Response to reviews of “Assessing the large-scale impacts of environmental change using a coupled hydrology and soil erosion model” submitted to *Earth Surface Dynamics* for consideration for publication.

*We warmly thank the two reviewers and the editor for their positive and constructive reviews of our manuscript. Below we provide a response to their concerns and explain which revisions were implemented and why a certain approach was taken. All changes are indicated in the document with indication of track changes.*

**Referee #1**
The paper presents an innovative combination of the existing SPHY hydrological and MMF erosion models, with intended use at the large catchment and decadal scales. Despite this foreseen use at large spatial and temporal scales, the combined model is presented as a physically-based model. I agree with this assessment: most relevant processes that determine catchment water and sediment yield are included, and well presented in the paper.

*We would like to thank the reviewer for his nice comments on the manuscript.*

My main concern in this part of the paper is that there is insufficient attention for the large number of parameters that these extra formulae introduce. I recommend that the reader be provided with more information about all parameters, especially whether they are 1) measurable or not, 2) available from literature, and if so for which kind of environments, or 3) most be obtained through calibration. Ideally, this would go together with a detailed global sensitivity analysis, that could give insight in how robust model simulations are under the weight of all these parameters. A good example for how to do this is <https://www.geosci-model-dev-discuss.net/gmd-2017-236/>/, or (I apologize) my own paper in Computers and Geosciences about the Lorica model a few years back. If the authors find that sensitivity analysis is a bridge too far in this already long paper, then that lends more weight to my first suggestion (provide details - even if it happens in supplementary material).

*Indeed, the model contains a large number of parameters, although most of them we obtained from literature and are referenced in the manuscript. Still, we agree that a table that contains a comprehensive list of all the parameters is very useful. Therefore, we have added a table to the Supplementary Material that includes all model parameters mentioned in the manuscript. The table indicates the following aspects: landuse-specific, measurable, calibration, literature based and a citation where we obtained the literature values of the parameters.*

The model is then calibrated and validated to simulate water and sediment yield for a large catchment in Spain, and two scenarios for the future state of the catchment are used to demonstrate the models’ capability. The quality of calibration and validation results is not concerning at first sight, but should be placed in the context of other models’ results - even though these are bound to be in other areas, for other timescales, etc. Only reporting such results leaves the reader with questions.
So far, the SPHY-MMF model has not been applied in other catchments, therefore, we cannot report previous calibration and validation results on soil erosion and sediment yield. However, the hydrological model SPHY has been applied previously. Terink et al. (2015) reports several model applications in Romania, the Himalaya and Chile. We obtained similar calibration and validation results as reported by Terink et al. (2015). We have referred to these results in the manuscript. Comparison with performance of other erosion models would indeed be interesting, but only if applied to the same catchment and using the calibration strategy. Otherwise, we do not know the origin of the differences in performance, making objective interpretation of results of little value.

During my review, I also missed reporting on results from the first (conservation agriculture) scenario – a climate change scenario appeared to get all the attention.

*The sustainable land management scenario was evaluated in section 3.3, where we applied reduced tillage to cereals and horticulture. The results are shown in Figure 7, indicated with the dashed lines. We have clarified this in the revised manuscript.*

Figures in the paper are good as it stands - although a bit more detail in them and their captions would make them more useful. I would appreciate another table with information on parameters (see my comment above). Detailed annotations and suggestions are available in the attached scan. All in all, I consider this an important contribution to literature presenting a model that usefully supplements the range of available models. I especially appreciate the authors’ detailed and deliberate explanation of model equations. In light of the modest suggestions for improvement, I suggest minor revisions.

*We have added references to equations in the figure captions of Figures 1, 2 and 3.*

Page 2, line 28: By now you should become a bit more specific about which models you are thinking of. Perhaps a table works best.

*We prefer not to mention specific models at this stage, especially given the large number of available erosion and sediment models. Nevertheless, we have added reference to two model review papers to give an indication of what kind of models we are referring.*

Page 3, line 22: Introduction: well structured, clear, but insufficiently supported by references. The fact that there are many references to choose from, should not lead to you not showing any.

*We have now supported the introduction with specific references.*

Page 3, line 32: Specially at daily resolution, should the erosion model not feed back to SPHY as well? You erode and deposit top soil, with implications for infiltration and erodibility.

*Ideally a feedback from the soil erosion model to the hydrological model would result in changes to the top soil depth and subsequently its soil physical properties. However, given the fact that the model is intended to be applied at decadal time scales, the*
erosion rates are not high enough (<1 mm yr\(^{-1}\)) to lead to substantial decreases of soil depth. Also, this could lead to problems when locally very high erosion rates are projected, eroding the top soil within the simulation period. For Landscape Evolution Models operating at longer time scales this would certainly be more relevant.

Page 5, line 5: Does the single flow algorithm limit your model’s usefulness to non-ploughed, i.e. non-smoothed, landscapes?

*We don’t expect this to be the case, especially at the spatial resolution the model is intended to be applied (i.e. between 200 m and 1 km). A single flow might affect flow accumulation and concentrated flow processes in some cases, therefore we are actually working on a revised version with possibility of multiple flow simulation to prevent excessive concentration of flow.*

Page 5, line 7: I am very sympathetic of the brief model descriptions, so I like 2.2. However it gives me the idea that this ‘physical-based model’ still has many calibration parameters. Can you give us an overview of measurable / calibration parameters.

*We have included a table in the Supplementary Material, see previous comments.*

Page 8, line 25: Have these been introduced yet? How many are there?

*The soil texture classes have been introduced in the introduction paragraph of section 2.3. There are three soil texture classes, i.e. sand, silt and clay.*

Page 11, line 11: Does that not follow from Eq. 20-22 and the amount of water in the reservoir?

*Equations 20-22 determine how much sediment is deposited in the cell of its origin, i.e. immediate deposition of detached particles. The trapping efficiency of the reservoirs (Eq. 30) determines how much of the total amount of sediment that is transported from all the upstream cells is deposited in the reservoir, which is function of the capacity of the reservoir and the drainage area of the subcatchment.*

Page 12, line 1: With Ch. 2 in mind:

1. Great and calm explanation. I think I know what this model does
2. The model has many parameters. A table, perhaps in suppl. mat. Would help to distinguish measureable, literature based and calibration parameters.

*We have included a table in the Supplementary Material, see previous comments.*

Page 12, line 1: These figures are great but can be made more useful by referring to your equations in them.

*We have included references to the equation in the figure captions.*
Page 14, line 17: Why validate on the uncertain, old NDVI period, and calibrate on the good? Can you split more “fairly”?

Indeed, it would be better to validate the model in a period where MODIS NDVI data are available. Unfortunately, these data are only available since 2000 and our climate forcing (precipitation and temperature) are only available until 2012. So we have a maximum of 13 ‘good’ data years available. Especially for calibration and validation of the soil erosion model, a fairly long period is needed to include a number of large events which cause most erosion. When we would split the data into two equally sized periods, we would get two periods of 6 or 7 years, which would limit the occurrence of large events within these periods. Therefore, we choose to use a calibration period of 10 years and a validation period of 20 years, even though no NDVI was available for the validation period.

Page 16, line 1: Table caption should clarify differences between cal/val target on one hand and Cerdan/Maetens number on other hand.

We are uncertain about what the reviewer means with this comment. The table shows two columns with predicted hillslope erosion rates under calibration and under validation runs respectively, followed by two columns with published hillslope erosion rates by Cerdan/Maetens.

Page 18, line 3: You do not discuss the conservation agriculture scenario results. Or is that your ‘reference’ scenario? That would be confusing and should be improved.

The sustainable land management (SLM) scenario was applied to two crops, i.e. cereals and horticulture, where we assumed that after harvest the fields are not tilled until the next sowing. We parameterized this by setting the plant height to 0 and leaving all other input parameters unchanged, which is different from the reference scenario. The results are shown in Figure 7, where the dashed lines show that soil erosion decreases under the SLM scenario. We have clarified this in section 3.3 and in the caption of Figure 7.

Page 20, lines 2-7: This feels a little too much like an abstract or an advertisement. If in discussion, better at the end after you have provided the reader with the insight that supports it.

We have removed this part from the manuscript.

Page 20, lines 15-21: Well, you calibrated a few other parameters, and literature values are not always directly transferable. This aspect deserves more attention.

We have added a discussion on the calibration procedure to the Discussion.

Page 20, line 22: If that’s your main finding, a much simpler model would do. Ample literature confirms this finding.
This is certainly not our main finding, rather the main limitation of the current model, i.e. that the model projects unrealistic high erosion rates in the cells where most flow accumulates. We are currently working on an enhanced channel erosion module to fix this. We have changed this sentence accordingly.

Page 21, line 2: Show/cite some examples from literature. People must have done this for a long time, I think.

We have added citations to recent publications that have incorporated fluvial processes into soil erosion and landscape evolution models.

Referee #2
First of all, I would like to congratulate the authors for the effort and dedication developed in this work. Any proposal of erosion modeling that goes beyond the estimation of potential annual erosive rates is an appreciable step forward for the scientific community, managers and, hence, the society. Reading the document has been easy, interesting and instructive to me.

We would like to thank the reviewer for his nice comments on the manuscript.

My general concerns are the following:
1) Studying the configuration of the model, with a clearly hillslope nature, I see its particular strength more related to the temporal scale of simulation, not so much with the spatial scale, and also with the role of vegetation on sediment transport and erosion processes. That is, both the considered dt and the adopted spatial resolution with its consequent limitations for the modeling of processes in Mediterranean environments can be justified by the model’s ability to generate long time series based on processes and distributed information under different land use or climate scenarios. This is not reflected in the current manuscript and, in my opinion, its limitations are then not sufficiently justified.

We agree that the temporal scale of the model is also a strength of the model, however, the model is intended to be applied at large spatial scales, from which the alternatives are mostly of empirical nature, such as WATEM-SEDEM, AGNPS, (R)USLE and SWAT (MUSLE). Most of these models do not include the most relevant hydrological and soil erosion processes that we explicitly consider in our model, in particular intra-annual vegetation development and sediment deposition. Indeed, the considered daily time step and the adopted spatial resolution induce limitations for detailed soil erosion assessments. We have included a discussion on these issues in the Discussion section. Furthermore, the model has limitations in its capacity to accurately simulate concentrated flow, as also mentioned in the Discussion and in response to Reviewer 1. We are therefore working on an enhanced channel erosion module. See also the comments below regarding the limitations and considerations regarding extreme events and the spatial resolution of the model.

2) The limitations of the model have to be declared and analyzed more in depth. Especially, I see problematic the modeling of extreme events, which are important in Mediterranean environments with frequent sub-hour time pulses. What is the implication of the runoff model
proposed in the results, as they indicate a considerable increase in this type of events in the considered future scenario?

We agree, in some environments, like in the Mediterranean, sub-hourly rainfall amounts are often responsible for most soil erosion. However, often (sub-)hourly data are not available at the large spatial scale the model is intended to be applied. While (sub-)hourly data may be obtained from local meteorological stations, the data need to be interpolated to the model domain, which most likely results in large spatial and temporal uncertainties. Also, most climate model output is only available with a daily time step. A (sub-)hourly time step would limit the application of climate change scenarios and beyond events. Our results (Figures 8 and 9) show that the model is capable to simulate the increase of soil erosion by the expected increase in extreme precipitation. We have included a discussion on the limitations regarding the daily time step in the Discussion section.

Has sub-hour rainfall data been analyzed? Could the model be modified to include these cases, \((\alpha = 1 \text{ at } t = n \text{ and } \alpha = 0 \text{ at } t \neq n?)\), I see an attenuation effect by the model for this cases.

The surface runoff equation (Eq. 8) includes a parameter that indicates the fraction of the daily rainfall that occurs in the hour with the highest intensity. This parameter could be set to 1, to indicate that all daily rainfall falls within one hour. However, rainfall in these environments is not only concentrated in one hour events and the case that the daily rainfall is more evenly spread over the day should also be considered. Although we used observed station data to determine the relation between daily and hourly precipitation, there is always a tradeoff between reality and model feasibility. The model is intended to be used at large spatial and temporal scales, which ultimately results in disregarding small scale phenomena (both spatial and temporal). For these phenomena a smaller scale model would be better suited.

Also, I see inconsistencies, or I do not understand, the units in this part of the model \((\alpha \text{ in } h^{-1}?, \ Q_{surf} \text{ mm/day}?)\), please clarify.

In the original manuscript we made some mistakes in the units for the variables used in Eq. 8. The infiltration rate \(f\) and precipitation \(P\) are in mm and \(\alpha\) is a fraction and, therefore, dimensionless. This gives \(Q_{surf}\) in mm as well. We have changed the text accordingly.

Another limitation is related to the selected cell size (200m grid size), Why this resolution? Is it related to the computational cost of the model? (I would like to know something about this issue), or is related to the remote sensing images? What limitations does this present from the point of view of the observed erosion processes in the study area, the forcing agents and their spatial distribution from the obtained results?

The selected cell size is a tradeoff between the hydrological model and the soil erosion model. Indeed, for soil erosion processes a smaller cell size would be more appropriate. The selected cell size of 200 m is the lowest possible value the hydrological model allows, according to Terink et al. (2015). Some sub-soil processes, such as lateral flow and base flow, only act at large spatial scales. Therefore, the model has a lower limit
for the spatial resolution. We have included a discussion on this issue in the Discussion section.

3) Fluvial vs hillslope contributions: the authors declare limitations of the model for modeling fluvial transport, which, in my opinion, should be assessed in the future from a fluvial sub-model that includes the basic erosion and transport processes (bedload + SS), integrating what that comes from the hillslopes (water and sediment) at different points. However, if I’m not wrong, the calibration/validation has been made from SSY estimated from reservoirs, what fraction corresponds to fluvial/hillslope contributions based on reservoir measurements?, this analysis is important and should be adressed given the process-based nature of the model.

Indeed, the current model does treats erosion in channels the same as erosion on hillslopes. As stated above, we are working on a separate channel erosion module which would be part of a future model update (see Discussion section). However, in the current model, we do account for channel deposition processes, through the transport capacity equation (Eq. 28). Currently, this equation largely corrects for the high erosion rates generated by high accumulated flow rates in the river network. The current model is not able to distinguish between hillslope and fluvial contributions. In a future update of the model we would be able to perform such analysis.

4) Although the document is well written and easy to read, the introduction seems too long and could be summarized.

We think that the Introduction provides the essential background to better understand the processes included in the model and its intended use. Furthermore, Reviewer 1 commented that the Introduction is well structured and clear and asked for supporting references. Therefore, we have tried to streamline the introduction as much as possible without removing crucial information.

On the contrary, more detailed information about the validation, calibration data, especially of the selected reservoirs (bathymetries, topographies, sediment grain sizes, ...) and SSY assessment is missing.

Reservoir sediment yield was obtained from literature (Avendaño-Salas et al., 1997), which included bathymetric data on changes in reservoir volume and bulk density of deposited sediment, from which we determined the yearly sediment yield. Hillslope erosion (SSY) was also calibrated using literature values (Cerdan et al., 2010; Maetens et al., 2012). We have clarified the calibration procedure in section 3.2.

It may be interesting to incorporate a section of uncertainty analysis.

As suggested by reviewer 1, instead of a full sensitivity analysis, which would make the paper too long at this stage, we have added a table to the Supplementary Material that includes all model parameters mentioned in the manuscript. The table indicates the following aspects: landuse-specific, measurable, calibration, literature based and a citation where we obtained the literature values of the parameters.
Please, check the citation format of the entire document.

*We have changed the citation format.*

In general, I encourage the authors to highlight the most interesting aspects of the model, taking into account the spatial and temporal scales adopted, as well as reasonably stating of the associated limitations in order to evaluate not only the model, but all the related challenges. Some minor comments are reported in the attached file.

Page 4, line 11: Please, specify satellite platform and data correction used.

*The user could provide any NDVI images, as long as they are in the same resolution and within the domain as the model. In the model application we used MODIS NDVI images, but the model is not limited to this specific dataset. Therefore, we do not specify here which satellite platform should be used, this is up to the user.*

Page 9, line 1: Put this values also at the context studied by Knapen et al. (Resistance of soils to concentrated flow erosion: A review).

*These values refer to the detachability of the soil by raindrop impact (K), rather than detachability of the soil by runoff (DR), which is used in Eq. 19. Both K and DR cannot directly be obtained from Knapen et al. (2007), which consider the concentrated flow erodibility and critical flow shear stress. Equations 18 and 19 differ from the soil detachment equations discussed in Knapen et al. (2007), which include several process-based approaches, such as excess shear stress, excess stream power and transport capacity deficit approaches. These approaches either use concentrated flow erodibility or critical flow shear stress to quantify the detachability of the soil by runoff. The SPHY-MMF model uses a different approach, which may be classified as an intermediate between empirical and process-based approaches. Therefore, the values reported in Knapen et al. (2007) are not directly comparable with the values for K and DR.*

Page 18, line 11: Are you sure that the model is capturing the increase of heavy precipitation? How this can condition these results? Please stress the limitation of the model and uncertainties.

*Figure 8 shows that an increase of heavy precipitation is expected under the future climate change scenario. This results in an increase of soil erosion as well (Figure 9). However, this does not lead to an increase of reservoir sediment yield, but a decrease. We argue that this is caused by a decrease of runoff, which causes a decrease of transport capacity (see Eq. 28).*
Assessing the large-scale impacts of environmental change using a coupled hydrology and soil erosion model

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Abstract. Assessing the impacts of environmental change on soil erosion and sediment yield at the large catchment scale remains one of the main challenges in soil erosion modelling studies. Here, we present a process-based soil erosion model, based on the integration of the Morgan-Morgan-Finney erosion model in a daily-based hydrological model. The model overcomes many of the limitations of previous large-scale soil erosion models, as it includes a more complete representation of crucial processes like surface runoff generation, dynamic vegetation development, and sediment deposition, and runs at the catchment scale with a daily time step. This makes the model especially suited for evaluation of the impacts of environmental change on soil erosion and sediment yield at large spatial scales, regional scales and over decadal periods. The model was successfully applied in a large catchment in southeastern Spain. We demonstrate the model’s capacity to perform impact assessments of environmental change scenarios, specifically simulating the scenario impacts of intra- and inter-annual variations in climate, land management and vegetation development on soil erosion and sediment yield.

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1 Introduction

Climate change will likely affect soil erosion and sediment yield across scales (e.g. Nearing et al., 2004; Li et al., 2006; Burt et al., 2016). However, assessing the impacts of environmental change on soil erosion and sediment yield at the large catchment scale remains one of the main challenges in soil erosion modelling studies (de Vente et al., 2013; Poesen, 2018). Most soil erosion and sediment yield models adopt simplified model formulations, are applied at low spatial and temporal resolutions, and often only partly represent the impacts of changes in land use or climate conditions. This often leads to unreliable results that do not sufficiently increase process understanding or support decision-making (de Vente et al., 2013). To overcome part of these limitations, here, we present a process-based, large-scale, soil erosion model, coupled to a hydrological model, accounting for the most relevant factors determining soil erosion by water, including saturated and infiltration excess surface runoff, dynamic vegetation development and sediment deposition.
First of all, soil erosion by water occurs by the impact of raindrops and by the flow of water on the soil surface or the river bed, overland flow and river flow. It is therefore crucial to quantify raindrop impact, overland flow and possible interactions with vegetation cover. Soil erosion by the impact of raindrops is a function of the amount and the size of the raindrops that reach the soil surface (Morgan, 2005). Vegetation cover can reduce the impact of raindrops by interception, separating the precipitation into direct throughfall, with a high impact, and leaf drainage, with a lower impact (Morgan and Nearing, 2011). Assessment of soil erosion, therefore, needs to account for spatial and temporal changes in vegetation cover. Nevertheless, most large-scale soil erosion assessments do not consider dynamic seasonal and inter-annual vegetation development, while previous studies have shown that cropping patterns, inter-annual trends in precipitation variability and land use changes can have a significant impact on soil erosion rates (e.g. Maetens et al., 2012).

Soil erosion is also a function of runoff (Morgan, 2005). Runoff generation depends on surface and sub-surface processes and is a function of precipitation volume and intensity, soil moisture and soil hydraulic properties (Kirkby, 1988). Process-based models often incorporate a separate hydrological model to simulate surface runoff generation, which then directly forces soil erosion by runoff (Morgan, 2005). Surface runoff may be generated by several distinct processes, from which saturation excess and infiltration excess are the most common processes (Beven, 2012). Saturation excess surface runoff occurs when the soil water content reaches saturation, while infiltration excess surface runoff occurs when the precipitation intensity exceeds the soils infiltration capacity. However, many large-scale soil erosion models only consider saturation excess surface runoff, disregarding the infiltration excess surface runoff mechanism. Infiltration excess surface runoff is a sub-daily process that is often only implemented in event-scale models (e.g. Nearing et al., 1989; Morgan et al., 1998). Infiltration excess surface runoff is an especially important process in areas where a major part of soil erosion takes place during extreme rainfall events with high precipitation intensities (Mulligan, 1998; López-Bermúdez et al., 2002; Farnsworth and Milliman, 2003; González-Hidalgo et al., 2007; Gonzalez-Hidalgo et al., 2012).

Furthermore, assessing catchment sediment yield further requires evaluation of the sediment transport capacity and sediment deposition. Sediment deposition occurs when the sediment transport capacity of the runoff is exceeded and basically depends on the interaction between the texture of the detached soil material, flow velocity and the roughness of the surface (Rose et al., 1983). Large particles are more likely to be deposited close to the source, while small particles are more easily brought and maintained into transport. The roughness of the surface is a combination of the roughness of the soil surface and the roughness caused by vegetation soil roughness and vegetation roughness (Chow, 1959). Many studies have highlighted the importance of accounting for sediment transport and sediment deposition, claiming that often a large part of the eroded sediment is deposited close to its source (Walling, 1983; de Vente et al., 2007). However, many large-scale soil erosion models insufficiently consider this process or even only simulate soil detachment processes.

From the available soil erosion models, process-based models aim to incorporate the most relevant processes driving soil detachment, sediment transport and deposition, as described in the previous paragraphs, and see Morgan (2005) for an overview of process-based models. Process-based models often run at small spatial (hillslope to small catchment) and temporal scales (hourly to daily time steps). Most detailed assessments are obtained from event-scale model applications in process-based models, such as WEPP (Nearing et al., 1989) and EUROSEM (Morgan et al., 1998), which require detailed observational
input data, such as (sub-)hourly precipitation and detailed spatial information, topographic data, and incorporate a large number of model calibration parameters, calibration parameters (Govers, 2011). While these models present a strong potential to provide increased process understanding, it is often unfeasible to obtain all required input data for large catchments. Furthermore, the high uncertainty on how input data and model parameters will change under scenarios of environmental change severely limits their application in large-scale assessments.

At larger scales, soil erosion is often assessed using so-called empirical erosion models, see de Vente et al. (2013) for an overview. These models are derived from field studies where soil erosion has been observed under different land use, management, soil, climate, and topographical conditions. The most well-known and applied empirical model is the Universal Soil Loss Equation (USLE; Wischmeier and Smith, 1978) and its derivatives RULSE (Renard et al., 1997) and MUSLE (Williams, 1995). While the empirical formulations of the USLE were obtained at plot-scale, the model is often applied at much larger scales, sometimes in combination with a sediment transport capacity equation or a sediment delivery ratio to assess sediment yield (e.g. Van Rompaey et al., 2001; de Vente et al., 2008). Due to its simplicity, the USLE can be applied with a relatively limited amount of input data. However, their main restriction is the limited number of processes accounted for (e.g. the USLE and RUSLE based models only consider sheet and rill erosion) and the limited potential to evaluate the impacts of changes in climate and land management (Govers, 2011; de Vente et al., 2013). Furthermore, these models are typically applied at annual time steps, largely neglecting intra-annual variation of climate and vegetation conditions.

Most current soil erosion models have a limited potential for application at larger temporal and spatial scales (i.e. process-based models) or lack sufficient representation of the underlying soil detachment and sediment transport processes and sensitivity to changes in land use or climate (i.e. empirical models), making them of limited use for scenario studies and process understanding. Here, we present a process-based soil erosion model based on the integration of the Morgan-Morgan-Finney erosion model (MMF; Morgan and Duzant, 2008) and the spatially distributed hydrological model Spatial Processes in Hydrology (SPHY; Terink et al., 2015). This integrated model overcomes many of the limitations of previous large-scale soil erosion models, as it includes a more complete representation of crucial processes, such as surface runoff generation, dynamic vegetation development, and sediment deposition, and runs at the catchment scale with a daily time step. This makes the model especially suitable for evaluation of the inter- and intra-annual impacts of environmental change on soil erosion and sediment yield at large spatial and temporal scales. In the next paragraphs we first present the different model components and enhancements as compared to previous models. Then we illustrate its functionality and potential for scenario studies by application to the Upper Segura catchment in southeastern Spain under present and projected future climate conditions.

2 Model Description

2.1 Model Overview

The SPHY-MMF model presented here is an integration of the (Modified) Morgan-Morgan-Finney soil erosion model into the SPHY hydrological model (version 2.1). Figure 1 shows the main hydrological and soil erosion processes considered by the
Figure 1. Overview of the model: (a) representation of a single cell, (b) the hydrological processes, and (c) the soil erosion processes, where $P$ is precipitation, $DT$ is direct throughfall (Eq. 14), $LD$ is leaf drainage (Eq. 13), $F$ is detachment by raindrop impact (Eq. 18), $H$ is detachment by runoff (Eq. 19), $D$ is immediate deposition (Eq. 20) and $G$ is sediment routed to downstream cells (Eq. 27).

model. SPHY is a spatially distributed leaky-bucket type model that simulates hydrological processes on a cell-by-cell basis at a daily timestep (Terink et al., 2015). The model is written in the Python programming language using the PCRaster dynamic modelling framework (Karssenberg et al., 2010). MMF is a conceptual soil erosion model that originally is applied with an annual time step. Here we present a modification of the model at a daily time step, fully integrated with the SPHY model. MMF receives input from the SPHY model, such as effective precipitation (throughfall), runoff and canopy cover for calculation of erosion and deposition processes. The model parameters are presented in Table S1.

2.2 Hydrological model

SPHY simulates most relevant hydrological processes (Figure 1b), such as interception, evapotranspiration, dynamic evolution of vegetation cover, surface runoff, and lateral and vertical soil moisture flow at a daily time step. The model is described in full detail by Terink et al. (2015), therefore, here we only provide a summary of the processes that are simulated by the model, some hydrological processes that have been changed with respect to the original SPHY model, and a detailed description of the processes that are related to the integration of MMF.
SPHY requires daily precipitation and temperature maps as input. Effective precipitation is determined by subtracting canopy storage and interception from precipitation. Canopy storage is determined from the Leaf Area Index (LAI), which is derived from Normalized Differenced Vegetation Index (NDVI) images. Reference evapotranspiration is determined using the Hargreaves equation (Hargreaves and Samani, 1985), which is subsequently multiplied by the crop coefficient to obtain the potential evapotranspiration. The crop coefficient is determined from the NDVI images using a linear relationship. Actual evapotranspiration is obtained by multiplying the potential evapotranspiration by a reduction factor for water deficit or water surplus, which are functions of current soil water content, soil hydraulic properties and plant-specific water need. Surface runoff is determined by a daily implementation of the Green-Ampt formula (Heber Green and Ampt, 1911) and is a function of infiltration, effective precipitation and soil hydraulic properties. The soil profile consists of three layers, i.e. rootzone, subzone and groundwater layer. Water can percolate from the rootzone to the subzone and from the subzone to the groundwater layer. Water travels from the subzone to the rootzone through capillary rise. Water drains from the rootzone as lateral flow and from the groundwater layer as baseflow. The total runoff is the sum of surface runoff, lateral flow and baseflow. All soil processes are functions of current water content (in the respective layers) and soil hydraulic properties, i.e. saturated hydraulic conductivity, saturated water content, field capacity and wilting point. Water is routed using a single flow algorithm (Karssenberg et al., 2010). A flow recession coefficient accounts for flow delay from channel friction. When reservoirs are present, the user can opt to include an advanced routing scheme accounting for reservoir storage and outflow.

2.2.1 Evapotranspiration

The actual evapotranspiration \( ET_a \) is determined by multiplying the potential evapotranspiration with the reduction parameters for water surplus and water deficit conditions. In the current version of the hydrological model we have changed the reduction parameter for water shortage conditions by the method proposed by Allen et al. (1998):

\[
K_s = \frac{TAW - D_r}{(1-p)TAW}
\]  

(1)

Where \( K_s \) is the reduction parameter for water shortage (-), \( TAW \) is the total available water in the rootzone (mm), \( D_r \) the root zone depletion (mm) and \( p \) the depletion fraction (-). The total available water \( TAW \) is defined as:

\[
TAW = \theta_{FC} - \theta_{WP}
\]  

(2)

Where \( \theta_{FC} \) is the soil water content at field capacity (mm) and \( \theta_{WP} \) the soil water content at wilting point (mm). The root zone depletion \( D_r \) is defined as:

\[
D_r = \theta_{FC} - \theta
\]  

(3)

Where \( \theta \) is the current soil water content (mm). The depletion fraction \( p \) is defined as the fraction of \( TAW \) that a crop can extract from the root zone without suffering water stress, which is determined by the following equation:

\[
p = p_{tabular} + 0.04(5 - ET_{pot})
\]  

(4)
Where \( p_{\text{tabular}} \) is a landuse-specific tabular value of the depletion fraction (-) and \( ET_{\text{pot}} \) is the potential evapotranspiration (mm). Values for the landuse-specific tabular value of the depletion fraction can be obtained from Allen et al. (1998) (Table 22).

Open-water evaporation is determined in the reservoir cells. In these cells all soil hydraulic processes are turned off and runoff equals precipitation. Open-water evaporation is determined as follows and assumes presence of water minus open-water evaporation. Reservoir cells cannot dry up, i.e. we assume that there is always water present in the reservoir cells. Open-water evaporation is determined as follows:

\[
ET_{\text{open-water}} = k_{c_{\text{open-water}}}ET_{\text{ref}} \tag{5}
\]

Where \( k_{c_{\text{open-water}}} \) is the crop coefficient value for open-water evaporation (-) and \( ET_{\text{ref}} \) is the reference evapotranspiration (mm). We set \( k_{c_{\text{open-water}}} \) to a value of 1.2, after Allen et al. (1998). In each time step the open-water evaporation is subtracted from the reservoir storage.

### 2.2.2 Infiltration excess surface runoff

The original SPHY model simulates saturated surface runoff but not infiltration excess surface runoff. Therefore, we have incorporated an infiltration excess equation at a daily time step based on the Green-Ampt formula (Heber Green and Ampt, 1911). We assumed a constant infiltration rate \( f \) (mm), which is determined for each cell and each day by:

\[
f = \frac{K_{\text{eff}}}{24} \left[ 1 + \frac{\theta_{\text{sat}} - \theta}{\theta_{\text{sat}}} \right]^\lambda \tag{6}
\]

Where \( K_{\text{eff}} \) is the effective hydraulic conductivity (mm), \( \theta_{\text{sat}} \) is the saturated water content (mm), \( \theta \) is the actual water content (mm), and \( \lambda \) is a calibration parameter (-). Bouwer (1969) suggested an approximation of \( K_{\text{eff}} \approx 0.5 K_{\text{sat}} \). We included a calibration parameter \( k \) to be able to change the value of \( K_{\text{eff}} \) as a fraction of \( K_{\text{sat}} \) (\( K_{\text{eff}} = kK_{\text{sat}} \)).

Infiltration excess surface runoff occurs when the precipitation intensity exceeds the infiltration rate \( f \) (Beven, 2012). Analysis of hourly precipitation time series for 25 years (1991-2015) from 5 precipitation stations in a large catchment in southeastern Spain showed that, on average, the highest precipitation intensity was recorded in the first hour of the rain storm and decreases linearly until the end of the storm. We assumed a triangular-shaped precipitation intensity \( p(t) \) (mm hr\(^{-1}\)) according to:

\[
p(t) = -\frac{1}{2} \alpha^2 Pt + \alpha P \tag{7}
\]

Where \( \alpha \) is the fraction of daily rainfall that occurs in the hour with the highest intensity (-), \( P \) is the daily rainfall (mm), and \( t \) is an hourly time step. Daily infiltration excess surface runoff \( Q_{\text{surf}} \) is determined as:

\[
Q_{\text{surf}} = \begin{cases} 
\frac{(\alpha P - f)^2}{\alpha^2 P} & \text{if } \alpha P > f \\
0 & \text{if } \alpha P \leq f
\end{cases} \tag{8}
\]
2.2.3 Dynamic vegetation processes

SPHY-MMF contains a dynamic vegetation module that allows characterization of the seasonal and inter-annual differences in vegetation cover and resulting canopy storage, interception and precipitation throughfall. The latter is subsequently used in both the hydrological and soil erosion model. A time series of NDVI images is used as input for the dynamic vegetation module. NDVI images may only be available for a limited period, e.g. from 2000 - present for MODIS NDVI images (Moderate Resolution Imaging Spectroradiometer; Didan, 2015). Therefore, in the Model Application section we present a method to obtain NDVI images for historical and future model assessments. The Leaf Area Index (LAI) is determined from the individual NDVI images using the following logarithmic relation, which is valid for vegetation that is evenly distributed over a surface (Sellers et al., 1996):

\[
LAI = \text{LAI}_{\text{max}} \frac{\log(1 - FPAR)}{\log(1 - FPAR_{\text{max}})}
\]  

(9)

Where \( \text{LAI}_{\text{max}} \) is the maximum LAI (-), \( FPAR \) is the photosynthetically active radiation (-) and \( FPAR_{\text{max}} \) is the maximum \( FPAR \) (-), which is set to 0.95 (Sellers et al., 1996). The maximum LAI \( \text{LAI}_{\text{max}} \) is vegetation dependent, values for several vegetation types can be found in Sellers et al. (1996). The photosynthetically active radiation \( FPAR \) is determined as follows:

\[
FPAR = \frac{(SR - SR_{\text{min}})(FPAR_{\text{max}} - FPAR_{\text{min}})}{SR_{\text{max}} - SR_{\text{min}}} + FPAR_{\text{min}}
\]  

(10)

Where \( SR \) is a transformation of NDVI (-), \( SR_{\text{min}} \) and \( SR_{\text{max}} \) are the minimum and maximum \( SR \) values (-), respectively, and \( FPAR_{\text{min}} \) is the minimum \( FPAR \) (-), which is set to 0.001 (Sellers et al., 1996). \( FPAR \) is bounded by \( FPAR_{\text{min}} \) and \( FPAR_{\text{max}} \). \( SR \) is determined as follows:

\[
SR = \frac{1 + NDVI}{1 - NDVI}
\]  

(11)

\( SR_{\text{min}} \) and \( SR_{\text{max}} \) are determined with Equation Eq. 11, applying an NDVI value corresponding to the 5% and 98% quantiles, respectively.

2.3 Soil erosion simulation with a daily-based Morgan-Morgan-Finney model

The soil erosion model is based on the Modified MMF model (Morgan and Duzant, 2008). In the current model (Figure Fig. 1c), total soil erosion is calculated from detachment by raindrop impact and detachment by runoff, while sediment yield is calculated by routing detached sediment, considering within cell deposition and sediment transport capacity. Detachment of soil particles from raindrop impact is determined from the total rainfall energy, which is determined for direct throughfall and leaf drainage, respectively. Detachment of soil particles by runoff is determined from the accumulated runoff from the hydrological model. Both soil erosion equations account for the fraction of the soil covered by stones and vegetation or snow and are determined separately for three texture classes (sand, silt, clay). Within cell deposition is calculated as a function of vegetation and surface roughness. The remainder of the detached sediment is taken into transport and routed through the catchment, taking into
account the transport capacity of the flow and the trapping efficiency of the reservoirs. The next paragraphs provide a detailed description of all these processes.

### 2.3.1 Estimation of rainfall energy

The total kinetic energy of the effective precipitation ($KE, \text{J m}^{-2}$) is used to determine the detachment of soil particles by raindrop impact and is defined as:

$$KE = KE_{DT} + KE_{LD}$$

(12)

Where $KE_{LD}$ is the kinetic energy of the leaf drainage ($\text{J m}^{-2}$) and $KE_{DT}$ is the kinetic energy of the direct throughfall ($\text{J m}^{-2}$).

The kinetic energy of the leaf drainage is based on Brandt (1990):

$$KE_{LD} = \begin{cases} 
0 & \text{for } PH < 0.15 \\
LD(15.8PH^{0.5} - 5.87) & \text{for } PH \geq 0.15 
\end{cases}$$

(13)

Where $LD$ is the leaf drainage (mm) and $PH$ is the plant height (m), specified for each landuse class.

The kinetic energy of the direct throughfall is based on a relationship described by Marshall and Palmer (1948), which is representative of a wide range of environments (Morgan, 2005):

$$KE_{DT} = DT(8.95 + 8.44 \log_{10} I)$$

(14)

Where $DT$ is the direct throughfall (mm) and $I$ is the intensity of the erosive precipitation ($\text{mm h}^{-1}$). The intensity of the erosive precipitation is a model parameter and varies according to geographical location. Morgan and Duzant (2008) proposes 10 \text{mm h}^{-1} for temperate climates, 25 \text{mm h}^{-1} for tropical climates and 30 \text{mm h}^{-1} for strongly seasonal climates (e.g. Mediterranean, tropical monsoon).

The leaf drainage $LD$, i.e. precipitation that reaches the soil surface as flow or drips from the leaves and stems of the vegetation, and direct throughfall $DT$, i.e. precipitation that reaches the soil surface directly through gaps in the vegetation cover, from equations 13 and Eq. 13 and Eq. 14, are obtained from the effective precipitation ($P_{\text{eff}}, \text{mm}$). The effective precipitation (throughfall, $P_{\text{eff}}, \text{mm}$) from the hydrological model is first corrected for the slope angle, following Choi et al. (2017):

$$P_{\text{eff}} = P_{\text{eff}} \cos S$$

(15)

Where $P_{\text{eff}}$ is the effective precipitation (mm) and $S$ the slope ($^\circ$).

Leaf drainage is determined as:

$$LD = P_{\text{eff}} CC$$

(16)
Where $CC$ is the canopy cover (proportion between zero and unity). The canopy cover is either introduced by a landuse-class specific tabular value or determined by the vegetation module. When the vegetation module is used, the canopy cover is obtained from the LAI (Equation 9), maximized by 1.

Direct throughfall becomes:

$$ DT = P_{eff} - LD $$  \hspace{1cm} (17)

### 2.3.2 Detachment of soil particles

Detachment of soil particles is determined separately for raindrop impact and accumulated runoff and is subsequently summed.

The detachment of soil particles by raindrop impact ($F$, kg m$^{-2}$) and the detachment of soil particles by runoff ($H$, kg m$^{-2}$) are determined for each of the soil texture classes separately and subsequently summed. The detachment of soil particles by raindrop impact is calculated as:

$$ F_i = K_i \frac{\%i}{100} (1 - GC) KE \times 10^{-3} $$  \hspace{1cm} (18)

With $K$ the detachability of the soil by raindrop impact (g J$^{-1}$), $i$ the textural class, with $c$ for clay, $z$ for silt and $s$ for sand, and $GC$ the ground cover (-). The detachability of the soil for each texture class is included as a model parameter, for which Quansah (1982) proposed $K_c = 0.1$, $K_z = 0.5$ and $K_s = 0.3$ g J$^{-1}$. The ground cover, expressed as a proportion between zero and unity, protects the soil from detachment and is determined by the proportion of vegetation and rocks covering the surface. The ground cover is set to 1 in case the surface is covered with snow, which is determined in the hydrological model.

The detachment of soil particles by runoff ($H$, kg m$^{-2}$) is calculated as:

$$ H_i = D R_i \frac{\%i}{100} Q^{1.5} (1 - GC) \sin 0.3 S \times 10^{-3} $$  \hspace{1cm} (19)

Where $Q$ is the volume of accumulated runoff (mm) and $DR$ the detachability of the soil by runoff (g mm$^{-1}$) and $Q$ is the volume of accumulated runoff (mm). The detachability of the soil for each texture class is included as a model parameter for which Quansah (1982) proposed $DR_c = 1.0$, $DR_z = 1.6$ and $DR_s = 1.5$ g mm$^{-1}$.

### 2.3.3 Immediate deposition of detached particles

A proportion of the detached soil is deposited in the cell of its origin and is as a function of the abundance of vegetation and the surface roughness. The percentage of the detached sediment that is deposited ($DEP$) is estimated from the relationship obtained by Tollner et al. (1976) and calculated separately for each texture class:

$$ DEP_i = 44.1 N_{f_i}^{0.29} $$  \hspace{1cm} (20)

Where $N_f$ is the particle fall number (-), defined as:

$$ N_{f_i} = \frac{lv_{si}}{vd} $$  \hspace{1cm} (21)
Where $l$ is the length of a grid cell (m), $v_s$ the particle fall velocity (m s$^{-1}$), $v$ the flow velocity (m s$^{-1}$) and $d$ the depth of flow (m). Particle fall velocities are estimated from:

$$v_s = \frac{1}{18 \delta^2 (\rho_s - \rho) g}{\eta}$$  \hspace{1cm} (22)

Where $\delta$ is the diameter of the particle (m), $\rho_s$ the sediment density (= 2650 kg m$^{-3}$), $\rho$ the flow density (typically 1100 kg m$^{-3}$ for runoff on hillslopes; Abrahams et al., 2001), $g$ gravitational acceleration (taken as 9.81 m s$^{-2}$) and $\eta$ the fluid viscosity (nominally 0.001 kg m$^{-1}$ s$^{-1}$ but taken as 0.0015 to allow for the effects of the sediment in the flow; Morgan and Duzant, 2008). When Equation Eq. 22 is applied to the three texture sizes of 2 µm for clay, 60 µm for silt and 200 µm for sand, this gives respective values of 2 $10^{-6}$ m s$^{-1}$ for clay, 2 $10^{-3}$ m s$^{-1}$ for silt and 0.02 m s$^{-1}$ for sand.

The flow velocity $v$ from Equation Eq. 21 is obtained by the Manning formula:

$$v = \frac{1}{n'} d^{2/3} S^{1/2}$$  \hspace{1cm} (23)

Where $n'$ is the modified Manning’s roughness coefficient (s m$^{-1/3}$), which is a combination of the Manning’s roughness coefficient for the soil surface and vegetation, defined as (Petryk and Bosmajian, 1975):

$$n' = \sqrt{n^2_{soil} + n^2_{vegetation}}$$  \hspace{1cm} (24)

The Manning’s roughness coefficient for bare soil $n_{soil}$ is set to 0.015 s m$^{-1/3}$, as suggested by Morgan and Duzant (2008) (Figure Fig. 2a). For tilled conditions (Figure Fig. 2b) the following equation is applied:

$$n_{soil} = \exp(-2.1132 + 0.0349RFR)$$  \hspace{1cm} (25)

Where RFR is the surface roughness parameter (cm m$^{-1}$). Values for RFR are tillage implementation specific and can be obtained from Morgan and Duzant (2008, Table IV). Morgan and Duzant (2008, Table IV).

The Manning’s roughness coefficient for regular spaced vegetation (Figure Fig. 2c) $n_{vegetation}$ is obtained from the following equation (Jin et al., 2000):

$$n_{vegetation} = \frac{d^{2/3}}{\sqrt{\frac{2g}{DNV}}}$$  \hspace{1cm} (26)

Where $D$ is the stem diameter (m) and $NV$ the stem density (stems m$^{-2}$). Stem diameter and stem density may be difficult to obtain for certain landuse classes with irregular spaced vegetation (e.g. forest, shrubland), therefore, users may opt to use tabular values for $n_{vegetation}$, e.g. from Chow (1959) (Figure Fig. 2d). Equation Preliminary model runs showed that Eq. 26 results in unrealistically high flow velocity values for landuse classes where the stem density is very low, such as in orchards. Therefore, in these conditions where the influence of vegetation on flow velocity is negligible, $n_{vegetation}$ can be set to 0.

Equations 21, 23 and 26 require a flow depth $d$, a model parameter that can be used in the model calibration. The value for $d$ should be taken such that it corresponds to a water depth from runoff generated within the cell margins, i.e. without accumulation of flow from upstream located cells.
Figure 2. Surface and vegetation roughness options: (a) bare soil, (b) tilled soil (Eq. 25), (c) regular vegetation (Eq. 26), and (d) irregular vegetation.

2.3.4 Sediment deposition and transport

The amount of sediment that is routed to downstream cells is determined from the sum of the detached sediment from raindrop impact (Equation Eq. 18) and accumulated runoff (Equation Eq. 19), subtracting the proportion of the sediment that is deposited within the cell of its origin (Equation Eq. 20):

\[
g = (F_i + H_i)(1 - (DEP_i/100)) \tag{27}
\]

The amount of sediment that is routed to downstream cells is the summation of the individual amounts for clay, silt and sand.

Sediment is routed using a routing scheme that takes into account both the transport capacity \( TC; \) ton \( \text{ha}^{-1} \) of the accumulated runoff and the trapping efficiency of the reservoirs \( TE; \) -. The transport capacity \( TC \) (Figure Fig. 3a) of the accumulated runoff is based on Prosser and Rustomji (2000):

\[
TC = \text{flow}_{\text{factor}} q_{\text{surf}} \beta S^\gamma \tag{28}
\]

Where \( \text{flow}_{\text{factor}} \) is a spatially distributed roughness factor (-), \( q_{\text{surf}} \) accumulated runoff per unit width \( (m^2 \text{ day}^{-1}) \), \( S \) the local energy gradient \(^\circ\), approximated by the slope, and \( \beta \) and \( \gamma \) are model parameters (-). As suggested by Prosser and Rustomji (2000) \( \gamma = 1.4 \) and \( \beta \) is used for model calibration.

The roughness factor \( \text{flow}_{\text{factor}} \) is determined as follows:

\[
\text{flow}_{\text{factor}} = \frac{v_{\text{actual}}}{v_{\text{b}}} \tag{29}
\]
Where $v_{\text{actual}}$ is the actual flow velocity ($\text{m s}^{-1}$) and $v_{\text{bare}}$ is the flow velocity for bare soil conditions ($\text{m s}^{-1}$). The actual flow velocity $v_{\text{actual}}$ is obtained from Equations Eq. 23-26, applying a water depth $d_{\text{actual}}$ of 0.25 m, which coincides with deeper rills from Morgan and Duzant (2008). The flow velocity for bare soil conditions $v_{\text{bare}}$ is obtained from Equation Eq. 23, applying values for $n' = 0.015 \text{ s m}^{-1/3}$ and $d = 0.005 - d_{\text{bare}} = 0.005$ m (Morgan and Duzant, 2008).

Reservoir sediment trapping efficiency $TE$ (Figure Fig. 3b), the percentage of sediment trapped by the reservoir, is calculated according to Brown (1943):

$$TE = 100 \left[ 1 - \frac{1}{1 + 0.0021 D \frac{C}{A_{\text{basin}}}} \right]$$  (30)

Where $D$ is a constant (-) within the range 0.046-1, depending on the reservoir operation characteristics that we set at 0.1, $C$ the reservoir capacity ($\text{m}^3$), and $A_{\text{basin}}$ the drainage area of the subcatchment ($\text{km}^2$).

### 3 Model Application

To illustrate the model performance, its functionality and capacity for use in scenario studies, we applied the model to the Upper Segura River catchment (2,589 km$^2$) under present and future projected climate conditions. The Upper Segura catchment is located in the headwaters of the Segura River in southeastern Spain (Figure Fig. 4). The elevation ranges between 411 and 2055 m.a.s.l. (Figure Fig. 4). The climate in the catchment is classified as temperate (Cfa and Cfb according to the Köppen-Geiger climate classification, 80%) and semi-arid (BSk, 20%). The catchment-average annual precipitation is 570 mm (for the period 1981-2000) and the mean annual temperature is 13.2 $^\circ$C (1981-2000).

The main landuse types are forest (45%), shrubland (40%), cereal fields (7%) and almond orchards (4%) (Figure Fig. 4), based on a detailed landuse map MAPAMA (2010). Agriculture accounts for 14% of the catchment’s surface area. Huerta is defined as small-scale traditional vegetable and/or fruit orchards, which are common in the study area. The main soil classes are Leptosols (38%), Luvisols (27%), Cambisols (16%) and Calcisols (11%), based on
Figure 4. Location and characteristics of the Upper Segura River catchment: (a) location of the catchment within Europe, (b) the hydrological calibration area (orange), the channels (light blue), the reservoirs (dark blue), and the calibration reservoirs (red dots), (c) Digital Elevation Model (Farr et al., 2007), (d) landuse map (MAPAMA, 2010), and (e) soil texture map (Hengl et al., 2017).

The SoilGrids database Hengl et al. (2017). There are 5 reservoirs located in the catchment (Figure 4b) with a total capacity of 663 Hm$^3$, which are mainly used to store water for irrigation purposes.

3.1 Input Data

All input data were prepared at a 200 m grid size. Daily precipitation data were obtained from the SPREAD dataset Serrano-Notivoli et al. (2017), with a 5 km spatial resolution. Daily temperature data were obtained from the SPAIN02 dataset Herrera et al. (2016), with a 0.11° resolution. Precipitation and temperature data were subsequently interpolated on the model grid using bivariate interpolation (Akima, 1996). Soil textural fractions (sand, clay and silt) and soil
Table 1. Input parameters for the soil erosion model.

<table>
<thead>
<tr>
<th>landuse class</th>
<th>PH</th>
<th>NV</th>
<th>D</th>
<th>GC</th>
<th>manning</th>
<th>sowing</th>
<th>harvest</th>
<th>other^1</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(m)</td>
<td>(stems m^-2)</td>
<td>(m)</td>
<td>(-)</td>
<td>(s m^-1/3)</td>
<td>(doy)^2</td>
<td>(doy)^2</td>
<td></td>
</tr>
<tr>
<td>cereal (harvested)</td>
<td>0.75</td>
<td>500</td>
<td>0.025</td>
<td>0.31</td>
<td>n.a.</td>
<td>288</td>
<td>166</td>
<td>T</td>
</tr>
<tr>
<td>huerta (harvested)</td>
<td>0.5</td>
<td>500</td>
<td>0.01</td>
<td>0.6^*CC^0.5</td>
<td>n.a.</td>
<td>n.a.</td>
<td>n.a.</td>
<td>T</td>
</tr>
<tr>
<td>horticulture (harvested)</td>
<td>0.3</td>
<td>6.25</td>
<td>0.25</td>
<td>0.39</td>
<td>n.a.</td>
<td>288</td>
<td>166</td>
<td>T</td>
</tr>
<tr>
<td>tree crops</td>
<td>2</td>
<td>n.a.</td>
<td>n.a.</td>
<td>&lt;0.01</td>
<td>n.a.</td>
<td>n.a.</td>
<td>n.a.</td>
<td>T, N.V.</td>
</tr>
<tr>
<td>vineyard</td>
<td>1</td>
<td>n.a.</td>
<td>n.a.</td>
<td>0.02</td>
<td>n.a.</td>
<td>n.a.</td>
<td>n.a.</td>
<td>T, N.V.</td>
</tr>
<tr>
<td>forest</td>
<td>10</td>
<td>n.a.</td>
<td>n.a.</td>
<td>0.57^*CC^0.53</td>
<td>0.2^3</td>
<td>n.a.</td>
<td>n.a.</td>
<td></td>
</tr>
<tr>
<td>shrubland</td>
<td>0.5</td>
<td>n.a.</td>
<td>n.a.</td>
<td>0.8^*CC^0.45</td>
<td>0.1^3</td>
<td>n.a.</td>
<td>n.a.</td>
<td></td>
</tr>
<tr>
<td>water/urban</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>n.a.</td>
<td>n.a.</td>
<td>n.a.</td>
<td>N.E.</td>
</tr>
</tbody>
</table>

^1 T = tillage, N.E. = no erosion, N.V. = no vegetation, ^2 Day of the Year, ^3 Obtained from Chow (1959)

Organic matter content were obtained from the global SoilGrids dataset (Hengl et al., 2017) at 250 m resolution. The soil hydraulic properties (saturated hydraulic conductivity, saturated water content, field capacity, and wilting point) were obtained by applying pedotransfer functions (Saxton and Rawls, 2006). A Digital Elevation Model was obtained from the SRTM dataset (Farr et al., 2007) at 30 m resolution and was resampled to the model grid (Figure using bilinear interpolation (Fig. 4d). The spatially distributed rock fraction map was obtained by applying the empirical formulations from Poesen et al. (1998), which determines rock fraction based on slope gradient.

Both the hydrological and the soil erosion model require landuse-specific input. We used a detailed landuse map (MAPAMA, 2010) that identifies 25 landuse classes within the study area. Values for the landuse-specific tabular value of the depletion fraction \( p_{\text{tabular}} \) to calculate actual evapotranspiration were obtained from Allen et al. (1998) (Table 22). Values for the maximum LAI \( (LAI_{\text{max}}) \) were obtained from Sellers et al. (1996). The soil erosion model requires landuse-specific input for plant height \( (PH) \), stem density \( (NV) \), stem diameter \( (D) \), ground cover fraction \( (GC) \) and, optionally, the Manning’s roughness coefficient for vegetation \( (n_{\text{vegetation}}) \). The user needs to specify whether the landuse class is non-erodible (e.g. pavement and water), tilled and/or non-vegetated (e.g. bare soil or tilled orchards). We obtained values for each of these parameters through observations from aerial photographs, expert judgement and as part of the calibration procedure (Table 1).

The tillage parameter \( RFR \) was set to 6, which corresponds to Cultivator tillage from (Table IV; Morgan and Duzant, 2008) (Morgan and Duzant, 2008, Table IV). The input parameters change when a crop is harvested, therefore, we varied the input parameters according to the sowing-harvest cycle representing the cropping cycle for horticulture and cereals. Table 1 shows the values of all the landuse-specific input parameters after calibration.
We applied the dynamic vegetation module to obtain crop coefficients and vegetation cover from NDVI, which we obtained from the 16-day Moderate Resolution Imaging Spectroradiometer (MODIS; Didan, 2015) data for the period 2000-2012. For model calibration (2001-2010) we used each of the individual NDVI images, after gap-filling (mainly due to cloud cover) with the long-term average 16-day period NDVI for the period 2000-2012.

For the model validation period (1981-2000) no NDVI images of sufficient quality and resolution were available, therefore we prepared NDVI model input accounting for the intra- and inter-annual variability. The intra-annual variability was obtained from the long-term average 16-day period NDVI for the period 2000-2012. The inter-annual variability was determined based on a log-linear relationship between the annual precipitation sum, annual mean temperature, annual maximum temperature and yearly-averaged NDVI for each of the 25 landuse classes for the period 2000-2012:

\[
NDVI_{\text{year}} = \beta_0 + \log(P_{\text{year}})\beta_1 + \log(P_{\text{year}-1})\beta_2 + \log(Tav_{\text{avg, year}})\beta_3
\]
\[+ \log(Tav_{\text{avg, year-1}})\beta_4 + \log(Tm_{\text{ax, year}})\beta_5 + \log(Tm_{\text{ax, year-1}})\beta_6 \]

(31)

Where \( NDVI \) is the yearly-averaged NDVI, \( P \) the annual precipitation sum, \( Tav \) the annual mean temperature, \( Tm \) the annual maximum temperature, and \( \beta_0-6 \) coefficients of the log-linear model. We used the annual climate indices of two years, the current year and the previous year, to account for the climate lag that may influence the vegetation development. A stepwise model selection procedure was applied for each of the 25 landuse classes, selecting the best combination of variables from equation Eq. 31 with the lowest AIC (Akaike Information Criterion) in R (version 3.4.0), using the stepAIC algorithm from the MASS package (Venables and Ripley, 2002).

### 3.2 Model Calibration & validation

We calibrated the model for the period 2001-2010. To prevent overfitting and achieve most realistic model calibration we set most of the potential calibration parameters at literature values and maintained the other parameters within reasonable physical limits of the parameter domain. We used daily discharge time series from the Segura River Basin Agency (Confederación Hidrográfica del Segura) for the Fuensanta reservoir (Figure Fig. 4b) to determine model performance for the hydrological model. The calibration procedure consisted of two steps. First, we optimized the water balance by comparing the difference between the observed and simulated discharge sum at the Fuensanta discharge station. We adjusted the calibration parameter \( \lambda \) from equation 8-Eq. 6 to obtain a surface runoff ratio between 2-10%, which previous studies reported to be representative for catchments with similar conditions (Descroix et al., 2001; Mekki et al., 2006; Love et al., 2010; Reaney et al., 2014). We used parameters from the dynamic vegetation module and soil hydraulic properties to optimize the percent bias of the discharge difference in discharge sum (percent bias). In the second step, using the parameter set from the first step, we optimized the Nash-Sutcliffe model efficiency (NSE; Nash and Sutcliffe (1970)) (NSE; Nash and Sutcliffe, 1970) at the Fuensanta discharge station by calibrating the routing parameter (\( k_x \)). The calibration resulted in a Nash-Sutcliffe efficiency (NSE) of 0.47 for the daily discharge data, a NSE of 0.76 for the monthly discharge data and a percent bias of 2.3% 5a(Fig. 5a). Model validation for the period 1981-2000 resulted in a NSE of 0.25 for the daily discharge data, a NSE of 0.39 for the
Figure 5. Discharge time series for the calibration (a) and validation period (b). The solid line correspond to the observed time series and the dashed orange line corresponds to the simulated time series.

monthly discharge data and a percent bias of -18.7% 5b. These model efficiency values are similar to previous SPHY model applications (Terink et al., 2015).

To calibrate the soil erosion model we first optimized the detached material going into transport \( G \) for 8 landuse classes (aggregated from 25 landuse classes), based on literature data (Cerdan et al., 2010; Maetens et al., 2012) (Table 2). The resulting optimized parameter values are presented in Table 1. Next, we optimized percent bias in the prediction of sediment yield at the reservoirs using measured reservoir sediment yield data from 4 reservoirs (Avendaño-Salas et al., 1997) (see Figure 4b). Annual sediment yield at the reservoirs was determined from the measured reservoir volume on two moments in time and the measured bulk density. Figure 4b shows the locations of the reservoirs used for calibration. The calibration procedure focused on the most sensitive parameter from the sediment transport capacity equation (Eq. 28), i.e. the \( \beta \) parameter. We obtained a percent bias of 0.0% in the calibration and -19.8% in the validation (see Figure 4).

3.3 Results

Here we present a selection of model results to illustrate the main capabilities of the SPHY-MMF model. Soil erosion shows an important intra-annual variability due to seasonal changes in climate forcing and vegetation cover (Figure 7). For crops with little to no ground cover (i.e. tree crops and vineyard), soil erosion follows the precipitation sum, with high values in the winter, spring and autumn months and low values in the summer months. Some crops show a distinct peak in the vegetation
Table 2. Calibration and validation of hillslope soil erosion and comparison with literature data (Mg km$^{-2}$ yr$^{-1}$).

<table>
<thead>
<tr>
<th>landuse class</th>
<th>calibration</th>
<th>validation</th>
<th>Cerdan et al. (2010)</th>
<th>Maetens et al. (2012)</th>
</tr>
</thead>
<tbody>
<tr>
<td>cereals</td>
<td>99.8</td>
<td>99.2</td>
<td>84.0</td>
<td>120.0</td>
</tr>
<tr>
<td>huerta</td>
<td>112.0</td>
<td>112.6</td>
<td>84.0</td>
<td>120.0</td>
</tr>
<tr>
<td>horticulture</td>
<td>145.5</td>
<td>165.4</td>
<td>84.0</td>
<td>120.0</td>
</tr>
<tr>
<td>tree crops</td>
<td>249.9</td>
<td>236.4</td>
<td>167.0</td>
<td>740.0</td>
</tr>
<tr>
<td>vineyard</td>
<td>194.7</td>
<td>194.6</td>
<td>862.0</td>
<td>30.0</td>
</tr>
<tr>
<td>forest</td>
<td>17.2</td>
<td>13.5</td>
<td>18.0</td>
<td>10.0</td>
</tr>
<tr>
<td>shrubland</td>
<td>54.9</td>
<td>39.1</td>
<td>54.0</td>
<td>20.0</td>
</tr>
<tr>
<td>water/urban</td>
<td>0.0</td>
<td>0.0</td>
<td>n.a.</td>
<td>n.a.</td>
</tr>
</tbody>
</table>

Figure 6. Average yearly sediment yield at the reservoirs for the calibration (blue) and validation period (red).

devlopment in the spring (April-May), e.g. huerta and horticulture. While this period has a relatively high precipitation sum, soil erosion decreases as a consequence of the increased vegetation cover indicated by the NDVI in this period.

The temporal variation of the vegetation development of cereals and horticulture shows a slightly distinct pattern from the other landuse classes. Both *lines crops* show an increase in the spring months (March-May), which indicates the rapid growth of these crops. *While in these months. However*, during the summer months (June-August) the NDVI decreases, which coincides with the period when the crops are harvested, followed by the post-harvest period. In the latter period, we assume bare soil
Figure 7. Monthly precipitation sum (mm), NDVI (−) and soil erosion (Mg km$^{-2}$ yr$^{-1}$) per landuse class for the period 1981-2000. The gray area indicates the period when cereals and horticulture are harvested and model parameters are changed to simulate bare soil conditions. The dashed lines in the lower panel show the soil erosion of cereals and horticulture without considering bare soil conditions in this period under the sustainable land management scenario.

conditions for these crops. For both crops this ultimately results in the highest annual erosion rates in the post-harvest period (October).

To illustrate the models capacity to perform scenario studies we evaluated the impacts of the application of sustainable land management and the impacts of a future climate change scenario. First, to assess the impacts of sustainable land management, we evaluated the application of conservation agriculture by assuming that no bare soil conditions occur after harvest of cereals and horticulture for the period June-October (dashed lines in Figure 7). This is a sustainable land management scenario in cereal and horticulture fields. We assumed that after harvest the cereal and horticulture fields are not tilled until the next sowing. We parameterized this by setting the plant height to 0 and leaving all other input parameters unchanged, i.e. stem density, diameter and ground cover, which in the conventional scenario are set to 0, as well. This will affect immediate deposition of detached particles through Eq. 26. The sustainable land management scenario leads to lower soil erosion estimates for these two landuse classes (dashed lines in Fig. 7), as a result of an increase of immediate deposition of detached particles.

Next, we simulated the impacts of a projected climate change scenario, by comparing predicted soil erosion rates and sediment yield under the reference scenario (1981-2000) with a future scenario (2081-2100). We used a future emission scenario
from the Representative Concentration Pathways (RCP; van Vuuren et al., 2011) that describes a continuous increase of GHG emissions throughout the 21st century, i.e. RCP8.5. For this exercise we used projected climate data for RCP8.5 obtained from one Regional Climate Model (CLMcom MPI-ESM-LR) from the EURO-CORDEX initiative (Jacob et al., 2014), for the period 2081-2100. The climate forcing (precipitation and temperature) was bias-corrected using quantile mapping (Thiemens et al., 2012) and we applied the dynamic vegetation model (Equation 31) to construct future NDVI input based on future climate conditions. Figure 8 shows the precipitation and vegetation response under the reference and future scenarios. The annual precipitation sum decreases in the future scenario, with a catchment-averaged decrease of 128 mm. However, heavy precipitation, defined as the 95th percentile of daily precipitation, considering only rainy days (>1 mm day$^{-1}$; Jacob et al., 2014), increases by 27% on average in the catchment. The NDVI increases in the western part of the catchment due to increasing temperatures and decreases in the eastern part of the catchment due to a combination of decreasing precipitation and increasing temperatures.

In the reference scenario the highest specific sediment yield (SSY) is projected in the river network (Figure 9), where accumulated runoff causes an increase of soil erosion rates (Equation 19). In the future climate scenario, the catchment-median SSY increases from 43.3 to 55.2 Mg km$^{-2}$ yr$^{-1}$, an increase of 27.7%. This shows that the increase in heavy precipitation has a more pronounced impact on soil erosion than the decrease of annual precipitation sum. The increase of heavy precipitation both leads to an increase of detachment by raindrop impact (Equation 18) and an increase of detachment by runoff (Equation 19), as a consequence of an increase in surface runoff due to infiltration excess surface runoff. However,
as a result of the increased vegetation cover in the western part of the catchment SSY decreases, despite the increased extreme precipitation intensities (Figure 8).

Reservoir sediment yield (SY) decreases in all five reservoirs between 42.4-59.0% in the future climate scenario. While it is likely that a decrease of SSY in the western part of the catchment causes a decrease of reservoir SY, it is less obvious why in the eastern part of the catchment an increase in SSY is not reflected in an increase in reservoir SY. The explanation for this lies in the fact that a decrease in precipitation sum causes a decrease of accumulated runoff and, subsequently, a decrease of sediment transport capacity (Equation Eq. 28), increased sediment deposition and decreased reservoir SY.

4 Discussion

The SPHY-MMF model, based on integration of the SPHY hydrological model with the MMF soil erosion model, provides an important step forward to simulate the regional scale impacts of environmental change on soil erosion and sediment yield. The model runs at a daily time step, incorporates the main hydrological driving processes (i.e. saturation and infiltration excess surface runoff), accounts for the most relevant soil erosion processes (i.e. soil erosion by raindrop impact, soil erosion by accumulated runoff and sediment deposition) and incorporates a dynamic vegetation module that is linked to both the hydrological and the soil erosion model. This provides the model with processes included in the model provide the flexibility and accuracy needed to reflect the impacts of intra-annual changes in land use, land management and climate (Figure 7) and the inter-annual response of vegetation development and soil erosion to changes in climate forcing, including changes in precipitation sum and intensity (Figure 9).

Availability of high quality input data is an important constraint and model parameter values are important constraints for many process-based soil erosion models. Although SPHY-MMF requires a wide range of input data, most data were obtained from publicly available global datasets at relatively high spatial and temporal resolution. Although climate data are
Climate data may often be an important constraint. However, long-term, high-resolution, gridded daily climate forcing datasets are becoming increasingly more available at national (Silva et al., 2007; Yin et al., 2015; Berezowski et al., 2016; Kotlarski et al., 2017), (sub-)continental (Mitchell, 2004; Haylock et al., 2008; Yatagai et al., 2012; van den Bessel-Vlaar et al., 2017) and even at global scale (Poesen et al., 1996; Poesen, 2018). This results in the model also (Huffman et al., 2001; Donat et al., 2013; Schamm et al., 2016). Although, the model includes a large number of parameters (Table S1), we do not expect this to limit the model’s applicability. Apart from the landuse-specific parameters, all soil erosion model parameters were obtained from literature, mainly from Morgan and Duzant (2008). Although some parameters may be obtained from calibration, the possibility to use literature values facilitates model application. The model requires a detailed landuse map to account for landuse-specific model parameters. We that drive soil erosion processes (Table S1), which may be inevitable because soil erosion is inherently landuse dependent. For example, we obtained literature values for two model parameters, i.e. depletion fraction and the maximum LAI, while other model parameters—five landuse related model parameters (Table S1), while others—were obtained through observations from aerial photographs, expert judgement and as part of the calibration procedure. This may be inevitable because soil erosion is inherently landuse dependent and model assessments should involve the inclusion of detailed local data to get reliable results. However, most of the ground cover for cereals was obtained by adjusting the stem density, assuming a certain ground cover per stem. Most other input datasets are publicly available and most model parameters may be obtained from literature, which makes the model applicable for any environment.

The model results show that the highest One of the main limitations of the model is that unrealistic high soil erosion rates are projected where most flow accumulates (Figure Fig. 9). This is mainly due to the high amounts of soil erosion predicted by Equation Eq. 19 for large runoff volumes. Similar behaviour was reported in a daily implementation of the MMF model by (Shrestha and Jetten, 2018)Shrestha and Jetten (2018), who therefore suggested to exclude higher order streams from the soil erosion assessment. We correct for the high erosion rates in the river network by including both immediate sediment deposition (Equation Eq. 20) and deposition when the transport capacity is exceeded (Equation Eq. 28). While indeed different erosional processes dominate in channels and streams (i.e. bank erosion and channel incision), which are not captured by Equation Eq. 19, high soil erosion rates may be expected in the river network since many studies stress the large contribution of gully and channel erosion to total sediment yield due to large volumes of accumulated runoff (Poesen et al., 1996; Poesen, 2018) (Poesen et al., 1996; de Vente et al., 2008; Vanmaercke et al., 2011; Poesen, 2018). However, detachment and transport processes in channels are likely different from those on hillslopes and the bed material of rivers differs from the soil texture. While Equation as used in the model, While Eq. 19 makes a distinction between the three textural classes, it most likely overestimates the erosion in the higher order channels, where in reality the bed material consists of coarser material, such as coarse sand and gravel, which is currently not included in the model. Therefore, in a future update of the model, we suggest to include a separate channel erosion, transport and deposition model, which should be able model, to simulate the most relevant channel erosion, transport and deposition processes more accurately. Recently, several models have been proposed that incorporate fluvial processes into soil erosion models (Arnold et al., 2012; Wei et al., 2017) and landscape evolution models (Baartman et al., 2012; Coulthard et al., 2013), which could serve as a starting point for further model development.
The model is intended to be applied at regional scales and over decadal periods that are most relevant for policy makers. This poses some limitations to the spatial and temporal representation of some essential soil erosion processes. First of all, the spatial resolution of the model is bounded by the hydrological model. Each cell generates runoff, which is a composite of surface runoff, lateral flow and base flow (Figure 1b). Lateral flow and base flow are generally only generated at large spatial scales, imposing a lower limit for the spatial resolution. Therefore, Terink et al. (2015) suggests a spatial resolution in the range between 200 m to 1 km. The lower limit of the spatial resolution may affect simulation of soil erosion processes. For instance, the detachment of soil particles by runoff is determined by slope, among other variables. The lower limit of the spatial resolution may result in a flattening of the Digital Elevation Model, especially affecting steep slopes. Ultimately, this results in lower soil erosion projections on the most extreme slopes. Second, the daily time step limits the simulation of high-intensity (sub-)hourly rain storms, that often cause most soil erosion (Nearing et al., 1990). Therefore, we included a model parameter ($\alpha$) describing the relation between measured hourly and daily precipitation (see Eq. 8). Nevertheless, given the spatial scale at which the model is applied, running the model with (sub-)hourly time steps may still be infeasible for various reasons. At regional scales, (sub-)hourly precipitation data are often not available, while spatial interpolation of (sub-)hourly precipitation data may introduce large uncertainties, jeopardizing the model outcome. Also, climate change assessments would become challenging, since most future climate model output is only available in daily time steps.

5 Conclusions

We have presented a new coupled hydrology, soil erosion and sediment yield prediction model (SPHY-MMF), and its application to the Upper Segura catchment for different climate and land management scenarios. The model is an integration of the MMF soil erosion model in the SPHY hydrological model and simulates most relevant hydrological and soil erosion processes at a daily time-step. The model considers soil detachment by raindrop and runoff, uses dynamic vegetation to simulate changes in the canopy cover, simulates saturation excess and infiltration excess surface runoff, simulates soil deposition in the cell of its origin and routes the sediment through the river network, considering the transport capacity of the flow. The model was successfully applied in a large catchment in southeastern Spain. We have shown that the model is capable of performing scenario assessments of changes in climate and land management. Furthermore, our results show that the model simulates the soil erosion response to intra-annual variability in climate conditions and vegetation development. While there remain multiple challenges to accurately simulating the impacts of environmental change on soil erosion and sediment yield, we consider the integrated SPHY-MMF model an important step forward to facilitate catchment scale scenario studies.

Code availability. The model source code is available online: https://github.com/JorisEekhout/SPHY/tree/SPHY2.1-MMF.

Competing interests. The author declares that they have no conflict of interest.
Acknowledgements. We acknowledge financial support from the "Juan de la Cierva" program of the Spanish Ministerio de Economía y Competitividad (FJCI-2016-28905), the Spanish Ministerio de Economía y Competitividad (ADAPT project; CGL2013-42009-R) and the Séneca foundation of the regional government of Murcia (CAMBIO project; 118933/JLI/13). The authors thank AEMET and UC for the data provided for this work (Spain02 v5 dataset, available at http://www.meteo.unican.es/datasets/spain02).
References


Table S1. Input parameters for the model. Parameter determination indicates if the parameter can be obtained from literature (L), is measurable (M) or should be obtained from calibration (C). The bold characters indicate how the parameter values were obtained in the model application.

<table>
<thead>
<tr>
<th>description</th>
<th>symbol</th>
<th>unit</th>
<th>equation</th>
<th>landuse-specific</th>
<th>parameter determination</th>
<th>reference</th>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>depletion fraction</td>
<td>( p_{\text{tabular}} )</td>
<td>-</td>
<td>4</td>
<td>( \times )</td>
<td>L</td>
<td>Allen et al. (1998, Table 22)</td>
</tr>
<tr>
<td>crop coefficient open-water evaporation</td>
<td>( k_{\text{open-water}} )</td>
<td>-</td>
<td>5</td>
<td></td>
<td>L/C</td>
<td>Allen et al. (1998)</td>
</tr>
<tr>
<td>calibration parameter infiltration rate</td>
<td>( \lambda )</td>
<td>-</td>
<td>6</td>
<td></td>
<td>C</td>
<td></td>
</tr>
<tr>
<td>fraction of daily rainfall</td>
<td>( \alpha )</td>
<td>-</td>
<td>8</td>
<td></td>
<td>M/C</td>
<td>Sellers et al. (1996)</td>
</tr>
<tr>
<td>maximum LAI</td>
<td>( LAI_{\text{max}} )</td>
<td>-</td>
<td>9</td>
<td>( \times )</td>
<td>L</td>
<td></td>
</tr>
<tr>
<td><strong>soil erosion model</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>plant height</td>
<td>( PH )</td>
<td>m</td>
<td>13</td>
<td></td>
<td>L/M/C</td>
<td></td>
</tr>
<tr>
<td>intensity of erosive precipitation</td>
<td>( I )</td>
<td>mm h(^{-1})</td>
<td>14</td>
<td></td>
<td>L/C</td>
<td>Morgan and Duzant (2008)</td>
</tr>
<tr>
<td>canopy cover(^1)</td>
<td>( CC )</td>
<td>-</td>
<td>16</td>
<td>( \times )</td>
<td>M/C</td>
<td></td>
</tr>
<tr>
<td>detachability by raindrop impact</td>
<td>( K )</td>
<td>g J(^{-1})</td>
<td>18</td>
<td></td>
<td>L/M/C</td>
<td>Quansah (1982)</td>
</tr>
<tr>
<td>detachability by runoff</td>
<td>( DR )</td>
<td>g mm(^{-1})</td>
<td>19</td>
<td></td>
<td>L/M/C</td>
<td>Quansah (1982)</td>
</tr>
<tr>
<td>ground cover</td>
<td>( GC )</td>
<td>-</td>
<td>18, 19</td>
<td>( \times )</td>
<td>M/C</td>
<td></td>
</tr>
<tr>
<td>water depth</td>
<td>( d )</td>
<td>m</td>
<td>21, 23, 26</td>
<td></td>
<td></td>
<td>Morgan and Duzant (2008)</td>
</tr>
<tr>
<td>sediment density</td>
<td>( \rho_s )</td>
<td>kg m(^{-3})</td>
<td>22</td>
<td></td>
<td>L/M</td>
<td>Morgan and Duzant (2008)</td>
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<tr>
<td>flow density</td>
<td>( \rho )</td>
<td>kg m(^{-3})</td>
<td>22</td>
<td></td>
<td>L/M</td>
<td>Morgan and Duzant (2008)</td>
</tr>
<tr>
<td>fluid viscoscity</td>
<td>( \eta )</td>
<td>kg m(^{-1}) s(^{-1})</td>
<td>22</td>
<td></td>
<td>L/M</td>
<td>Morgan and Duzant (2008)</td>
</tr>
<tr>
<td>diameter of soil particles</td>
<td>( \delta )</td>
<td>m</td>
<td>22</td>
<td></td>
<td>L/M</td>
<td>Morgan and Duzant (2008)</td>
</tr>
<tr>
<td>Manning’s roughness bare soil</td>
<td>( n_{\text{soil}} )</td>
<td>s m(^{-1/3})</td>
<td>24</td>
<td></td>
<td>L/C</td>
<td>Morgan and Duzant (2008)</td>
</tr>
<tr>
<td>Manning’s roughness vegetation</td>
<td>( n_{\text{vegetation}} )</td>
<td>s m(^{-1/3})</td>
<td>24</td>
<td>( \times )</td>
<td>L/C</td>
<td>Chow (1959)</td>
</tr>
<tr>
<td>surface roughness for tilled soil</td>
<td>( RFR )</td>
<td>cm m(^{-1})</td>
<td>25</td>
<td></td>
<td>L/C</td>
<td>Morgan and Duzant (2008)</td>
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<tr>
<td>stem diameter</td>
<td>( D )</td>
<td>m</td>
<td>26</td>
<td>( \times )</td>
<td>L/M/C</td>
<td></td>
</tr>
<tr>
<td>stem density</td>
<td>( NV )</td>
<td>stems m(^{-2})</td>
<td>26</td>
<td>( \times )</td>
<td>M/C</td>
<td></td>
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<td></td>
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<tr>
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<td>-</td>
<td>28</td>
<td></td>
<td>L/C</td>
<td>Prosser and Rustomji (2000)</td>
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<tr>
<td>parameter transport capacity 2</td>
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<td>-</td>
<td>28</td>
<td></td>
<td>L/C</td>
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<td>water depth bare soil</td>
<td>( d_{\text{bare}} )</td>
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<td>29</td>
<td></td>
<td>L/C</td>
<td>Morgan and Duzant (2008)</td>
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<tr>
<td>water depth transport capacity</td>
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<td>29</td>
<td></td>
<td>L/C</td>
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<tr>
<td>trapping efficiency constant</td>
<td>( D )</td>
<td>-</td>
<td>30</td>
<td></td>
<td>L/C</td>
<td>Brown (1943)</td>
</tr>
</tbody>
</table>

\(^1\) can be obtained from NDVI

References


