Dear Editor

Many thanks for handling our paper and for contacting several reviewers, who came back with critical, though constructive and helpful comments. We greatly acknowledge the feedbacks and suggestions of an additional comment, which we have fully considered upon revising our article. Many thanks for these contributions!

Outline of how we have addressed the major points raised by the reviewers
The reviewers centered their critiques and concerns on three closely related issues, which we have not considered with the required care upon writing our first version of this manuscript. We addressed these points and thus took the opportunity to complement our manuscript with additional information to better constrain our inferences. The major points concern (i) the differences between threshold conditions for floods resulting in either an alteration of the channel architecture (channel forming floods) or in the incipient motion of individual clasts (A. Wickert); (ii) the importance of protrusion effects on the entrainment of large clasts and the consequences on the Shields variable $\phi$ (A. Wickert; R. Hodges), and (iii) mismatches between experimental results and our inferences (P. Carling, R. Hodges, McLelland). We have addressed these points in three new individual chapters in the manuscript. There, we shortly summarize the related state of research, and we outline where these points contradict our conclusions, and how. We then have adjusted our inferences and interpretations accordingly.

As a major outcome of our revision, we specified the conditions under which imbrications possibly record the occurrence of supercritical flows. In particular, we find that imbrications possibly record supercritical flows provided that (i) $\phi$-values are larger than c. 0.05, which might be appropriate for streams in the Swiss Alps; (ii) average stream gradients exceed c. 0.5±0.1°; and that (iii) relative bed roughness values, i.e. the ratio between the water depth $d$ and the $D_{94}$, are larger than $\sim$0.06±0.01. While we cannot rule out that imbrication may be formed during subcritical flows with $\phi$–values as low as 0.03, as a large number of flume experiments reveal, our results from Alpine streams suggest that clast imbrications are likely recorders of upper flow regime conditions, provided that the clasts form well-sorted and densely packed clusters. We consider that these differences may be rooted in a misfit between the observational and experimental scales. (please see lines in the revised manuscript 24-33).

As a consequence, we changed the title to Clast imbrications in coarse-grained mountainous streams and stratigraphic archives possibly suggest deposition under upper flow regime conditions.

Please find below a summary of how we have addressed the major points (i) to (iii).

Differences between thresholds for sediment transport during channel forming floods and during the incipient motion of individual clasts
We have discussed this point in a separate section, where we outlined (i) why this distinction will not change our major conclusions, and (ii) why the consideration of the incipient motion of individual clasts is a more appropriate approach for the understanding of imbrication formation. We mention that our calculations are based on the incipient motion of individual clasts, which we use as justification for selection of equation (1a) for all other considerations. This approach might be perceived as a large contrast to the hydrological conditions during channel forming floods where thresholds for the evacuation of sediment are up to 1.2 times larger, as theoretical and field-based analyses and have shown (Parker, 1978; Philips and Jerolmack, 2016; Pfeiffer et al., 2017). Nevertheless, the consequences on the outcome of our calculations are minor, at least when the Froude number dependencies on the slope and bed roughness parameters are considered. In fact, a 1.2-times larger threshold will increase the $\phi$–values (equation 1b) to the range between
0.036 and 0.072. However, as illustrated in Figure 3, this will not change the general pattern. In addition, while channel forming floods are mainly associated with equal mobility of a large range of sediment particles, the formation of an imbricated fabric involves the clustering of individual clasts only. We use these arguments to justify our preference for using equation 1a (incipient motion of clasts) rather than equation 1b (channel forming floods) (please see lines 488-500).

The importance of protrusion effects on the entrainment of large clasts, and the consequences on the Shields variable $\phi$

This is a major point, because the consequence of protrusion effects is a lowering of the Shields variable $\phi$ to a value as low as 0.03, with the result that supercritical conditions will not establish. We made a major effort to argue why protrusion effects are likely not to reduce the thresholds and thus the $\phi$-values, at least for the mountainous streams we have encountered in the Swiss Alps. We included the following text in our revised manuscript:

Larger bed surface grains, as is the case for most of the imbricated clasts, may exert lower mobility thresholds because of a greater protrusion and a smaller intergranular friction angle, as noted by Buffington and Montgomery (1997) in their review. Related consequences have been explored in experiments (e.g., Buffington et al., 1992) and through field-based studies, which were likewise complemented with experiments in the laboratory (Johnston et al., 1998). These studies resulted in the notion that the entrainment of the largest clasts (e.g., the $D_{84}$) most likely requires lower flow strengths than the shift of median-sized sediment particles. As a consequence, while $\phi$-values might be as high as 0.1 for the displacement of the $D_{50}$ (Buffington et al., 1992), conditions for the incipient dislocation of large clasts could be significantly different. In particular, for clasts that are up to five times larger than the $D_{50}$ (which corresponds to the ratio between the $D_{84}$ and the $D_{50}$ of the Swiss data, Table 1), Buffington et al (1992) and also Johnston et al. (1998) predicted $\phi$-values that might be as low as 0.03 or even less. Related $\phi$-values, for instance, have indeed been applied for mountainous streams where the supply of sediment from the lateral hillslopes has been large (van der Berg and Schlunegger, 2012). Large sediment fluxes have been considered to result in a poor sorting and a low packing of the material, and thus in low thresholds particularly for the incipient motion of large clast (Lenzi et al., 2006; van der Berg and Schlunegger, 2012). Our calculations predict that an upper flow regime is very unlikely to establish at these conditions ($\phi$-value of 0.03). However, we consider it unlikely that the formation of most of the imbrications, as we did encounter in the analyzed Alpine streams and in the stratigraphic record, were associated with thresholds as low as those proposed by e.g., Lenzi et al. (2006) and van der Berg and Schlunegger (2012). We base our inference on the observation that the analyzed gravel bars display an arrangement where large clasts are generally well sorted and densely packed, both on subaerial (during low water stages) and subaquatic bars. This results in a high interlocking degree of sediment particles within the bars we have encountered in the field. In addition, field inspections showed that the base of most of the large clasts, particularly those in subaqueous bars, are embedded and thus buried in finer grained material, and only very few clasts are lying isolated and flat on their a-b-planes. This implies that the fine-grained sediment particles have to be removed before these clasts can be entrained. In this case, hiding effects associated with $\phi$-values >0.5 would possibly be appropriate for the prediction of material entrainment of the finer-grained sediments before the larger clasts can be shifted (Buffington and Montgomery, 1997). As a consequence, a dislocation of these clasts and thus a rearrangement of the sedimentary fabric most likely require that large thresholds have to be exceeded, which is mainly accomplished through high-discharge events with large flow strengths. We thus propose that the use of $\phi$-values of c. 0.05, which is commonly used for the entrainment of the $D_{50}$ (Paola and Mohring, 1996), is also adequate for the calculation of the hydrological conditions associated with the fabric we have encountered in the field. We do acknowledge, however, that this hypothesis warrants a test with quantitative data, which we have not available. Please note that the low Froude numbers and thus the low $\phi$-values of 0.3 inferred for the Thur and the Birse streams might be underestimated,
because photos that were taken during high stage flows of these streams display clear evidence for multiple hydraulic jumps over m-long reaches (Spreafico et al., 2001, p. 71 and 77) (Lines 50-56)

**Mismatches between experimental results and our inferences**

A major concern of various reviewers addresses the differences in the conclusions between our work and the results derived from experiments. These reproduce imbrications under steady and lower flow regime conditions either through rolling, sliding, or tilting in response to differential winnowing of the fine-grained material. The result is the formation of channel bed armors. Contrariwise, we suggest that imbrications, particularly of coarse-grained cluster bedforms, record high stage and most likely supercritical floods. Our inference critically depends on the assignment of $\phi$-values for the mobilization of clasts. While experimental results suggest that $\phi$-values as low as 0.03 (and lower) appear as suitable conditions for the shift of clasts in experiments, we suggest that these thresholds are possibly too low to explain the mobilization of the coarse-grained fraction of the material in our streams. We base our inference on the observation that the coarse-grained material in subaquatic and subaerial bars correspond to bedforms of well-clustered and armored arrangements of clasts. Most important, we consider the mismatch in scales as the major difficulty for comparing laboratory experiments with our natural examples. We devoted a full new section to outline our inferences. The following text is a copy of a new section 4.3 entitled *The formation of imbrications in experiments* where we discuss these points: Interpretations of the possible linkages between hydrological conditions upon material transport and the formation of imbrications are hampered because experiments have not been designed to explicitly explore these relationships. In addition, as noted by Carling et al. (1992), natural systems differ from the conditions in experiments because of the contrasts in scales. Despite these limitations, it was possible to reproduce the formation of clast imbrications in subcritical flumes (Carling et al., 1992), or at least in the absence of any change in flow regime in many experiments. For instance, Qin et al. (2013) quantified the imbrications that resulted from the experiments by Aberle and Nikora (2006) where flows have been stationary. Carling et al. (1992) additionally showed that the shape of a clast has a strong control on the thresholds for incipient motion, the style of motion, and the degree of imbrication. A similar arrangement of clasts was formed in the experiments by Powell et al. (2016) and Bertin and Friedrich (2018), who reproduced imbrications with low Froude numbers between c. 0.55 and 0.9. Powell et al. (2016) additionally showed that the material can be entrained with $\phi$-values as low as 0.03, which is consistent with calculations of Froude numbers for some of the streams in Switzerland. Also during experiments, Johansson (1963) reported particle vibration before entrainment either through rolling or sliding. He noted that imbrication was formed at conditions, which corresponded to the lower flow regime during the flume experiments. Finally, based on field observations, Sengupta (1966) reported examples where imbrication was most likely initiated by the development of current crescents around pebbles that were embedded in sand, and that these processes possibly occurred during lower regime flows. Such eddies preferentially develop at the upstream end of pebbles, which then leads to winnowing of the fine-grained sand at the upstream edge and the tilting of this particular clast. Additional sliding, pivoting and vibrating of these sediment particles might then result in the final imbrication. If this process occurs multiple times and affects the sand-gravel interface at various sites, then an armored bed with imbricated clasts can establish without the necessity of supercritical flows, changes in flow regimes, as experimental results have shown (Aberle and Nikora, 2006; Haynes and Pender, 2007). They may even form in response to prolonged periods of sub-threshold flows, as summarized by Ockelford and Haynes (2013).

However, inspections of photos illustrating the experimental set up reveal that the surface grains are either flat lying on finer-grained sediments before their entrainment (Figure 3 in Powell et al., 2016), occur isolated on the ground (Figure 2.1b in Carling et al., 1992), or have a low degree of interlocking (Figure 3a in Lamb et al., 2017). Interestingly, the experiment by Buffington et al. (1992) followed a different strategy, where a natural bed-
surface of a stream was peeled off with epoxy. They subsequently used this peel in the laboratory to approximate a natural channel bed surface (see their Figure 4), on top of which they randomly placed grains with a known size distribution. Buffington and co-authors then measured the friction angle of the overlying grains, based on which they calculated the critical boundary shear stress values $\phi$. In all experiments, the surface morphology of the sedimentary material is flat and lacks topographic variations, which we found as reach-scale alternations of riffles, transverse bars and pools in the field. The low $\phi$-values of 0.03, which appears to be typical of bed surface conditions that develop in laboratory flumes (Ferguson, 2012), as summarized by Powell et al. (2016), could possibly be explained by these limitations. Furthermore, and probably more relevant, the lengths of the experimental reaches are generally less and range between e.g., 4.4 meters (Powell et al., 2016), 15 meters (e.g., Lamb et al., 2017) and even 20 meters (Aberle and Nikora, 2006). We acknowledge that in most experiments the variables have been normalized through a constant Reynolds number. This normalization also includes the experimental $D_{50}$-grain sizes, which are very similar to those we have determined for our selected streams (Litty and Schlunegger, 2017). Nevertheless, we find it really hard to upscale some of the results associated with these experiments to our natural cases where standing waves of 1 m, and even between 5 and 8 meters lengths may occur (our Figures 1B, 5B, 6B), which are not reproducible in the experiments. In addition, Powell et al. (2016) observed that the water surface stayed relatively stable during their experiments, and that the flows were steady and uniform without hydraulic jumps. This contrasts to our natural cases where upper and lower flow regimes alternate over short distances even during low-stage flows. Finally, while winnowing of fine grained material, tilting of clasts and subsequent bed armoring might be a valuable mechanism for the explanation of imbrications during low stage flows in experiments, we consider it unlikely that these results can be directly translated to our field observations. We base our inference on two closely related arguments. First, our reported groups of imbricated clasts tend to be arranged as cluster bedforms (e.g., Figures 6D, 7B), which rather form in response to selective deposition of large clasts than selective entrainment of fine-grained material (Figure 6A). Second, observations (Berther, 2012) and calculations (Litty and Schlunegger, 2017) have shown that effective sediment transport in these streams is likely to occur on decadal time scales (and most likely much shorter; van der Berg and Schlunegger, 2012), at least for subaquatic bars. Sediment transport is then likely to occur over a limited reach only. This means that a large fraction of the shifted material per flood has a local source situated in the same river some hundreds of meters farther upstream where bars are also well armored, thus requiring large thresholds for the removal of clasts. In addition, on subaerial bars, waning stages of floods result in the deposition of fine-grained material and not in the winnowing of sand, as our observations have shown. Accordingly, while low $\phi$-values and thus a lower flow regime might be appropriate for predicting the entrainment of the sediment particles in experiments, greater thresholds and thus larger $\phi$-values are likely to be appropriate for our natural examples for the reasons we have explained in above. (Lines 588-668)

Based on these arguments, we came to the conclusion that clast imbrications are likely to be associated with supercritical flows provided that (i) channel gradients are steeper than c. 0.5°±0.1°, and (ii) large clasts are tightly packed, closely arranged as cluster bedforms and partly embedded in finer-grained sediment, yielding in thresholds that are large enough ($\phi$-values >0.05) to allow supercritical conditions to occur. As mentioned further above, we thus have modified the title and adjusted the abstract accordingly.

Specific points raised by reviewer Wickert
Reviewer’s comment:
12. What does "presumably" mean here?

Our response:
The text has been specified.
Reviewer’s comment:
19. What kind of "bed roughness values" are these? Please also note units, if needed.

Our response:
This has been specified.

Reviewer’s comment:
43. considered to record

Our response:
Corrected.

Reviewer’s comment:
62. justifications → justification

Our response:
Corrected

Reviewer’s comment:
92. More precisely, the shear stress exerted by the fluid on the bed (shear stress is not an intrinsic property of the fluid)
93. inertial force

Our response:
Both have been corrected.

Reviewer’s comment:
95. You include “x” as a subscript of D in the denominator but not in the numerator. Please be consistent. (Also, i is typically chosen for size classes, if this is the intent of including it, as it seems to be.)
96. gravitational acceleration

Our response:
Both have been corrected.

Reviewer’s comment:
99-101. You are mixing the use of φ as the Shields stress (any applied stress, but made clarify here; I think you want the latter definition.

Our response:
Yes indeed; this has been corrected.

Reviewer’s comment:
103-106. I think that you will need a reference for this claim, and it may be good to discuss which grain sizes will be more likely or less likely to be entrained, as this becomes important in heterogeneous mixtures.

Our response:
This has been done.

Reviewer’s comment:
107-108. Lamb et al. (2008) compile the relevant data from that time.

Our response:
We have added this reference.
Reviewer’s comment:
112. 84th percentile; D84 is the size class at that percentile
Our response:
This has been specified.

Reviewer’s comments:
120. Wong and Parker (2006) noted an error in M-P M’s original analysis and suggest a value of 0.0495 for critical Shields stress. (In fact, they suggest two values, with the one that I am writing being for maintaining the 3/2 relationship with transport.
Our response:
We are grateful for this note and have used the updated φ-value of 0.0495≈0.05 instead.

Reviewer’s comments:
122. A channel-forming flood must exceed the threshold of motion, and this equation therefore cannot be correct. For many rivers, the Parker (1978) criterion of channel-forming discharge at approximately 1.2 times critical holds. See Phillips and Jerolmack (2016) and Pfeiffer et al. (2017) for a more recent discussion. This and the previous comment must be propagated through the paper.
Our response:
We have addressed this point in a separate section. Please see also our general statement of how we have modified the manuscript.

Reviewer’s comments:
Furthermore, the MPM relationship that you invoke here is designed for only one size class of gravel that comprises the river. This may be appropriate in some cases for the but does not include the extra boost of mobility given to large grains as a result of protruding from a finer-grained bed. This “hiding factor” is important. It will reduce the effective Shields coefficient (phi), and I expect that not including it will cause your Froude number estimates to be anomalously high.
Our response:
We have addressed the issue about hiding and protrusion effects in a separate chapter, as we agree that this has major implications and warrants a careful discussion. Please see our response to the general concerns further above.

Reviewer’s comments:
Finally, you are missing a g in this equation. I have checked and you do not seem to propagate this error, so it is probably just a local typo.
126-129. Your reason for this relationship working is about the hydraulic radius, but the other important piece is the steady, uniform flow assumption.
Our response:
We have addressed both points in the revised manuscript.

Reviewer’s comments:
134. 1 “s” in Weisbach
153-155. Manning’s n is a function of grain size; see Gary Parker’s work (Parker, 1991) or his e-book. This is also cited (perhaps more conveniently) by Wickert and Schildgen (2018, Eq. 13); you can rearrange this equation to solve for Manning’s n.
178-179. Yes! At incipient motion. I suggest that you use this wording instead of “channel-forming” unless/until you are discussing floods that move significant sediment and reshape the channel.
212. calculation of (instead of “to calculate”) 213-214. Do you mean that backwater effects become important?
224-226. Is this a qualitative description of the hiding factor? If so, it would be nice to see estimates better quantified, as the Froude number of the depositional conditions is key to your conclusions.

230. It could be good to note that your “roughness” is Darcy-Weisbach friction factor, to be unambiguous.

Our response:
We have addressed all points addressed above either through specifications in the text, or through editorial improvements and typo corrections.

Reviewer's comment:
238-241. This may be true, but I am calling this into question on the basis of your using the D84

Our response:
This addresses the issue about hiding and protrusion effects, which we have fully discussed in a separate chapter. Please see our answer above.

Reviewer's comment:
242-250. See Lamb (2008) and update this paragraph; I do not think the Shields parameter increase will be as extreme as the Mueller study alone shows.

Our response:
Yes indeed. We have adjusted the text accordingly.

Reviewer's comments:
263. Artificial river banks can fundamentally alter the flow hydraulics and the self-regulation of channel width. This artificial narrowing can increase flow velocities and alter the Froude number. Do you know that your knowledge of the hydrograph, the bed shear stress, and the age of the imbrications are all consistent with being from either before or after the modifications were made?

Our response:
The values we used and related time scales are all consistent with the chronology of anthropogenic corrections. We have made this point in the revised manuscript.

Reviewer's comments:
320-321. I do not see how a floodplain would confine a gravel-bed river, especially on an aggrading alluvial fan. Could you please explain or change this statement?

349. A general comment on the data section: your focus in the writing is more on the non-imbricated sediments in the geological record and the imbricated sediments in the modern rivers. I think it is important to make clear to the readers that you have both conditions from both environments at the very start.

Our response:
We have clarified the first question and taken into consideration the second point.

Reviewer's comments:
432-434. These are the forces driving particle motion, but weight also operates on the particle.
439. Could you use the long axes of the particle in this equation as the lever arm? You have measured them, it appears.
467. Are flow velocities really higher on steeper slopes? Or do roughness and shallower overall flow decrease the velocity proportionately?
471. My reading of the Lamb et al. (2008) study was that it included a significant data-driven component, which has a large compilation; my impression is that you are not taking
into account this compilation and instead prefer the field measurements from Mueller (2005). This choice needs justification.

Our response:
We are grateful for the acknowledgement of our usage of the English. We addressed all additional points in the sense that specifications have been added in the text.

**Specific points raised by reviewer R. Hodges**

Reviewer’s comment:
Having read the previous two reviews, I agree with the points that they raise. I’ve also looked at the authors’ responses. However, I’m still unconvinced by the argument that imbricated fabrics only form under super-critical flows, and less convinced that strong imbrication will only occur at the specific location of the transition between sub- and super-critical regimes. I agree with Carling that it is not clear from the paper whether you are claiming that imbrication occurs when Fr > 1, or only at the locations where flow is transitioning at a hydraulic jump. If it is the latter case, then how do you reconcile the widespread occurrence of imbrication across bars with the limited spatial extent of hydraulic jumps? Could you predict the spatial occurrence of hydraulic jumps and see whether that matched the spatial occurrence of imbrication?

Our response:
We suggest that imbrication occurs when Fr > 1. Clusters of imbricated clasts might then result in hydraulic jumps, as is particularly observed during low water stages. We have clarified this issue in the revised version of our manuscript.

Reviewer’s comment:
There are some flume studies that are relevant to your work which demonstrate imbricated fabrics forming in subcritical flows. Burtin and Friedrich (2018) demonstrate imbrication in flows with Fr = 0.54 and 0.55 (calculated from their Table 2). Powell et al (2016) demonstrate imbrication in flows with Fr ≈ 0.60 to ≈ 0.94, with the amount of imbrication not varying with Fr. (Fr is calculated using their stated slopes, depth and roughness ratio, and your equations 6 and 8). Are these data consistent with your argument?

Our response:
We have discussed this issue in a separate section in the discussion (new section labelled “The formation of imbrications in experiments”). Please see our explanations above.

Reviewer’s comment:
I think that Figure 3 could be clearer, and is potentially misleading. Panels A/B and C/D show different things; Fr values in A/B and imbrication in C/D. By using the same colour scheme across all panels you are equating imbrication with Fr > 1, but it’s hard to tell whether the data support this. I can see that as slope increases, Fr is likely to be > 1 and more imbrication is observed. The pattern with bed roughness is less clear. In B Fr > 1 is most likely at intermediate roughness, however the imbrication all occurs at high roughness. The sites with no imbrication occur at the sort of roughness values that correspond to the highest Fr values; therefore the two patterns don’t look similar to me. Why not calculate the Fr values for entrainment of D84 in the field and rock deposits, and see whether you get a consistent pattern between the Fr value and whether imbrication is observed?
Our response:
We have separated the two figures and changed the colours in order to avoid this confusion. We have not specifically calculated the F-values for the field data mainly because this will heavily depend on channel slope and the bed roughness values, and particularly on the $\phi$-values. However, we modified the discussion to make the linkage between field-based observations and modelling results more transparent and clearer. Please see lines 640-692 of our revised manuscript.

Reviewer’s comment:
I would have liked to see some attempt to quantify the amount of imbrication that is observed in the field and rocks. In your response to Carling you refer to shallow and strongly dipping grains, and suggest that the former might form under sub-critical flows. If this is the case, then your argument is not as simple as imbrication equals super-critical flows. You would need a more robust method to quantify the amount of imbrication, and a dataset to determine the relationship between imbrication amount and flow regime.

Our response:
Unfortunately, we don’t have quantitative data to properly constrain these observations. We therefore frame our hypothesis around other arguments. We provide evidence from the field, documenting that sites with imbrications are also the reaches where we observed supercritical flows during high stages. Please see lines 665-677 of the revised manuscript.

Reviewer’s comment:
As with Carling, I’m also unconvinced by the argument that grain rolling is necessary for imbrication to occur. I would have thought it possible for a grain to be entrained by sliding, and to slide or flip into an imbricated position on deposition. There is also evidence that beds can undergo some restructuring at sub-critical flows, which has potential to include imbrication.

Our response:
We agree and we have removed this section.

Reviewer’s comment:
19: I’m not convinced that this description of a threshold is consistent with Fig 3 and later parts of the paper, in which you describe Fr values decreasing again at high slopes and roughness values.

Our response:
Our results reveal that imbrications possibly record supercritical flows provided that (i) $\phi$-values are larger than c. 0.05, which might be appropriate for streams in the Swiss Alps; (ii) average stream gradients exceed c. 0.5±0.1°; and that (iii) relative bed roughness values, i.e. the ratio between the water depth $d$ and the $D_{84}$, are larger than $\sim 0.06\pm0.01$. We have clarified these points in the revised manuscript.

Reviewer’s comment:
119: I agree with Wickert that you need to consider hiding effects. The stated Shield’s criterion values of 0.03 to 0.06 normally refer to D50, and in the case of hiding effects (i.e. in most gravel beds) then the Shields value of D84 would be less than for D50. In your response you argue that imbricated grains would be harder to move, and there- fore a
higher value is appropriate; however, if you are considering how grains become imbricated from a non-imbricated bed, then you don’t need to make this adjustment. It’s important to address this issue, because the dimensionless critical shear stress that you use affects whether you reach super-critical flows in Fig 3. If a value less than 0.047 is most appropriate, then it doesn’t support your argument about the importance of super-critical flows.

Our response:
We agree that hiding and protrusion effects are relevant, and that these have a measurable influence on the $\phi$-values and thus on the outcome of our calculations. We discussed the related effects in a separate chapter. We actually find that because most of the largest clasts are either embedded in finer-grained particles, or form well-sorted and densely packed clusters, the finer grained material has to be removed before the largest grains can be entrained. This actually calls for the consideration of hiding effects with larger thresholds. We have discussed this point in full detail in lines 499-543.

Reviewer’s comment:
122: Don’t include 0.047 in eq. 3; use $\phi$ instead as this is consistent with what you show later on when this equation gets combined with others in equations 9 and 10.

Our response:
This has been done.

Reviewer’s comment:
225: You do refer here to the idea of sorting, and therefore hiding, effects affecting the value of $\phi$, but this would be better explained earlier on when you are considering the appropriate value of $\phi$.

Our response:
This has been done.

Reviewer’s comment:
305: I assume that you are looking at exposures that are parallel to the flow direction, but you don’t state whether this is the case. The amount of imbrication that you observe is likely to be affected by the direction of the exposure with respect to the flow direction.

Our response:
We are looking parallel to the flow direction. We have clarified this point.

Reviewer’s comments
350: It might be useful to have a summary of which exposures shows imbrication and which didn’t.

Our response:
The sites/sections which bedrock with or without imbrications are shown on e.g., Figure 2 in Garefalakis and Schlunegger (2018) and in Schlunegger and Norton (2015). We refer to these articles where sites of the sections including the corresponding units are shown and illustrated.
Reviewer's comments
373: It's not obvious to me how eq. 1 explains the decrease in Fr at high slopes and high roughness. This could be more clearly explained. See Lamb et al. (2017) for analysis of the relationships between flow resistance, flow depth and slope.

Our response:
We acknowledge that we have not correctly interpreted these trends. Indeed, the tendency towards lower Froude numbers for a channel gradient >1° (φ >0.05) and a bed roughness >0.3 (φ >0.05) is somewhat unexpected. We explain these trends through the non-linear relationships between slope, water depth, the energy loss within the roughness-layer, and the velocity at the flow’s surface.

Reviewer's comments
423: Changes with slope depend on whether flow depth and hence relative roughness also changes.

Our response:
Indeed. However, we have removed this entire section, because the following statements about rolling/sliding have not convinced P. Carling either.

Reviewer's comment:
449: I don't follow the argument here. I think that you're arguing that because of the pivot angle, then φ should be greater than the typical 0.03 to 0.06? You don't need imbrication to get pivot angles greater than 5 to 10° though. Most gravel grains have higher pivot angles; see Kirchner et al. (1990), Buffington et al. (1992) and Johnston et al. (1998) among others.

Our response:
We have removed this entire section as none of the reviewers has been fully convinced by this.

Reviewer's comment:
583: Where or how are the data available?

Our response:
Actually, the grain size data and other material (Table 1) we have used have already been published, and all new material we have used are presented this article. This means that this particular statement becomes obsolete, so we have removed it.

Specific points raised by reviewer S. McLelland
Reviewer's comment:
Comments by line (I've avoided repeating comments already made by others): 50: The diagram suggests that hydraulic jumps occur at a grain-scale (as shown in Figure 1 and later in Fig 5)? Is this a representative of realistic situations?

Our response:
Yes, it is. We have mentioned this in the revised version.

Reviewer's comment:
169: It's not clear why sediment structures are associated with ‘channel forming floods’. As
experiments have shown, bed structuring can take place as mobile or static armours develop which may be just high flow events rather than channel forming events.

Our response:
This relates to the same comment by A. Wickert. We have corrected the text accordingly.

Reviewer's comment:
288: Are these groups of imbricated clasts cluster bedforms or are they just embedded in the bed structure? It would be useful to distinguish whether or not your structures are clusters both in terms of the moderns streams and stratigraphic record.

Our response:
These are indeed cluster bedforms. We have specified the text accordingly.

Reviewer's comment:
355: You use D/d in text, but D84/d in equations. 373: Equation 1 does directly related to flow depth (d) or D84

Our response:
Both address the same point. We have corrected the text accordingly.

Thank you very much for handling our work.

Sincerely

The authors

References:


Clast imbrications in coarse-grained mountainous streams and stratigraphic archives possibly suggest deposition under upper flow regime conditions

Fritz Schlunegger, Philippos Garefalakis
Institute of Geological Sciences
University of Bern, Switzerland
fritz.schlunegger@geo.unibe.ch
philippos.garefalakis@students.unibe.ch

Abstract
Clast imbrications are one of the most conspicuous sedimentary structures in coarse-grained clastic deposits of modern rivers but also in the stratigraphic record. In this paper, we test whether the formation of such a fabric could be related to the occurrence of upper flow regime conditions in streams. To this extent, we calculated the Froude number at the incipient motion of coarse-grained bedload for various values of relative bed roughness and stream gradient as these are the first order variables that can particularly be extracted from stratigraphic records. We found that a steeper energy gradient, or slope, and a larger bed roughness tend to favor the occurrence of supercritical flows. We also found that at the incipient motion of grains, the ratio $\phi$ between the critical shear stress for the entrainment of a sediment particle and its inertial force critically controls whether flows tend to be super- or subcritical during sediment entrainment. We then mapped the occurrence of clast imbrications in Swiss streams and compared these data with the outcomes of the hydrologic calculations. The results reveal that imbrications possibly record supercritical flows provided that (i) $\phi$-values are larger than c. 0.05, which might be appropriate for streams in the Swiss Alps; (ii) average stream gradients exceed c. 0.5±0.1°; and that (iii) relative bed roughness values, i.e. the ratio between the water depth $d$ and the $D_{90}$, are larger than ~0.06±0.01. While we cannot rule out that imbrication may be formed during subcritical flows with $\phi$-values as low as 0.03, as a large number of flume experiments reveal, our results from Alpine streams suggest that clast imbrications are likely recorders of upper flow regime conditions, provided that the clasts form well-sorted and densely packed clusters. We consider that these differences may be rooted in a misfit between the observational and experimental scales.

1 Introduction
Conglomerates, representing the coarse-grained spectrum of clastic sediments, bear key information about the provenance of the material (Matter, 1964), the environment in which these sediments were deposited (Rust, 1978; Middleton and Trujillo, 1984),

and the hydro-climatic conditions upon transport and deposition of the sediments (Duller et al., 2012; D’Arcy et al., 2017). Conglomerates display the entire range of possible sedimentary structures including a massive-bedded fabric, cross-beds and horizontal stratifications. However, the most striking features are clast imbrications (Figure 1A), which refer to a depositional fabric where sediment particles of similar sizes overlap each other, similar to a run of toppled dominoes (e.g., Pettijohn, 1957; Yagishita, 1997; Rust, 1984; Potsma and Roep, 1985; Todd, 1996). Imbrications may lead to armor development and the interlocking of clasts. As a consequence the search for possible controls on the formation of this fabric has received major attention in the literature (e.g., Bray and Church, 1980; Carling, 1981; Aberle and Nikora, 2006).

In the past decades, the occurrence of clast imbrications in streams has been considered to record high stage flows (Rust, 1978; Miall, 1978; Sinclair and Jaffey, 2001). The related conditions could possibly correspond to the upper flow regime, where the flow velocity of a stream v exceeds the wave’s celerity c (Allen, 1997), i.e. the speed of a wave on the water surface. The ratio v/c between these velocities has been referred to as the Froude number $F$ where in theory $F>1$ denotes upper flow or supercritical conditions, while $F<1$ is characteristic for the lower flow regime or alternatively subcritical conditions (Engelund and Hansen, 1967). A hydraulic jump, which is characterized by a distinct increase in flow surface elevation and a decrease in flow velocity, then marks the downstream transition from a super- to a subcritical flow (Figure 1A). These hydrological conditions are particularly mirrored by the surface texture in relation to water depth. Surface waves that form under subcritical conditions have wavelengths that are smaller than the water depths (Figure 1B). The surface waves tend to migrate and fade out in the upstream direction with respect to the flow. Contrariwise, the wavelengths of standing waves, which represent one possible characteristic feature of supercritical conditions ($F=1$), are significantly larger than the corresponding water depths, and the surface waves are stationary. Hydraulic jumps are manifested themselves by a sudden deceleration of the flow velocity and by an overturning of the flow surface (Figure 1).

Significant sediment accumulation may occur underneath the hydraulic jump upon deceleration of the flow’s velocity (Slootman et al., 2018). Contrariwise, a downstream change from a lower to an upper flow regime occurs gradually and has no distinct surface expression, neither in terms of flow depth nor flow surface texture. While these mechanisms have been well explored and frequently reported both from modern environments (e.g., Figure 1) and fine grained stratigraphic records (Alexander et al., 2001; Schluenegger et al., 2017; Slootman et al., 2018) and illustrated on photos from the field (Spreat sacio et al., 2001), less evidence for an upper flow regime has been documented from the coarse grained fraction of clastic sediments such as conglomerates. This even led Grant (1997) to note that upper flow regime conditions in fluvial channels are
rare, and that the use of the Froude number for constraining flood and palaeo-flood measurements lacks justification from sedimentary records. In the same sense, Jarrett (1984) and Trieste (1992, 1994) considered that reports of inferred supercritical flows might be biased by underestimations of the bed roughness in mountainous streams. Nevertheless, the surface texture of the flow illustrated in Figure 1A is characteristic for many mountainous streams (Spreatico et al., 2001), where hydraulic jumps are observed on the stoss side of large imbricated clasts. In addition, because the entrainment of large clasts such as cobbles and boulders does involve large shear stresses and thus high discharge flows (Rust, 1978; Miall, 1978; Sinclair and Jaffey, 2001), it is possible that the transport and deposition of these particles, and particularly the formation of an imbricated fabric, may occur during supercritical flows. Here, we explore the validity of this hypothesis for modern coarse-grained streams and stratigraphic records, and we calculate the related hydrological conditions. Similar to Grant (1997), we determine the Froude number at conditions of incipient motion of coarse-grained bedload for various bed roughness and stream gradient values. We then compare the results with data from modern streams in the Swiss Alps, stratigraphic records and published results of laboratory experiments.

2 Methods

2.1 Expressions relating flow regime to channel gradient and bed roughness

Channel depth and grain size are the simplest and most straightforward variables that can be extracted from stratigraphic records (Duller et al., 2012). It has been shown that quantitative information about these variables can be used as basis to calculate palaeo-slope and roughness values of streams for the geologic past (Paola and Mohring, 1996; Duller et al., 2012; Schlunegger and Norton, 2015; Garefalakis and Schlunegger, 2018). We therefore decided to focus on the simplest expressions relating channel depth and grain size to flow strength and sediment transport, such as that the resulting formulas can also be applied to geological records. We are aware that this will be associated with large generalizations and simplifications, which will not consider the entire range of complexities that are usually associated with the transport of coarse-grained bedload in streams.

2.2 Boundary conditions

In the following, we consider the hydrological situation at the incipient motion of coarse-grained bedload. For these conditions, the dimensionless Shields parameter $\phi$ can be computed, which is the ratio between the shear stress exerted by the fluid on the bed $\tau_{cb}$ and the particle’s inertial force at the incipient motion (Shields, 1936; Paola et al., 1992; Paola and Mohring, 1996; Tucker and Slingerland, 1997):

$$\phi = \frac{\tau_{cb}}{(\rho - \rho) g D_s} \quad (1a).$$
Here, \( \tau_{CD} \) denotes the critical shear stress, or alternatively the Shields stress, which is required to shift a sediment particle with the grain size \( D_i \). The constants \( \rho_s \) (2700 \( kg/m^3 \)) and \( \rho \) denote the sediment and water densities, and \( g \) is the gravitational acceleration. The relationship expressed in equation (1a) predicts that a sediment particle with diameter \( D_i \) will be transported if the ratio between the fluid’s shear stress \( \tau_{CD} \) and the particle’s inertial force equals the value of \( \phi \). Assignments of values to \( \phi \) vary considerably and largely range between c. 0.03 and 0.06, depending on the site-specific arrangement, the sorting, and the interlocking of the clasts (Buffington and Montgomery, 1997; Church, 1998). This also includes the hiding and protrusion of small and large clasts, respectively, which may exert a strong influence on the threshold conditions upon clast entrainment (e.g., Egiazaroff, 1965; Parker et al., 1982; Andrews, 1984; Kirchner et al., 1990). In the same sense, a smooth and flat channel bed surface, which may be a well-armored channel floor with well-sorted clasts, is likely to offer a greater resistance for the entrainment of a sediment particle than a gravel bar with a poorly sorted arrangement of the bed material (Egiazaroff, 1965; Buffington and Montgomery, 1997).

The relationships denoted in equation (1a) differ for the case of channel forming floods. At these conditions, channel forming Shield stresses \( \tau_{channel} \) are up to 1.2 times (Parker, 1978) above the threshold \( \tau_{CD} \) for the initiation of motion. Pfeiffer et al. (2017) additionally showed that some rivers have \( \tau_{channel}/\tau_{CD} \) ratios that are even higher. The consideration of channel forming floods thus requires larger thresholds and thus a modification of equation (1a), which then takes the following form:

\[
\frac{\phi^2}{\left(\frac{\chi_{\text{channel}}}{\chi_{\text{CD}}} - 1\right) g D_i} = \frac{\tau_{\text{channel}}}{(\rho_s - \rho) g D_i} = 1.2 \phi \quad (1b).
\]

Equation (1a) can then be transformed to an expression, which quantifies the critical shear stress for the entrainment of a sediment particle with a distinct grain size \( D_i \):

\[
\tau_{\text{CD}} = \phi(\rho_s - \rho) g D_i \quad (2).
\]

Among the various grain sizes, the \( D_{84} \) grain size has been considered as more suitable for the characterization of the gravel bar structure than the \( D_{50} \) (Howard, 1980; Hey and Thorne, 1986; Grant et al., 1990). In addition, the \( D_{84} \) has also been considered as a valuable parameter for the quantification of the relative bed roughness, which is defined as the ratio between grain size and water depth (e.g., Wiberg and Smith, 1991). If this inference is valid, then a major alteration of channel-bar arrangements requires a flow strength that is large enough to entrain the grain size represented by the 84th percentile.

Based on the results of flume experiments (Meyer-Peter and Müller, 1948) and observations in the field (Andrews, 1984), a Shields variable of \( \phi = 0.047 \) has...
conventionally been employed in a large number of studies (e.g., Paola and Mohring, 1996) particularly if the $D_{50}$ is considered. Note that a re-analysis (Wong and Parker, 2006) of the Meyer-Peter and Müller equation (1948) returned values of $\phi = 0.0495 \pm 0.05$, which we thus applied in this paper. However, experiments also showed that material transport can occur at much lower thresholds where $\phi$-values are as low as 0.03 (Ferguson, 2012; Powell et al., 2016). A $\phi$-value of 0.03 might particularly be an appropriate threshold for the entrainment of the $D_{84}$, because of possible protrusion effects (e.g., Kirchner et al., 1990). Finally, Mueller et al. (2005) proposed that $\phi$ depends on channel gradients, where $\phi$ (for the $D_{50}$ grain size) might exceed 0.1 for channels that are steeper than 1.1°. It appears that the thresholds for the entrainment of sediment strongly vary according to site and experiment specific conditions. We therefore employed the entire range of $\phi$-values from 0.03 to 1.1 to comply with these complexities, which also includes channel forming floods (Parker, 1978).

2.3 Hydrology, bed shear stresses and incipient motion of clasts

Bed shear stress is calculated using the approximation for an uniform flow down an inclined plane (e.g., Tucker & Slingerland, 1997), where:

$$\tau = g \rho S d$$  \hspace{1cm} (3)

Here, $S$ denotes the channel gradient, and $d$ is the water depth. This relationship has been considered as adequate for streams with a steady, uniform flow, and where channel widths are more than 20 times larger than water depths, which is commonly the case for most rivers (Tucker and Slingerland, 1997). Alternatively, bed shear stresses can also be computed as a function of the kinetic energy (Ferguson, 2007), where:

$$\tau = f \rho v^2$$  \hspace{1cm} (4)

In this relationship, $v$ is the flow velocity. The variable $f$, referred to as the Darcy-Weisbach friction factor (e.g., Papaevangelou et al., 2010), denotes the energy loss due to friction within the roughness layer at the bottom of the flow. It also considers skin friction effects within the flow column (Ferguson, 2007). These relationships illustrate that assignments of values to $f$ are complicated and vary considerably. Ferguson (2007) reduced these complexities to a single expression (equation 5), where he considered roughness-layer (Krogstad and Antonia, 1999) and skin friction effects on the velocity of a water column at its surface. In the Ferguson (2007) relationship, $f$ depends on water depths $d$ relative to the grain size $D_{84}$ and thus on the relative bed roughness:
Here, \( a_1 \) and \( a_2 \) are constants that vary between 7–8 and 1–4, respectively (Ferguson, 2007). A calibration of equation 5 by Ferguson (2007), where the \( D_a \) was employed as the threshold grain size, returned values of 7.5 and 2.36 for \( a_1 \) and \( a_2 \), respectively, which we adapt in this paper. We additionally considered possible consequences of energy loss through assignments of different values to the Shields (1936) variable (see explanation of equation 1a above). We are aware that we could also employ the Manning’s number \( n \) for the characterization of the channel’s fabric (Whipple, 2004) and the relative bed roughness (Jarrett, 1984). Related expressions deviated by Jarrett (1984) predict that the Manning’s number \( n \) hinges on the channel gradient and water depth only and does not consider a dependency on the bed structure. We thus prefer to use Ferguson’s (2007) approach (eq. 6), which explicitly includes the relative bed roughness, consistent with the most recent work by Wickert and Schildgen (2018, see their equation 13).

As outlined in the introduction, the Froude number \( F \) can be approximated through the ratio between the flow velocity \( v \) and the celerity of a surface wave \( c \). For shallow water conditions, which is commonly the case for rivers and streams, this relationship can be computed if the water depth \( d \) is known:

\[
F = \frac{v}{c} = \frac{v}{\sqrt{gd}} \tag{6}
\]

Combining equation 3, 4, and 6 yields then a simple expression where:

\[
F = \sqrt{\frac{S}{f}} \tag{7}
\]

This expression states that the flow regime, expressed here by the Froude number \( F \), depends on two partly non-related variables. In particular, for a given bed friction \( f \), which depends on the bed roughness, (Ferguson, 2007), upper flow regime conditions tend to establish for steep channels. Contrariwise, lower regime flows may occur in a steep environment where poorly sorted material exerts a large resistance on the flow, thereby reducing the flow velocity and hence the Froude number. Accordingly, where the entrainment of sediment particles can be expressed through the Shields (1936) variable \( \phi \), the dependency of \( F \) on the channel gradient \( S \) can be computed through the combination of equations 2, 3, 5, and 7:

\[
F = \sqrt{\frac{S}{\frac{\rho S}{\phi(\rho_s - \rho)} a_1^2 + \frac{\rho S}{\phi(\rho_s - \rho)} a_1^2}} \tag{8}
\]
Alternatively, also during channel forming floods, an expression where the Froude number depends on the bed roughness $D_{50}/d$ only can be achieved through the combination of equations $2$, $3$, and $7$:

$$ F = \frac{8 \cdot \phi (\rho_s - \rho) \cdot D_{50}}{\rho^* f} \left(\frac{d}{D_{50}}\right)^{7} $$

We thus used equations $8$ and $2$ to calculate the Froude numbers at the incipient motion of the $D_{50}$ grain sizes. We then compared these results with data from modern streams and stratigraphic records.

2.4 Collection of data from modern streams and stratigraphic records

We used observations about clast arrangements in gravely streams in Switzerland. We paid special attention to the occurrence of clast imbrications, as we hypothesize that this fabric may document the occurrence of upper flow regimes (Figure 1) upon sedimentation and gravel bar migration. We selected those sites for which Litty and Schlunegger (2017) reported grain size data (Table 1). At these locations, we explored multiple gravel bars for the occurrence or absence of clast imbrications over a reach of several hundreds of meters. We then determined a mean energy gradient over a c. 500 m-long reach, which we calculated from topographic maps at scales 1:10’000.

The selected streams are all situated around the Central Alps (Figure 2), have various upstream drainage basins and different source rock lithologies (Spicher, 1980) and grain size distributions. At sites where grain size data has been collected, the ratio between the clasts’ medium $b$- and longest $a$-axes are constant and range between 0.67 and 0.72 irrespective of the grain size distribution in these streams (Litty and Schlunegger, 2017). For these sites, we calculated the bed roughness $D_{50}/d$ at the incipient motion of the $D_{50}$.

Here, related water depths $d$ were determined through the combination of equations $2$, and $3$, and using the channel gradient $S$ at these sites.

The Swiss Federal Office for the Environment (FOEN) estimated the Froude numbers for various flood magnitudes of selected streams situated on the northern side of the Swiss Alps (Spreafico et al., 2001; see Figure 2 for location of sites). These estimates are based on flow velocities, flow depths and cross-sectional geometries of channels. The authors of this study also determined the corresponding channel gradient over a reach of several hundred meters. Because we will calculate the dependency of the Froude number on the channel gradient and the thresholds for the entrainment of sediment, expressed through different $\phi$-values, we will use the Spreafico et al. (2001) dataset to constrain the range of possible $\phi$-values for streams in Switzerland.

We finally identified possible relationships between channel gradient, bed roughness, and the occurrence of clast imbrications from stratigraphic records. We focused on the Late Oligocene suite of alluvial megafan conglomerates (Rigi and Thun sections, Figure 2).
3 Results

3.1 Calculation of flow regimes as a function of bed roughness and channel gradient

We calculated the Froude numbers $F$ for different values of channel gradient $S$, bed roughness $D_{50}$, and threshold conditions $\phi$ for the incipient motion of material, and we compared these results with observations from modern streams and stratigraphic records.

We avoided calculation of the Froude numbers for slopes steeper than 1.4° because channels tend to adopt a step-pool geometry in their thalwegs (Whipple, 2014), for which our simple calculations might no longer apply. We set the thresholds for critical flow conditions to a Froude number $F$=0.9, which is consistent with estimations for the formation of upper flow regime bedforms by Koster (1978). Calculations were initially carried out using a Shields variable of $\phi = 0.0495 \pm 0.05$, as this value has commonly been used in a large number of studies (see above). The results reveal that the Froude number increases with steeper channels (Figure 3A) and reaches the field of critical conditions for \(\approx 0.5^\circ\) slopes. The values reach a maximum of nearly 1 where channel gradients are between \(-0.8^\circ\)\,-\(1^\circ\). Froude numbers then slightly decrease for channels steeper than \(1^\circ\) and finally reach a value of 0.9 for gradients \(>1.2^\circ\). In the case of greater thresholds for the incipient motion of clasts, which is expressed through a larger Shields (1936) variable of $\phi = 0.06$, flows adapt supercritical conditions for channels steeper than \(-0.4^\circ\). For cases where the thresholds for the entrainment of the material are less (expressed here through a lower Shields (1936) variable of $\phi = 0.03$), streams remain in the lower flow regime.

The Froude number pattern is quite similar for increasing bed roughness (Figure 3B). For threshold conditions expressed through a Shields (1936) variable $\phi = 0.0495 \pm 0.05$, the Froude numbers increase with higher relative bed roughness. Supercritical conditions are reached for a bed roughness of c. 0.1, after which the Froude numbers decrease with greater roughness. At larger threshold conditions for sediment entrainment, expressed through a Shields variable $\phi = 0.06$, upper flow regime conditions might prevail for bed surface roughness values between 0.06 and 0.5. Smaller and larger roughness values will keep the flow in the lower regime. Contrariwise, the stream will not shift to the upper regime for $\phi$-values as low as 0.03. Note that the consideration of the full range of roughness-layer and skin friction effects, expressed through the coefficients $a_i$ and $a_j$ in equation (8), shifts the pattern of Froude values to lower and higher values. But this will not
alter the general finding that upper flow regime conditions at the incipient motion of gravels might be expected for channel gradients \( S \) that are steeper than \( 0.5^\circ \pm 0.1^\circ \), and for a bed roughness \( D_{50}/d \) greater than \(-0.06\).

We also calculated the Froude numbers for a Shields variable of \( \phi = 0.1 \), because observations have shown that thresholds for the entrapment of sediment particles may increase with steeper channels (Mueller et al., 2005; Ferguson, 2012). This might be an exaggeration (Lamb et al., 2008), but will give an upper bound for the dependence of the Froude number on the Shields variable. We additionally considered the case where the Shields (1936) variable depends on the channel gradient \( S \) through \( \phi = 2.81^*S+0.021 \) (Mueller et al., 2005). These relationships have been established using bed load rating curves, which are based on field surveys in mountainous streams in North America and England. We found that the flows shift to critical conditions for channels steeper than between \( 0.5^\circ \) and \( 0.6^\circ \) (slope dependent \( \phi \) and for a bed roughness \( >0.04 \ (\phi = 0.1) \). In summary, the calculations predict that water flow may shift to upper flow regime conditions for: (i) \( \phi \)-values larger than \( 0.05 \), (ii) slopes steeper than \(-0.5^\circ \pm 0.1^\circ \); and (iii) relative bed roughness values greater than \(-0.06\pm0.01 \).

3.2 Estimates of \( \phi \)-values from modern streams in the Central Alps

Spreafico et al. (2001) estimated the Froude numbers for various streams situated on the northern side of the Swiss Alps. Related values range between 0.2 and 1.1 and generally increase together with channel gradients (vertical bars on Figure 3A). The surface expressions of the flows particularly of the Birse and Thur streams (labeled as \( b \) and \( t \) on Figure 3A) are characterized by multiple hydraulic jumps (Spreafico et al., 2001, p. 71 and p. 77). Therefore, the inferred small Froude numbers (between 0.6 and 0.9) of these streams have to be treated with caution.

The Froude number estimates by Spreafico et al. (2001) disclose a large scatter in the relationship to the channel gradient (Figure 3A, vertical bars). This can partially be explained by site-specific differences in bed roughness, which are related to anthropogenic corrections and constructions (Spreafico et al., 2001). Nevertheless, the comparison between these data and the results of our calculations reveal that the entire range of \( \phi \)-values between 0.03 and 0.1 has to be taken into account for the hydrological conditions in the streams surrounding the Swiss Alps (Figure 3A). This also implies that the selection of a threshold, expressed by the \( \phi \)-value, warrants a careful justification, which we present in the discussion.

3.3 Data about the occurrence or absence of clast imbrications from modern streams

Here, we present evidence for imbrications and non-imbrications from modern rivers, and we relate these observations to channel slope (Figure 4A) and bed roughness.
Data on grain size, stream runoff and channel morphology are available for several rivers in the northern, the central and the southern part of the Swiss mountain belt. These streams are situated both in the core of the Alps and the foreland. The bedrock-geology of their headwaters includes the entire range of lithologies from sedimentary units to schists, gneisses and granites. In the same sense, the streams cover the full range of water sources in their headwaters including glaciers and surface runoff. Except for the Maggia River between the sites Bignasco and Losone (Figure 2), all streams are channelized, and the rivers generally flow in a bed that is laterally confined by artificial riverbanks. These are either made up of concrete walls or outsized boulders. In this context, information about the hydrographs, grain size and the results of the shear stress calculations consider the time after these constructions have been made.

Channel morphologies

The thalweg of the streams meanders between the artificial walls within a 20 to 50 m-wide belt. Flat-topped longitudinal bars that are several tens of meters long and that emerge up to 1.5 m above the thalweg are situated adjacent to the artificial riverbanks on the slip-off slope of these meanders. They evolve into subaquatic transverse bars, or riffles, farther downstream where the thalweg shifts to the opposite channel margin. Channels are deepest and flattest along the outer cutbank side of the meanders and in pools downstream of riffles, respectively. The thalweg then steepens where it crosses the transverse bars and riffles. This is also the location where some streams show evidence for standing waves with wavelengths >5 m (e.g., at Reuss, Figure 5). Standing waves have also been encountered in the Waldemme River at Littau (Figure 6B) when water runoff at that particular site was c. 100 m³/s and when rumbling sounds suggested that clasts were rolling or sliding. The streams thus display a complex pattern where channel depths, flow velocities and possibly also hydrological regimes alternate over short distances of tens to hundreds of meters. These arrangements of channel-bar pairs and particularly their positions within the channel belt have been stable over the past years as the locations of the gravel bars are still the same as the ones reported by Litty and Schlunegger (2016).

Streams with evidence for clast imbrication

Inspections of gravel bars have shown clear evidence for imbrications in the Glenner, the Landquart, the Verzasca, and the Waldemme rivers (Table 1). In these streams, channel gradients range between 0.6° (Waldemme) and 1.2° (Glenner) (Figure 4A). The sizes of the $D_{54}$ range between 3 cm (Waldemme) and 12 cm (Glenner). The gravel lithology includes the entire variety from sedimentary (Waldemme) to crystalline constituents (Glenner, Landquart, Verzasca). The inferred bed roughness at the incipient motion of the $D_{54}$ includes the range between c. 0.125 (Waldemme) and 0.31 (Glenner) (Figure 4B).
At Maggia, Reuss and Waldemme Littau, the largest clasts are arranged as triplets or quadruplets of imbricated constituents within generally flat lying to randomly-oriented finer grained sediment particles. The density of these arrangements ranges between 5 groups per 10 m² (Maggia Bignasco, Maggia Losone) to c. 10 groups per 10 m² (Maggia Visletto, Reuss, Waldemme Littau e.g. Figure 6D). The channel gradients at these sites span the range between c. 0.3 and 0.6°, and the $D_{50}$ clasts are between 3 and 9 cm large (Reuss and Maggia Visletto). Accordingly, the relative bed roughness at the incipient motion of the $D_{50}$ ranges between 0.07 and 0.16.

At all sites mentioned above, clasts on subaquatic and subaerial gravel bars are generally arranged as well-sorted and densely packed clusters, possibly representing incipient bedforms (e.g., Figure 6D). In most cases, grains imbricate behind an outsized clast, which usually delineates the front of imbricated arrangements of sediment particles. In addition, the lowermost 10-20% part of most of the large clasts is embedded, and thus buried, in a fine-grained matrix, which was most likely deposited during the waning stage of a flood. Isolated, non-buried clasts that are flat lying on their $a$-$b$-planes do occur but are less frequent than embedded clasts or constituents arranged in clusters. The inclination dip of the $a$-$b$-planes ranges between c. 20-40° (Figure 6D). Finally, streams with clast imbrications display surface expressions, which point to an upper flow regime during low (e.g., Reuss, Figure 5B) and high-water stages (e.g., Waldemme, Figure 6B).

Streams with little or no evidence for clast imbrication

Gravel bars within the Emme stream are made up of generally flat lying gravels and cobbles. A small tilt of <10° of $a$-$b$-planes occurs where individual clasts slightly overlap each other, similar to a shingling arrangement of particles. This is particularly the case in pools and on the upstream stoss-side of longitudinal and transverse bars where channel gradients are flat. Also in the Emme River, clast imbrications occur in places only where gravel bars have steep downstream slip faces, which are mainly observed at the end of transverse bars. At sites where imbrication is absent, most of the clasts are lying flat on their $a$-$b$-planes, and embedding by finer-grained material is less frequently observed than in streams with clast imbrications. The channel gradient is less than 0.5°, and the size of the $D_{50}$ measures 2 cm. The bed roughness of this stream, calculated for the incipient motion of the 84th grain size percentile, ranges between 0.07 and 0.10. Finally, the flow displays a smooth surface expression during low- and high-water stages (Speziale et al., 2001, p. 53), which is a characteristic evidence for lower flow regime conditions.

The channel morphology of the Sense River differs from that of the Emme stream in the sense that bedrock reaches alternate with alluvial segments over a wavelength of 100-200 meters and more. Alluvial segments are flat (c. 0.3°) and host lateral and transverse gravel
bars where the $D_{sl}$ measures 6 cm. On top of these bars, gravels are generally lying flat on their a-b-planes (Figure 6C). Imbrications are observed where some of these gravels are overlapping each other, resulting in a dip angle of 10-20°. Contrariwise, bedrock reaches (site $S'$ on Figure 4A) that form distinct steps in the thalweg are up to 0.5° steep and partly covered by subaquatic longitudinal bars (Figure 1B) where imbricated clasts alternate with flat-lying grains at the meter scale. The channel bed surface is generally well-sorted and well- armored where clasts are either interlocked, partly isolated, and also rooted in a finer-grained matrix, as a photo of a subaquatic longitudinal bar shows (Figure 6A). At these sites, upper flow regime segments laterally change to lower flow regime reaches over short distances of a few meters (Figure 1B). While we have made this observation during low water stages only, it is very likely that sub- and supercritical flows also change during flood stages over short distances, as various examples of Alpine streams show (Spreafico et al., 2001).

3.4 Data about the occurrence or absence of clast imbrications from stratigraphic records

Here, we calculated patterns of bed roughness and related channel gradients and explored c. 50 conglomerate sites for the occurrence or absence of clast imbrications. We used published data about channel depth $d$, surface gradients S and information about the pattern of the $D_{sl}$, which have been reported from the Late Oligocene alluvial megafan conglomerates at Rigi (47°03'N / 8°29'E) and Thun (46°46'N / 7°44'E) situated in the Molasse foreland basin north of the Alpine orogen (Figure 2, Table 1). The depositional evolution of these conglomerates has been related to the rise of the Alpine mountain belt and the associated erosional history of this orogen (Kempf et al., 1999; Schlunegger and Castelltort, 2016).

The deposits at Rigi are c. 3600 m thick and made up of an alternation of conglomerates and mudstones (Stürm, 1973) that were deposited between 30 and 25 Ma according to magneto-polarity chronologies and mammal biostratigraphic data (Engesser and Kälin, 2017). Garefalakis and Schlunegger (2018) subdivided this alternation of conglomerates and mudstones into four segments labeled as $\alpha$ through $\delta$. The lowermost segments $\alpha$ and $\beta$ are an alternation of mudstones and conglomerate beds and were deposited by gravelly streams (Stürm, 1973). According to Garefalakis and Schlunegger (2018), the depositional area was characterized by a low surface slope ranging between 0.2±0.06° and 0.4±0.2°. Channel depths span the range between 1.7 and 2.5 m, and the $D_{sl}$ values are between 2 and 6 cm. These measurements result in bed roughness values between 0.02 and 0.05. Except for one site, we found no imbrications in outcrops of $\alpha$ and $\beta$ units (Figures 4, 7A).

The top of the Rigi section, referred to as segments $\gamma$ and $\delta$ by Garefalakis and
Schlunegger (2018), is an amalgamated stack of conglomerate beds deposited by non-confined braided streams (Stürm, 1973). Garefalakis and Schlunegger (2018) inferred values between 0.65±0.2° and 0.9±0.4° for the palaeo-gradient of these rivers (Table 1). $D_{50}$ values range between 6 and 12 cm, and palaeo-channels were c. 1.2 m deep. This yields a relative bed roughness between c. 0.05 and 0.12. Interestingly, a large number of conglomerate sites within the segments $\gamma$ and $\delta$ display evidence for clast imbrications in outcrops parallel to the palaeo-discharge direction (Figures 4, 6B). In addition, some outcrops show sedimentary structures that correspond to cluster bedforms of imbricated clasts (C on Figure 7B). However, at all sites, the lateral extents of groups with imbricated clasts are limited to widths of 1-2 meters. Please refer to Garefalakis and Schlunegger (2018) and their Figure 2 for location of sites displaying units $\alpha$ through $\delta$.

The up to 3000 m-thick conglomerates at Thun are slightly younger, and the ages span the time interval between c. 26 and 24 Ma according to magneto-polarity chronologies (Schlunegger et al., 1996). Similar to the Rigi section, the conglomerates at Thun start with an alternation of conglomerates, mudstones and sandstones, which has been referred to as unit A. This suite is overlain by an up to 2000 m-thick amalgamated stack of conglomerate beds (unit B). Channel depths within unit A range between 3 to 5 m, and streams were between 0.1° and 0.3° steep. Channels in the overlying unit B were shallower and between 1.5 and 3 m deep. Stream gradients varied between 0.4° and 1°, depending on the relationships between inferred water depths and maximum clast sizes (Schlunegger and Norton, 2015). In outcrops parallel to the palaeo-discharge direction, sequences with imbricated clasts have only been found in unit B where palaeo-channel slopes were steeper than 0.4° (Figure 4A). Similar to the Rigi section, the lateral extents of groups with imbricated clasts are limited to widths of a few meters only. No data is available for computing the $D_{50}$ grain size, with the consequence that we cannot estimate the bed roughness for the Thun conglomerates. Please see Schlunegger and Norton (2015) for location of sites where units A and B are exposed.

Similar to the modern examples, imbricated clasts form a well-sorted cluster and commonly include the largest constituents of a gravel bar. In most cases, clasts imbricate behind an outsized constituent, which usually delineates the front of an imbricated arrangement of clasts (Figure 7B).

### Discussion

#### 4.1 Selection of preferred boundary conditions

Our calculations reveal that the results are strongly dependent on: (i) the selection of values for the Shields variable $\phi$; (ii) the way of how we consider variations in slope $S$ at the bar and reach scales, and (iii) the consideration of flood magnitudes which either result in the motion of individual sediment particles or the alteration of the shape of an entire
channel (channel forming floods). This section is devoted to justify the selection of our preferred boundary conditions.

Thresholds regarding channel forming floods versus incipient motion of individual clasts
We constrained our calculations on the incipient motion of individual clasts and used equation (1a) for all other considerations. This approach might be perceived as a large contrast to the hydrological conditions during channel forming floods where thresholds for the evacuation of sediment are up to 1.2 times larger, as theoretical and field-based analyses and have shown (Parker, 1978; Philips and Jerolmack, 2016; Pfeiffer et al., 2017). Nevertheless, the consequences on the outcome of our calculations are minor, at least when the Froude number dependencies on the slope and bed roughness parameters are considered. In fact, a 1.2-times larger threshold will increase the $\phi$-values (equation 1b) to the range between 0.036 and 0.072. However, as illustrated in Figure 3, this will not change the general pattern. In addition, while channel forming floods are mainly associated with equal mobility of a large range of sediment particles, the formation of an imbricated fabric involves the clustering of individual clasts only. We use these arguments to justify our preference for using equation 1a (incipient motion of clasts) rather than equation 1b (channel forming floods).

Protrusion and hiding effects and consequences for the selection of $\phi$-values
Larger bed surface grains, as is the case for most of the imbricated clasts, may exert lower mobility thresholds because of a greater protrusion and a smaller intergranular friction angle, as noted by Buffington and Montgomery (1997) in their review. Related consequences have been explored in experiments (e.g., Buffington et al., 1992) and through field-based studies, which were likewise complemented with experiments in the laboratory (Johnston et al., 1998). These studies resulted in the notion that the entrainment of the largest clasts (e.g., the $D_{84}$) most likely requires lower flow strengths than the shift of median-sized sediment particles. As a consequence, while $\phi$-values might be as high as 0.1 for the displacement of the $D_{50}$ (Buffington et al., 1992), conditions for the incipient dislocation of large clasts could be significantly different. In particular, for clasts that are up to five times larger than the $D_{50}$ (which corresponds to the ratio between the $D_{84}$ and the $D_{50}$ of the Swiss data, Table 1), Buffington et al (1992) and also Johnston et al. (1998) predicted $\phi$-values that might be as low as 0.03 or even less. Related $\phi$-values, for instance, have indeed been applied for mountainous streams where the supply of sediment from the lateral hillslopes has been large (van der Berg and Schlunegger, 2012). Large sediment fluxes have been considered to result in a poor sorting and a low packing of the material, and thus in low thresholds particularly for the incipient motion of large clast...
(Lenzi et al., 2006; van der Berg and Schlunegger, 2012). Our calculations predict that an upper flow regime is very unlikely to establish at these conditions (φ-value of 0.03). However, we consider it unlikely that the formation of most of the imbrications, as we did encounter in the analyzed Alpine streams and in the stratigraphic record, were associated with thresholds as low as those proposed by e.g., Lenzi et al. (2006) and van der Berg and Schlunegger (2012). We base our inference on the observation that the analyzed gravel bars display an arrangement where large clasts are generally well sorted and densely packed, both on subaerial (during low water stages) and subaquatic bars. This results in a high interlocking degree of sediment particles within the bars we have encountered in the field. In addition, field inspections showed that the base of most of the large clasts, particularly those in subaquatic bars, are embedded and thus buried in finer grained material, and only very few clasts are lying isolated and flat on their a-b-planes. This implies that the fine-grained sediment particles have to be removed before these clasts can be entrained. In this case, hiding effects associated with φ-values >0.5 would possibly be appropriate for the prediction of material entrainment of the finer-grained sediments before the larger clasts can be shifted (Buffington and Montgomery, 1997). As a consequence, a dislocation of these clasts and thus a rearrangement of the sedimentary fabric most likely require that large thresholds have to be exceeded, which is mainly accomplished through high-discharge events with large flow strengths. We thus propose that the use of φ-values of c. 0.05, which is commonly used for the entrainment of the D₅₀ (Paola and Mohring, 1996), is also adequate for the calculation of the hydrological conditions associated with the fabric we have encountered in the field. We do acknowledge, however, that this hypothesis warrants a test with quantitative data, which we have not available. Please note that the low Froude numbers and thus the low φ-values of 0.3 inferred for the Thur and the Birse streams might be underestimated, because photos that were taken during high stage flows of these streams display clear evidence for multiple hydraulic jumps over m-long reaches (Spreafico et al., 2001, p. 71 and 77).

Variations in channel gradient at the bar and reach scales

Figure 3 shows that the results largely hinge on the values of φ and S. We applied equation 3 while inferring a steady uniform flow and a bed slope, which is constant over a distance of 500 m. We did not consider any smaller-scale slope variations that are caused by downstream alternations of bars, riffles and pools as we lack the required quantitative information. This inference results in an energy slope, which is neither equal to the water surface slope nor to the bed slope. Such inequalities increase substantially when unsteady non-uniform super-critical flows and transitions are considered (e.g., Figure 1A), which is not fully described by equations 3 and 4, and which introduces a bias. These variations in channel floor morphologies are likewise not depicted in experiments either (e.g., Buffington...
et al., 1992; Powell et al., 2016), which could partially explain the low $\phi$-values that result from these studies. We justify our simplification because we are mainly interested in exploring whether supercritical flows are likely to occur for particular $\phi$- and channel gradient values.

4.2 Relationships between channel gradient, bed roughness and flow regime

We have found an expression where the Froude number $F$, and thus the change from the lower to the upper flow regime, depends on the channel gradient $S$ and the bed roughness $D_b$ (eq. 7). This relationship also predicts that the controls of both parameters on the Froude number are to some extent independent from each other. Under these considerations, the similar pattern of how the Froude number $F$ depends on channel gradient and bed roughness (Figure 3) appears unexpected. However, we note that we computed both relationships for the case of the incipient motion of the grain size percentile $D_{50}$. This threshold is explicitly considered by equation 2, which we used as basis to derive an expression where the Froude number depends on the channel gradient or the bed roughness only. Therefore, it is not surprising that the dependencies of the Froude number on gradient and bed roughness follow the same trends. In addition, Blissenbach (1952), Paola and Mohring (1996) and also Church (2006) showed that channel gradient, water depth and grain size are closely related parameters during the entrainment of sediment particles. In particular, channels with coarser grained gravel bars tend to be steeper and shallower than those where the bed material is finer grained (Church, 2006). In the same sense, also in steeper streams, bed roughness values tend to be larger than in flatter channels (Whipple, 2004). We use the causal relationships between these variables to explain the similarity in the patterns illustrated in Figures 3A and 3B.

The tendency towards lower Froude numbers for a channel gradient $>1^\circ$ ($\phi >0.05$) and a bed roughness $>0.3$ ($\phi >0.05$) is somewhat unexpected. We explain these trends through the non-linear relationships between slope, water depth, the energy loss within the roughness-layer, and the velocity at the flow’s surface.

4.3 The formation of imbrications in experiments

Interpretations of the possible linkages between hydrological conditions upon material transport and the formation of imbrications are hampered because experiments have not been designed to explicitly explore these relationships. In addition, as noted by Carling et al. (1992), natural systems differ from the conditions in experiments because of the contrasts in scales. Nevertheless, it was possible to reproduce the formation of clast imbrications in subcritical flumes (Carling et al., 1992), or at least in the absence of any change in flow regime in many experiments. For instance, Qin et al. (2013) quantified the imbrications that resulted from the experiments by Aberle and Nikora (2006) where...
flows have been stationary. Carling et al. (1992) additionally showed that the shape of a clast has a strong control on the thresholds for incipient motion, the style of motion, and the degree of imbrication. A similar arrangement of clasts was formed in the experiments by Powell et al. (2016) and Bertin and Friedrich (2018), who reproduced imbrications with low Froude numbers between c. 0.55 and 0.9. Please note that we inferred these numbers from the experimental setup of these authors. Powell et al. (2016) additionally showed that the material can be entrained with $\phi$-values as low as 0.03, which is consistent with calculations of Froude numbers for some of the streams in Switzerland. Also during experiments, Johansson (1963) reported particle vibration before entrainment either through rolling or sliding. He noted that imbrication was formed at conditions, which corresponded to the lower flow regime during the flume experiments. Based on field observations, Sengupta (1966) reported examples where imbrication was most likely initiated by the development of current crescents around pebbles that were embedded in sand, and that these processes possibly occurred during lower regime flows. Such eddies preferentially develop at the upstream end of pebbles, which then leads to the winnowing of the fine grained sand at the upstream edge and the tilting of this particular clast. Additional sliding, pivoting and vibrating of these sediment particles might then result in the final imbrication. If this process occurs multiple times and affects the sand-gravel interface at various sites, then an armored bed with imbricated clasts can establish without the necessity of supercritical flows, or changes in flow regimes, as experimental results have shown (Aberle and Nikora, 2006; Haynes and Pender, 2007). Such a fabric may even form in response to prolonged periods of sub-threshold flows, as summarized by Ockelford and Haynes (2013). Finally, using flume experiments in a 0.3 m-wide, 4 m-long, recirculating tilting channel flume, Brayshaw (1984) was able to reproduce cluster bedforms with imbricated clasts during subcritical flows ($F$-numbers between 0.03 and 0.07). However, inspections of photos illustrating the experimental set up reveal that the surface grains are either flat lying on finer-grained sediments before their entrainment (Figure 3 in Powell et al., 2016), occur isolated on the ground (Figure 2.1b in Carling et al., 1992), or have a low degree of interlocking (Figure 3a in Lamb et al., 2017). Interestingly, the experiment by Buffington et al. (1992) followed a different strategy, where a natural bed-surface of a stream was peeled off with epoxy. They subsequently used this peel in the laboratory to approximate a natural channel bed surface (see their Figure 4), on top of which they randomly placed grains with a known size distribution. Buffington and co-authors then measured the friction angle of the overlying grains, based on which they calculated the critical boundary shear stress values $\phi$. In all experiments, the surface morphology of the sedimentary material is flat and lacks topographic variations, which we found as reach-scale alternations of riffles, transverse bars and pools in the field. The low $\phi$-values of 0.03, which appears to be typical of bed surface conditions that develop in
laboratory flumes (Ferguson, 2012), as summarized by Powell et al. (2016), could possibly be explained by these conditions. Furthermore, and probably more relevant, the lengths of the experimental reaches are generally less and range between e.g., 4.0 meters (Brayshaw, 1984), 4.4 meters (Powell et al., 2016), 15 meters (e.g., Lamb et al., 2017) and even 20 meters (Aberle and Nikora, 2006). We acknowledge that in most experiments the variables have been normalized through an e.g., constant Reynolds or Froude number (Brayshaw, 1984). This normalization also includes the experimental $D_{50}$-grain sizes, which are very similar to those we have determined for our selected streams (Litty and Schlunegger, 2017). Nevertheless, we find it really hard to upscale some of the results associated with these experiments to our natural cases where standing waves of 1 m, and even between 5 and 8 meters lengths may occur (our Figures 1B, 5B, 6B), which are not reproducible in the experiments. In addition, Powell et al. (2016) observed that the water surface stayed relatively stable during their experiments, and that the flows were steady and uniform without hydraulic jumps. This contrasts to our natural cases where upper and lower flow regimes alternate over short distances even during low-stage flows. Finally, while winnowing of fine grained material, tilting of clasts and subsequent bed armouring might be a valuable mechanism for the explanation of imbrications during low stage flows in experiments, we consider it unlikely that these results can be directly translated to our field observations. We base our inference on two closely related arguments. First, our reported groups of imbricated clasts tend to be arranged as cluster bedforms (e.g., Figures 6D, 7B), which rather form in response to selective deposition of large clasts (Brayshaw, 1984) than selective entrainment of fine-grained material (Figure 6A). Second, observations (Berther, 2012) and calculations (Litty and Schlunegger, 2017) have shown that effective sediment transport in these streams is likely to occur on decadal time scales (and most likely much shorter; van der Berg and Schlunegger, 2012), at least for subaquatic bars. Sediment transport is then likely to occur over a limited reach only. This means that a large fraction of the shifted material per flood has a local source situated in the same river some hundreds of meters farther upstream where bars are also well armored. This possibly calls for large thresholds for the removal of clasts. In addition, on subaerial bars, waning stages of floods result in the deposition of fine-grained material and not in the winnowing of sand, as our observations have shown. Accordingly, while low $\phi$-values and thus a lower flow regime might be appropriate for predicting the entrainment of the sediment particles in experiments, greater thresholds and thus larger $\phi$-values are likely to be appropriate for our natural examples for the reasons we have explained in above.

4.4 Possible relationships between flow regimes and clast imbrications based on field observations
Here, we provide evidence for proposing that clast imbrications can be linked with supercritical flows provided that the gravel bars form a well-sorted arrangement of densely packed particles with a clast-supported fabric, as we have encountered in our streams. We sustain our inferences with (i) published examples from natural environments; (ii) our observations from Swiss streams; and (iii) the results of our calculations.

For the North Saskatchewan River in Canada, Shaw and Kellerhals (1977) reported gravel mounds on a lateral gravel bar, which have a regular spacing between 2 and 3 meters and a relatively flat top. Shaw and Kellerhals considered these bedforms as antidunes, which might have formed in the upper flow regime. Also in modern gravely streams, transverse ribs, which are a series of narrow, current-normally orientated accumulations of large clasts, were considered as evidence for the deposition either under upper flow regime conditions, or in response to upstream-migrating hydraulic jumps (e.g., Koster, 1978; Rust and Gostin, 1981). Koster (1978) additionally reported that these bedforms are associated with clast imbrications (Figure 2 in Koster, 1978). Alexander and Fielding (1997) found modern gravel antidunes with well-developed clast imbrications in the Burdekin River, Australia. Finally, Taki and Parker (2005) reported cyclic steps of channel floor bedforms with wave-lengths that are 100–500 times larger than the flow thickness. These bedforms most likely represent chute-and-pool configurations (Taki and Parker, 2005), which could have formed in response to alternations of upper and lower flow regime conditions, as outlined by Grant (1997). In such a situation, the upstream flow on the stoss-side of the bedform may experience a reduction of the flow velocity, with the effect that the flow may shift to subcritical conditions. This could be associated with a hydraulic jump and a drastic reduction of the flow velocity and thus with a drop of shear stresses (Figure 1A). In gravelly streams, such a situation could result in the deposition of clasts. In such a scenario, the site where sediment accumulates most likely migrates upstream (Figure 8).

Inspections of modern gravel bars in the Central European Alps and of stratigraphic records (Figure 4) reveal the occurrence of imbrications where channel slopes are steeper than 0.4°–0.5°, and where the values of bed roughness exceed c. 0.06. The results of our generic calculations (Figure 3) reveal that under these circumstances, flows might become supercritical provided that φ-values are greater than c. 0.05 (Figure 3). This is supported by observations from the Waldemme and Reuss Rivers (slope >0.5°) during high stage and low stage flows (Figures 5B and 6B) that provide evidence for standing waves and thus supercritical flows. Contrariwise, the reach of the Emme River is flatter (slope <0.4°), imbrications are largely absent, and flows generally occur in the lower flow regime (Sprecacio et al., 2001, p. 53). We thus propose that a channel gradient of c. 0.5° is critical for both the formation of clast imbrications and possibly also for the establishment of supercritical flows. Based on these relationships, we also suggest that the generation of imbrications may be associated with upper flow regime conditions.
The proposed threshold slope is consistent with the results of previous work, where upper flow regime bedforms such as transvers ribs have been described for e.g., the Peyto Outwash (slope c. 1.09°), the Spring Creek (same slope; McDonald and Banerjee, 1971), and the North Saskatchewan River (slope 0.52°; Dept. Mines and Tech. Survvs., 1957). This is also in agreement with observations (Mueller et al., 2005) and the results of theoretical work calibrated with data (Lamb et al., 2008). In particular, Mueller et al. (2005) suggested that a $\phi$-value of c. 0.03 is suitable for slopes <0.35°, while $\phi > 0.1$ might be more appropriate for the mobilization of coarse-grained sediment particles in channels steeper than 1.1°. This might be an overestimate of the $\phi$-dependency of slope (Lamb et al., 2008), but it does show that $\phi$-values larger than the commonly used $\phi$-values between 0.04 and 0.05 might be appropriate where channels are steep (see also Ferguson, 2012). Finally, Simons and Richardson (1960, p. 45) noted that flows rarely exceeded unity Froude numbers over an extended period of time in a stream with erodible banks. We thus use the conclusion of their discussion to explain the limited spatial extent of individual ensembles of imbricated clasts in modern streams and stratigraphic records.

5 Summary and conclusions

We started with the hypothesis that the transport and deposition of coarse-grained particles, and particularly the formation of an imbricated fabric, may be related to changes in flow regimes. We then calculated the Froude number $F$ at conditions of incipient motion of coarse-grained bedload for various bed roughness and stream gradient values, and we compared the results with data from modern streams and stratigraphic records. The results suggest that imbricated clasts are likely to provide evidence for the occurrence of supercritical conditions, particularly at sites where channel gradients are steeper than ~0.5° and where $\phi$-values are greater than c. 0.05. We do acknowledge that our field-based inferences are associated with large uncertainties regarding channel gradients and grain size (Litty and Schlunegger, 2017), and that they lack a quantitative measure of the spatial distribution of clast imbrications and clast arrangements (Bertin and Friedrich, 2018). In the same sense, the hydrologic calculations and force balancing approaches are based on the simplest published expressions where water flow is related to sediment transport. Larger complexities, which complicate any considerations of material transport (Engelund and Hansen, 1967), have not been considered. This includes, for instance, large supply rates of sediment (van der Berg and Schlunegger, 2012; Bekaddour et al., 2013), changes in bed morphology, spatial variations in turbulence, the shape and the sorting of grains, the 3D arrangement of clasts (Lamb et al., 2008; Hodge et al., 2009), and more complex hydrological conditions including upper-stage plain beds, hydraulic drops, and standing waves (Johansson, 1963). In addition, the occurrence or absence of imbrications also strongly depends on the shape of the involved clasts (Carling et al., 1992). In particular,
clasts with a relatively large c-axis tend to form steeper imbrications compared to those constituents where the c-axis is short. In addition, experimental results of Hattingh and Illenberger (1995) showed that spheres and rods have a higher mobility than blades and discs, which is explained by differences in the related lift and drag forces exerted on each shape-type together with the angle of repose and pivotability of these shape types. Unfortunately, we lack the quantitative dataset to properly address these points. We also acknowledge that imbrications do form during subcritical flows in flume experiments at conditions, which can be characterized by low $\phi-$values (Brayshaw, 1984; Carling et al., 1992; Powell et al., 2016; Lamb et al., 2017). However, as already noted above, we find it quite hard to upscale the experimental results (<20 meters) to the reach scale of our observations where standing waves with wavelengths as long as 8 meters have been observed (Figure 6B).

Despite our simplifications, we find evidence for proposing that clast imbrications are likely to be associated with supercritical flows provided that (i) channel gradients are steeper than c. 0.5°±0.1°, and (ii) large clasts are tightly packed, closely arranged as cluster bedforms and partly embedded in finer-grained sediment. Mobilization and rearrangements of these structures require larger thresholds (Brayshaw, 1985), which might be large enough ($\phi-$values possibly >0.05) to allow supercritical conditions to occur. These findings might be useful for the quantification of hydrological conditions in coarse-grained stratigraphic archives such as conglomerates. As a further implication, the occurrence of imbrications in clastic sediments may be used to infer a minimum value of 0.5°±0.1° for the palaeo-topographic slope. Such a constraint might be beneficial for palaeo-geographic reconstructions and for the analysis of a basin’s subsidence history through the back-stripping of strata (e.g., Schlunegger et al., 1997). Finally, for modern streams, the presence of imbrications on gravel bars with closely packed clasts might be more conclusive for inferring an upper flow regime upon material transport than other bedforms such as transverse ribs or antidunes (Koster, 1978; Rust and Gostin, 1981), mainly because clast imbrications have a better preservation potential and are easier to recognize in the field.

**Figure captions**

Figure 1: **A)** Photo showing hydraulic jump, and conceptualization of situation displayed in photo of Figure 1A. $F=Fro\text{u}\text{d}e$ number; $v=flow$ velocity, $d=water$ depth. **B)** Photo from Sense River, and cross-sections through reaches with upper and lower flow regimes. Surface waves ($\lambda=20-30$ cm) tend to fade out towards the upstream direction relative to the flow movement where subcritical flows prevail (section to the left). A hydraulic jump separates segments with a supercritical flow from reaches with a subcritical flow where the bedrock builds a ramp. The
reach illustrated by the section to the right is characterized by standing waves with wavelengths $\lambda = 100$ cm. The dashed line illustrates the trace of the plane that separates lower from upper regime flows. Please see Figure 2 for location of photo.

Figure 2: Sites where modern gravel bars in streams were inspected for the occurrence of clast imbrications (blue dots). The figure also shows the locations of the stratigraphic sections where conglomerates were analyzed for their sedimentary structures. $S=$Sense; $E=$Emme; $WE_{L}=Waldemme$, $WL=Waldemme$ at Littau, $R=$Reuss; $L=$Landquart; $G=Glenner$, $M_{b}, M_{v}$, $M_{l}=Maggia$ at Bignasco, Visetello and Losone; $V_{r}, V_{m}, V_{c}=Verzasca$ at Frasco, Motta and Lavertezzo. See Table 1 for coordinates of sites.

The black squares are sites where Spreafico et al. (2001) have estimated channel gradients and Froude numbers for low and high-stage flows. $b=$Birse-Moutier, $e=$Emme-Burgdorf, $g=Glatt-Fällanden$, $g=Glatt-Fällanden$, $g=Glatt-Fällanden$ at Bignasco, Visetello and Losone; $V_{r}, V_{m}, V_{c}=Verzasca$ at Frasco, Motta and Lavertezzo. See Table 1 for coordinates of sites.

Figure 3: Relationships between A) channel slope and Froude number $F$, and B) relative bed roughness and $F$. These were calculated as a function of various Shields (1936) variables $\phi$. The pale green field indicates the conditions where an upper flow regime could prevail, while the yellow field delineates the occurrence of lower flow regime conditions. In this context, we set the threshold to a Froude number of c. 0.9. This is consistent with the estimation of parameters for the formation of upper flow regime bedforms by Koster (1978). Note that the bed roughness is the ratio between the $D_{50}$ and the water depth $d$ at the incipient motion of that particular size class. The vertical bars on Figure 3A also illustrate the Froude numbers that have been estimated by Spreafico et al. (2001) for the following streams and locations: $b=$Birse-Moutier, $e=$Emme-Burgdorf, $g=Glatt-Fällanden$, $g=Glatt-Fällanden$, $g=Glatt-Fällanden$, $g=Glatt-Fällanden$ at Bignasco, Visetello and Losone. Please note that the low values for the Thur and Birse Rivers might represent underestimates as these streams show evidence for multiple hydraulic jumps during high stage flows.

Figure 4: This figure relates the occurrence of imbrications (blue bars) or no imbrications (red bars) to A) channel slopes and B) relative bed roughness. Red bars with blue hatches indicate that imbrications have been found in places. Blue bars with red hatches suggest that imbrications dominate the bar morphology, but that reaches without imbrications are also present on the same gravel bar. Data from modern streams are displayed above the horizontal axes, while
information from stratigraphic sections are placed below the slope and roughness axes, respectively. \( S = \text{Sense, } S' = \text{Sense with bedrock reach, } \\
E = \text{Emme, } WE = \text{Waldemme, } WL = \text{Waldemme at Littau, } \\
L = \text{Landquart, } G = \text{Glenner, } M_b, M_v, M_l = \text{Maggia at Bignasco, Visletto and Losone; } \\
V_b, V_M, V_L = \text{Verzasca at Frasco, Motta and Lavertezzo. See Table 1 for } \\
coordinates of sites, and Figure 2 for locations where data were collected.

**Figure 5**  A) Reuss River with evidence for standing waves along the thalweg. Othophoto reproduced by permission of swisstopo (BA 18065). Please see Figure 2 for location.  B) Transverse and lateral bars in the Reuss River with imbricated clasts on the lateral bar forming a riffle, and standing waves where the thalweg crosses the riffle. The wavelength of the standing wave is c. 5 m. Arrow indicates flow direction. Please see Figures 2 and 5A for location of photo.

**Figure 6:** Photos from the field.  A) Photo of subaquatic longitudinal bar taken along the steep bedrock/gravel bar reach of the Sense River (see Figure 1B for location of photo). The clasts in the foreground are clustered and imbricated, forming the nucleus of a possible cluster bedform. This fabric most likely formed when rolling clasts came to a halt behind the boulder at the front. The clasts in the background are either flat lying or slightly imbricated. Except for a few sites, nearly all grains are either partially buried by finer grained material or interlocked by neighboring clasts. The overlying flow shows evidence for supercritical conditions with standing waves.  B) Standing waves with a wavelength of c. 8 m in the Waldemme at Littau. Water fluxes are c. 100 m$^3$/s. Arrow indicates flow direction.  C) Flat lying clasts on a lateral bar in the Sense River. Arrow indicates clasts that are overlapping each other, resulting in a shallow dip of <10° of the overriding clast.  D) Imbricated clasts within the Maggia River at Visletto. Arrow indicates flow direction. Please note that the imbricated arrangements of clasts mainly include the largest constituents of the gravel bar in the middle of the photo, and clasts of similar sizes. Therefore, for this set of imbricated clasts, we do not consider that protrusion effects might play a major role. See Figure 2 for location and Table 1 for coordinates.

**Figure 7:**  A) Conglomerates at Rigi with no evidence for clast imbrications. White lines indicate the orientation of the bedding.  B) Conglomerates at Rigi with imbricated gravels to cobbles that are arranged as cluster bedforms (C). Arrow indicates paleoflow direction. White line refers to the bedding. Note that the steep dip (>25°) of the a-b-planes of the imbricated clasts. See Figure 2 for location and Table 1 for coordinates.
Figure 8: Conceptual sketch illustrating the formation of an ensemble of imbricated clasts as time proceeds (A through C). According to this model, the site of sediment accumulation will migrate upstream. \( F = \text{Froude number}; v = \text{flow velocity}, d = \text{water depth}. \)

Table 1: Grain size and observational data and that have been collected in the field. See text for further explanations.

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Author contribution

FS designed the study and carried out the calculations, PG and FS collected the data, FS wrote the text with contributions by PG, both authors contributed to the analyses and discussion of the results.

Data availability

The authors declare they have no conflict of interest.

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Figure 1

Hydraulic jump

$F < 1$

$F \geq 1$

Imbricated clasts

A

Flow direction

Fig. 6A

B

Figure 1
Figure 3
Figure 4

Color legend for modern sediments:
- Full imbrication
- >10 groups of imbricated clasts per 10 m²
- c. 5 groups of imbricated clasts per 10 m²
- No imbrication

Color legend for stratigraphic archives:
- Full imbrication
- No imbrication
Figure 5
Figure 6
Figure 8

Hydraulic jump

A

Hydraulic jump

B

Hydraulic jump

C

Imbricated clasts

Figure 8

$F \geq 1$

$F < 1$

$F \geq 1$

$V_3$

$V_2$

$V_3'$

$V_2'$

$F \geq 1$

$F < 1$

$F \geq 1$
### Modern gravel bars

| Site name | Site coordinates | DEM cotds | OIS cotds | DEMDQD | DMD cotds | Gradient (\%) | Gradient (\%) | Inferred water depth (m) | Roughness | Intensive
|-----------|-----------------|-----------|-----------|---------|-----------|---------------|---------------|--------------------------|-----------|---------|
| Flame E   | 41°29'11"N 7°14'58"W | 2.3       | 5.2       | 0.006-0.098 | 0.081-1 | 0.06-0.10 | 0.07-0.1 | 0.07-0.10 | Intensive
| Glennes G | 41°44'24"N 7°55'19"W | 12        | 58        | 0.009-0.138 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | Intensive

### Landscapes

| Study area | Site coordinates | DEM cotds | OIS cotds | DEMDQD | DMD cotds | Gradient (\%) | Gradient (\%) | Inferred water depth (m) | Roughness | Intensive
|------------|-----------------|-----------|-----------|---------|-----------|---------------|---------------|--------------------------|-----------|---------|
| Landon | 41°27'35"N 7°45'36"W | 10        | 3.5       | 0.006-0.095 | 0.081-1 | 0.06-0.10 | 0.07-0.1 | 0.07-0.10 | Intensive
| Wix | 41°42'34"N 7°30'30"W | 10.7      | 5.6       | 0.009-0.138 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | Intensive

### Vegetation

| Study area | Site coordinates | DEM cotds | OIS cotds | DEMDQD | DMD cotds | Gradient (\%) | Gradient (\%) | Inferred water depth (m) | Roughness | Intensive
|------------|-----------------|-----------|-----------|---------|-----------|---------------|---------------|--------------------------|-----------|---------|
| Flame E   | 41°29'11"N 7°14'58"W | 2.3       | 5.2       | 0.006-0.098 | 0.081-1 | 0.06-0.10 | 0.07-0.1 | 0.07-0.10 | Intensive
| Glennes G | 41°44'24"N 7°55'19"W | 12        | 58        | 0.009-0.138 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | Intensive

### Vegetation Laverocken

| Study area | Site coordinates | DEM cotds | OIS cotds | DEMDQD | DMD cotds | Gradient (\%) | Gradient (\%) | Inferred water depth (m) | Roughness | Intensive
|------------|-----------------|-----------|-----------|---------|-----------|---------------|---------------|--------------------------|-----------|---------|
| Flame E   | 41°29'11"N 7°14'58"W | 2.3       | 5.2       | 0.006-0.098 | 0.081-1 | 0.06-0.10 | 0.07-0.1 | 0.07-0.10 | Intensive
| Glennes G | 41°44'24"N 7°55'19"W | 12        | 58        | 0.009-0.138 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | Intensive

### Exposed

| Study area | Site coordinates | DEM cotds | OIS cotds | DEMDQD | DMD cotds | Gradient (\%) | Gradient (\%) | Inferred water depth (m) | Roughness | Intensive
|------------|-----------------|-----------|-----------|---------|-----------|---------------|---------------|--------------------------|-----------|---------|
| Flame E   | 41°29'11"N 7°14'58"W | 2.3       | 5.2       | 0.006-0.098 | 0.081-1 | 0.06-0.10 | 0.07-0.1 | 0.07-0.10 | Intensive
| Glennes G | 41°44'24"N 7°55'19"W | 12        | 58        | 0.009-0.138 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | Intensive

### Stenographic archives

| Study area | Site coordinates | DEM cotds | OIS cotds | DEMDQD | DMD cotds | Gradient (\%) | Gradient (\%) | Inferred water depth (m) | Roughness | Intensive
|------------|-----------------|-----------|-----------|---------|-----------|---------------|---------------|--------------------------|-----------|---------|
| Flame E   | 41°29'11"N 7°14'58"W | 2.3       | 5.2       | 0.006-0.098 | 0.081-1 | 0.06-0.10 | 0.07-0.1 | 0.07-0.10 | Intensive
| Glennes G | 41°44'24"N 7°55'19"W | 12        | 58        | 0.009-0.138 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | 0.10-0.13 | Intensive

Table 1