarse resolution land cover fractions and leaf area index (LAI) from MPI-ESM also affect the total erosion rates. Using coarse resolution data to calculate the C factor of the adjusted RUSLE model results in discrepancies between the C and S factors. For example, consider a large coarse resolution grid cell with a complex topography where cropland is allocated in flat areas and forest in the steeper areas. Even though the C factor is calculated correctly as combination of cropland and forest fractions, it is applied to the whole grid cell. This leads to an overestimation of erosion rates for flat areas, as erosion is in the first order controlled by the slope through the S factor. We attempted to correct for this by introducing slope classes for each coarse grid cell with resolution of MPI-ESM (1.875 degrees). The cropland was then allocated to the flatter areas, while in the steeper areas more of the other land cover types were allocated to the steeper areas. However, this only had a minor effect on the overall erosion rates, indicating that this is not the major source for the overestimated erosion rates.

Additionally, the absence of the seasonality in the C factor results in discrepancies between the C and R factors. Neglecting the support practice (P) and slope-length (L) factors in the adjusted RUSLE model also affect the erosion rates. As the Rhine catchment has a long land-use history, land management strategies were implemented historically to decrease soil erosion rates. We partly captured the effects of land management in the C factor; however, agricultural regions, where they may play an important role, results in an overestimation of the increases of soil erosion, especially during the 1950's. However, we expect that introducing the P and this does not affect the overall trends. This assumption is also supported by Doetterl et al. (2012), who shows that the L factors in the model will reduce the soil erosion rates in cropland and P factors explain only up to 22% of the variability in water erosion rates on cropland in the USA.

Also, biases in the adjusted RUSLE model, such as the unadjusted C and K factors and the low performance of the model in mountainous areas, have an equally important effect on the total erosion rates.

Another large uncertainty in our sediment budget model, besides the biases in erosion rates, is the choice of the equilibrium state. We found a decreasing trend in the floodplain sediment storage in the transient simulation when using the equilibrium state based on the mean conditions of 6000 BP. This can be attributed to the different spatial distribution of erosion and the average high erosion rate for the mid-Holocene of 7.8 t ha$^{-1}$ year$^{-1}$. When switching from the equilibrium state to the transient state, the erosion rates drop and the its spatial distribution changes significantly. This leads to a decreased sediment flux from upstream areas and overall decreased sediment production rates that result in a drop decrease in sediment storage in the floodplains. For the hillslopes we found that the equilibrium state has minimal to no influence on the total sediment storage for the last millennium.

The initial conditions determine the amount and spatial distribution of erosion in the catchment dur-
ing the time that the model runs to equilibrium. Therefore, the equilibrium state that is then reached, largely determines the spatial distribution, trend, and amount of the sediment storage during the transient period.

**Finally, Furthermore**, the different ensemble simulations for the period 1850-2005AD do not differ strongly in precipitation and land cover/land use change, and therefore, do not contribute much to the uncertainty in the overall erosion rates and sediment storage. This period is also too short to find significant effects on the sediment storage from climate change using different ensemble simulations.

There are also some limitations to the model. The sediment yield cannot be reproduced accurately simulated for catchments where the initial state of the catchment is uncertain. However, with accurate data input on climate and land cover, the model can be made applicable for tropical catchments on the timescale of the last millennium, after adjusting the model parameters for these catchments. This is because we expect the effect of the last glaciation to be minimal on tropical catchments. In combination with low human activities in 850AD, this time period seems reasonable. This can be tested in the future by applying a future application of the model on other large catchments.

Furthermore, a more concrete parameterization for the residence time and deposition of floodplain sediment, and a possible new parameterization for the residence time of hillslope sediment could lead to an improvement of the model. Finally, more validation with long-term sediment storage from other catchments, especially tropical catchments, would be an important contribution in making the model better applicable on the global scale.

## 4 Conclusions

In this study we introduced a new model to simulate long-term, large-scale soil erosion and redistribution based on the sediment mass-balance approach. The main objective here was to develop a sediment budget model that is compatible with Earth System Models (ESMs), to simulate large-scale spatial patterns of soil erosion and redistribution for floodplains and hillslopes following climate change and land use change. We applied this sediment budget model on the Rhine catchment as a first attempt to investigate its behavior and validate the model with observed data on sediment storage and erosion rates.

We show that the model reproduces the scaling relationships between catchment area and sediment storage found in observed data from Hoffmann et al. (2013). These scaling relationships show that the floodplain storage increases significantly non-linearly with catchment area while the hillslope storage scales linearly with catchment area in contrast to hillslope storage. The scaling exponents can be modified by changing the spatial distribution of erosion or by changing the residence time for floodplains. However, the main feature of the scaling relationships...
which is that floodplain storage increases stronger with catchment area as hillslopes, is behavior not changed. Based on this we conclude that the scaling relationships are behavior is an emergent feature of the model and mainly dependent on the underlying topography. We found a mean soil erosion rate of $2.8 \pm 0.002 \, \text{t ha}^{-1} \text{year}^{-1}$ for the last millennium (850 - 2005AD). This is an overestimation when compared to the minimum Holocene erosion rate of $1.2 \pm 0.32 \, \text{t ha}^{-1} \text{year}^{-1}$ from Hoffmann et al. (2013). Also for present day the erosion rates from our model are overestimated. We argue that this is mainly due to the coarse resolution input data on climate and land cover, and the fact that the land cover factor of the erosion model is not adjusted for a coarse resolution application. Additionally, the absence of the seasonality in the $C$ factor plays a role, and other biases of the adjusted RUSLE model, such as the neglect of the land management and slope-length factors. However, we aim with the sediment budget model to distinguish between the floodplain and hillslope sediment storage, simulate their long-term behavior, and more specifically estimate the spatial distributions of sediment rather than the total amounts. For this objective a coarse estimation of erosion is sufficient.

The simulated erosion rates resulted in a change in floodplain and hillslope sediment storage during the last millennium of $11.95 \pm 0.03$ and $29.68 \pm 0.01$ Gt, respectively. Based on this and the observed data we estimate that the climate and land use changes during the last millennium contribute between 25 - 50% to the total sediment storage for the past 7500 years.

Disentangling the contribution from climate change and land use change to the change in sediment storage during the last millennium for the Rhine catchment, we find that the climate change simulation results in a total change in sediment storage in floodplains and hillslopes of 2.9 and 15.4 Gt, respectively. While the land use change simulation results in a total change in sediment storage in floodplains and hillslopes of 10 and 27.4 Gt, respectively. This shows that land use change contributes the most to the total change in sediment storage during the last millennium for the Rhine catchment.

Furthermore, the model reproduces the overall spatial distribution of floodplain sediment storage in floodplains during the last millennium. However, there are some outliers, such as the Mosel catchment sub-catchment for which the model simulates a too high sediment storage. This could be a result of biases in the erosion rates and the fact that our model is limited to the last millennium. We also found that the hillslope storages of the sub-catchments show a similar spatial pattern as the floodplain storage.

When analyzing the timeseries of erosion rates and storage during the last millennium we found that the model reproduces the timing of the maxima in erosion rates as found in the study of Bork (1989). We also find that land use change is the main driver behind the trends in erosion and sediment storage for both floodplains and hillslopes. For floodplains, however, climate change has a non-negligible impact on the temporal variability of sediment storage. When keeping the land cover constant to the conditions in the period 850 to 950AD, we find that the sediment storage still in-
increases due to an increased trend in precipitation during the last millennium.

We conclude that our sediment budget model is a promising tool for estimating large-scale long-term sediment redistribution. An advantage of this model is its capability to use the framework of ESMs to predict trends in sediment storage and yields for the past, present and future.

The next steps in quantifying soil redistribution on the global scale are the application of the sediment budget model on other large catchments, and validation of the model with existing data on net soil redistribution, sediment storage or yields. Furthermore, in order to make the soil redistribution model better applicable on a global scale and to prevent conflict with the underlying assumption of the simultaneous presence of floodplains and hillslopes in each grid box, the model needs to be made independent of grid resolution.

Finally to have a complete picture of the net soil redistribution and the feedbacks on the carbon and nutrient cycles, it is essential to model also other types of soil erosion, such as wind erosion (Chappell et al., 2015), tillage erosion (Van Oost et al., 2009) and gully erosion (Poesen et al., 2003).

Acknowledgements. The article processing charges for this open-access publication have been covered by the Max Planck Society. J.Pongratz was supported by the German Research Foundation’s Emmy Noether Program (PO 1751/1-1).
References


Figure 1a. Model scheme (a) with multiple flow routing (b)

Figure 1b. 

Figure 1. Model scheme (a) with multiple flow routing (b)
Figure 2. The Rhine catchment [Hoffmann et al. 2013]
Figure 3a. Scaling of floodplain (a) and hillslope (b) sediment storage from the transient simulation in the non-Alpine part of the Rhine catchment. The black dots and black trend line correspond to the observed sediment storage values from [Hoffmann et al. (2013)](Hoffmann2013). The colored dots and colored trend line correspond to modelled sediment storage values that correspond to the observation points from [Hoffmann et al. (2013)](Hoffmann2013) and fall into the borders of the Rhine catchment.
Figure 4. Observed versus modelled floodplain sediment storage for Rhine sub-catchments. The values are in percentage (actual storage divided by the sum times 100). Data on the observed sediment storage is taken from [Hoffmann et al. (2007)]. RMSE is the root mean square error.
Figure 5. Land cover and precipitation variability averaged over the Rhine catchment for the last millennium.
The red line is the 10 year mean total precipitation for the Rhine catchment. The background colors are land cover types, starting from the darkest grey to the lightest: forest, bare soil, grass, crop and pasture. Land cover and precipitation data is from MPI-ESM.
Figure 6a. (a) Timeseries of simulated average erosion (black line), average deposition (green line) and the total change in sediment storage (blue line) with respect to 850-950 AD for floodplains in the last millennium in the Rhine catchment.

Figure 6b. (b) Timeseries of simulated average erosion (black line), average deposition (green line) and the total change in sediment storage (blue line) with respect to 850-950 AD for hillslopes in the last millennium in the Rhine catchment.

Figure 6. (a) Timeseries of simulated average erosion (black line), average deposition (green line) and the total change in sediment storage (blue line) with respect to 850-950 AD for floodplains in the last millennium in the Rhine catchment. (b) Timeseries of simulated average erosion (black line), average deposition (green line) and the total change in sediment storage (blue line) with respect to 850-950 AD for hillslopes in the last millennium in the Rhine catchment.
Figure 7. Simulated change in (a) floodplain and (b) hillslope sediment storage for the Rhine catchment during the last millennium. Shown are the sediment storage for the climate change simulation, where land cover is set to the conditions of the period 850-950 AD (CC - blue line), the sediment storage for the land use change simulation, where the climate is set to the conditions of the period 850-950 AD (LUC - red line), and the sediment storage where both climate and land cover change during the last millennium (CC and LUC - black line).
Table 1. Simulation specifications for the application of the sediment budget model for the Rhine catchment. For each experiment with the sediment budget model the type of simulation (equilibrium or transient), the time period, and the initial conditions on which the simulation is based on, are given. Furthermore, we also provide the number of simulations we made with the model for a certain type of simulation, and the experiment from MPI-ESM that we used to derive the input data to force the sediment budget model.

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Simulation</th>
<th>Time period</th>
<th>Initial conditions</th>
<th>MPI-ESM of ensemble simulations</th>
<th>number of ensemble simulations</th>
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<td></td>
</tr>
<tr>
<td>default</td>
<td>transient-part1</td>
<td>850-1850 AD</td>
<td>850-950 AD last millennium</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>default</td>
<td>transient-part2</td>
<td>1850-2005 AD</td>
<td>transient-part1 historical</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>default</td>
<td>transient-part1</td>
<td>850-1850 AD</td>
<td>6000 BP last millennium</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>default</td>
<td>transient-part2</td>
<td>1850-2005 AD</td>
<td>transient-part1 historical</td>
<td>2</td>
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<tr>
<td>climate change</td>
<td>transient-part1</td>
<td>850-1850 AD</td>
<td>850-950 AD last millennium</td>
<td>1</td>
<td></td>
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<td>transient-part2</td>
<td>1850-2005 AD</td>
<td>transient-part1 historical</td>
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<td>land use change</td>
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<td>850-1850 AD</td>
<td>850-950 AD last millennium</td>
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<td>land use change</td>
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<td>1850-2005 AD</td>
<td>transient-part1 historical</td>
<td>1</td>
<td></td>
</tr>
</tbody>
</table>

Table 2. Summary of regression results of the scaling of at the end of the equilibrium and transient simulations. Here we consider only the grid cells that correspond to the observation points from [Hoffmann et al. (2013)](https://doi.org/10.1002/2013jf002,022) and fall into the borders of the Rhine catchment. The r-value is the Pearson correlation coefficient, and the slope and intercept are the scaling parameters.

| | Floodplains | | Hillslopes | |
|----------------|---------------|----------------|---------------|
| | slope | intercept | r-value | slope | intercept | r-value |
| Equilibrium | 1.659 ± 0.037 | 3.123 ± 0.130 | 0.99 | 1.085 ± 0.060 | 6.429 ± 0.180 | 0.94 |
| Transient ensemble 1 | 1.198 ± 0.038 | 3.877 ± 0.133 | 0.98 | 1.050 ± 0.064 | 4.963 ± 0.193 | 0.93 |
| Transient ensemble 2 | 1.202 ± 0.038 | 3.853 ± 0.133 | 0.98 | 1.048 ± 0.065 | 4.971 ± 0.194 | 0.93 |
| Transient ensemble 3 | 1.203 ± 0.038 | 3.85 ± 0.133 | 0.98 | 1.048 ± 0.065 | 4.972 ± 0.194 | 0.93 |
| Hoffmann et al. (2013) | 1.230 ± 0.060 | 4.450 | 0.96 | 1.080 ± 0.070 | 5.380 | 0.96 |

Table 3. Summary of regression results of the scaling of sediment storage after the equilibrium and transient simulations. Here we consider all grid cells in the Rhine catchment area. The r-value is the Pearson correlation coefficient, and the slope and intercept are the scaling parameters.

| | Floodplains | | Hillslopes | |
|----------------|---------------|----------------|---------------|
| | slope | intercept | r-value | slope | intercept | r-value |
| Equilibrium | 1.685 ± 0.015 | 2.827 ± 0.039 | 0.80 | 1.118 ± 0.016 | 6.327 ± 0.040 | 0.62 |
| Transient ensemble 1 | 1.330 ± 0.017 | 3.406 ± 0.042 | 0.67 | 1.111 ± 0.015 | 4.741 ± 0.039 | 0.63 |
| Transient ensemble 2 | 1.332 ± 0.017 | 3.401 ± 0.042 | 0.67 | 1.112 ± 0.015 | 4.740 ± 0.039 | 0.63 |
| Transient ensemble 3 | 1.332 ± 0.017 | 3.400 ± 0.042 | 0.67 | 1.112 ± 0.015 | 4.741 ± 0.039 | 0.63 |

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Table 4. Summary of regression results of the sensitivity analysis on floodplain sediment storage scaling. Here we consider only the previously mentioned selected grid cells in the Rhine catchment area. $\tau$ is the residence time of floodplain sediment. The r-value is the Pearson correlation coefficient, and the slope and intercept are the scaling parameters.

<table>
<thead>
<tr>
<th></th>
<th>slope</th>
<th>intercept</th>
<th>r-value</th>
</tr>
</thead>
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<tr>
<td><strong>Equilibrium</strong></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>$\tau$ median = 50 years</td>
<td>1.787 ± 0.041</td>
<td>2.143 ± 0.143</td>
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<tr>
<td>$\tau$ median = 260 years</td>
<td>1.659 ± 0.037</td>
<td>3.123 ± 0.13</td>
<td>0.99</td>
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<tr>
<td>$\tau$ median = 500 years</td>
<td>1.616 ± 0.037</td>
<td>3.496 ± 0.128</td>
<td>0.99</td>
</tr>
<tr>
<td><strong>Transient</strong></td>
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<td></td>
<td></td>
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<tr>
<td>$\tau$ median = 50 years</td>
<td>1.464 ± 0.055</td>
<td>2.59 ± 0.193</td>
<td>0.97</td>
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<tr>
<td>$\tau$ median = 260 years</td>
<td>1.198 ± 0.038</td>
<td>3.877 ± 0.133</td>
<td>0.98</td>
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<tr>
<td>$\tau$ median = 500 years</td>
<td>1.145 ± 0.035</td>
<td>4.128 ± 0.122</td>
<td>0.98</td>
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</table>

Table 5. Summary of sediment storage $M$ (Gt), erosion ($E$) and deposition ($D$) rates in $\text{t ha}^{-1}\text{ year}^{-1}$, and the related uncertainty ranges for the Rhine catchment for the period 850-2005 AD. The uncertainty values represent the range in the mean values due to different ensemble simulations.

<table>
<thead>
<tr>
<th></th>
<th>Mean $M$</th>
<th>Ensemble uncertainty $M$</th>
<th>Mean $E$</th>
<th>Ensemble uncertainty $E$</th>
<th>Mean $D$</th>
<th>Ensemble uncertainty $D$</th>
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<tr>
<td>Floodplains</td>
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<td>0.01</td>
<td>2.787</td>
<td>0.0015</td>
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<td>0.0005</td>
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<tr>
<td>Hillslopes</td>
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<td>2.787</td>
<td>0.0015</td>
<td>1.491</td>
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<tr>
<td>Whole Rhine catchment</td>
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<td>0.02</td>
<td>2.787</td>
<td>0.0015</td>
<td>2.787</td>
<td>0.0015</td>
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Table 6. Observed versus modelled sediment storage (Gt) for Rhine sub-catchments. The catchment area is given in $\text{km}^2$. Data on the observed sediment storage is taken from Hoffmann et al. (2007).

<table>
<thead>
<tr>
<th>Catchment</th>
<th>Catchment area</th>
<th>Observed floodplain storage</th>
<th>Modelled floodplain storage</th>
<th>Modelled hillslope storage</th>
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<tr>
<td>Lippe</td>
<td>4858</td>
<td>1.62</td>
<td>0.03</td>
<td>0.07</td>
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<td>Lower Rhine</td>
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<td>Emscher</td>
<td>806</td>
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<td>Ruhr</td>
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<td>0.15</td>
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<td>Mosel</td>
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<tr>
<td>Neckar</td>
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<td>4.19</td>
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<td>Ill</td>
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<td>4.66</td>
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<td>2.28</td>
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